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# Chirped Pulse Fourier Transform Microwave Spectroscopy of Nitrogen-Containing Organic Molecules 

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#### Abstract

Chirped Pulse Fourier Transform Microwave (CP-FTMW) spectroscopy is a powerful analytical technique. Its versatile applications include molecular structure determination, generating molecular rotational signatures for astrochemistry and probing weak inter- and intra-molecular interactions as well as large amplitude motions. For this thesis, experiments were performed with the CP-FTMW Spectrometer at Newcastle University operating in the $2.0-18.5 \mathrm{GHz}$ region, featuring a pulsed valve for supersonic expansion and a laser ablation source for gas-phase generation of non-volatile species.

The microwave spectra of i) phosphine-carboxamide and a van der Waals complex with argon, ii) two monohydrate isomers of imidazole, iii) methylimidazole isomers and iv) monohydrate complexes of methylimidazole isomers are reported and analyzed. Molecular rotations probed in the microwave spectra are directly correlated to the geometry of these species. Detection of isotopologues, in natural isotopic abundance or by using isotopically enriched samples, allows for full or partial structure determination and rationalization of large amplitude motions.

Phosphine-carboxamide is a phosphorus-bearing analogue of urea. Coordination of an argon atom highlights that the electronic density is concentrated at the amide site. The monohydrate complexes of imidazole exhibit bifunctional hydrogen bonds with imidazole acting either as a proton donor or acceptor. The spectra of methylimidazole isomers exhibit internal rotation of the $\mathrm{CH}_{3}$ group in each isomer. The relative energy required to surmount the barrier to internal rotation in each isomer is relatable to the position where the $\mathrm{CH}_{3}$ substitutes on the imidazole ring. The barrier depends on the chemical environment and orbital overlap between the $\mathrm{CH}_{3}$ group and the adjacent C-H bonds. In the monohydrate complexes of methylimidazole only one type of hydrogen bonding was detected and internal rotation of $\mathrm{CH}_{3}$ group was observed. Results are supported by ab initio and density functional theory (DFT) calculations.


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Properties of relevant nuclei reproduced from the IUPAC Green Book.

| Atomic number $Z$ | Element <br> symbol | Mass <br> number $A$ | Atomic mass $\frac{m_{a}}{u}$ | Isotopic <br> abundance <br> $100 x$ | Nuclear <br> spin $I$ | Quadrupole <br> moment $\frac{Q}{f m^{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | H | 1 | $1.00782503207(10)$ | $99.9885(70)$ | $+1 / 2$ |  |
| 6 | (D) | 2 | $2.0141017778(4)$ | $0.0115(70)$ | +1 | $+0.286(2)^{* *}$ |
|  | (T) | $3^{*}$ | $3.0160492777(25)$ |  | $+1 / 2$ |  |
| 7 | C | 12 | $12($ by definition) | $98.93(8)$ | +0 |  |
|  |  | 13 | $13.0033548378(10)$ | $1.07(8)$ | $-1 / 2$ |  |
| 8 | N | 14 | $14.0030740048(6)$ | $99.636(20)$ | +1 | $+2.001(10)$ |


| 12 | Mg | 24 | $23.985041700(14)$ | $78.99(4)$ | +0 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 25 | $24.98583692(3)$ | $10.00(1)$ | $+5 / 2$ | $+19.9(2)^{* *}$ |
|  |  | 26 | $25.982592929(30)$ | $11.01(3)$ | +0 |  |
| 15 | P | 31 | $30.97376163(20)$ | 100 | $+1 / 2$ |  |
|  | Ar | 36 | $35.967545106(29)$ | $0.3365(30)$ | +0 |  |
| 29 |  | 38 | $37.9627324(4)$ | $0.0632(5)$ | +0 |  |
|  |  | 40 | $39.9623831225(29)$ | $99.6003(30)$ | +0 |  |

*Asterisk denotes an unstable nuclide (for elements without naturally occurring isotopes it is the most stable nuclide).
** Under quadrupole moment, double asterisk indicates that more than one value is given in the original compilation.

## Publications

Molecular geometries and other properties of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{AgI}$ and $\mathrm{H}_{3} \mathrm{~N} \cdots \mathrm{AgI}$ as characterized by rotational spectroscopy and Ab Initio calculations; Chris Medcraft, Eva Gougoula, Dror M. Bittner, John Mullaney, Susana Blanco, David P. Tew, Nicholas R. Walker, and Anthony C. Legon, The Journal of Chemical Physics, 147, 234308 (2017)

A chalcogen-bonded complex $\mathrm{H}_{3} \mathrm{~N} \cdots \mathrm{~S}=\mathrm{C}=\mathrm{S}$ formed by ammonia and carbon disulfide characterized by chirped-pulse broadband microwave spectroscopy; Eva Gougoula, Chris Medcraft, Ibon Alkorta, Nicholas R. Walker, and Anthony C. Legon, The Journal of Chemical Physics, 150, 084307 (2019)

Conformational isomers of trans-urocanic acid observed by rotational spectroscopy; Graham A. Cooper, Chris Medcraft, Eva Gougoula, and Nicholas R. Walker, Physical Chemistry Chemical Physics, 21, 9495 (2019)

Barrier to Internal Rotation in Methylimidazole Isomers Determined by Rotational Spectroscopy; Eva Gougoula, Chris Medcraft, Julianne Heitkämper and Nicholas R. Walker, Journal of Chemical Physics, 151, 144301 (2019)

A Chalcogen-Bonded Complex $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N} \cdots \mathrm{~S}=\mathrm{C}=\mathrm{O}$ characterized by Rotational Spectroscopy, Eva Gougoula, Joe A. Moxon, Nicholas R. Walker and Anthony C. Legon, Chemical Physics Letters, (2020)

Bifunctional Hydrogen Bonding of Imidazole with Water Explored by Rotational Spectroscopy and DFT Calculations; Eva Gougoula, Daniel J. Cole and Nicholas R. Walker, Journal of Physical Chemistry A, 124, 2649 (2020)

## Oral Presentations

Chirped-Pulse Fourier Transform Microwave Spectroscopy; Eva Gougoula and Nicholas R. Walker, Annual Northern Universities Meeting on Chemical Physics, Manchester Metropolitan University, July 2018

Barriers to Internal Rotation and Water/Argon Complex Formation in Methylimidazoles by Broadband Rotational Spectroscopy; Eva Gougoula and Nicholas R. Walker, The University of Nottingham, January 2019

Broadband Rotational Spectroscopy at Newcastle University; Eva Gougoula and Nicholas R. Walker, Newcastle University, May 2019

Barriers to Internal Rotation in Structural Isomers of Methylimidazole; Eva Gougoula, Chris Medcraft, Julianne Heitkämper and Nicholas R. Walker, University of Illinois, June 2018

A chalcogen-bonded complex $\mathrm{H}_{3} \mathrm{~N} \cdots \mathrm{~S}=\mathrm{C}=\mathrm{S}$ formed by Ammonia and Carbon Disulphide and characterised by Broadband Rotational Spectroscopy; Eva Gougoula, Chris Medcraft, Ibon Alkorta, Nicholas Walker and Anthony C. Legon, University of Illinois, June 2019

## Poster Presentations

Broadband Rotational Spectrum of 5-Nitroimidazole and 2-Methyl-5-Nitroimidazole; Eva Gougoula and Nicholas R. Walker, University of Durham, January 2018

Fourier Transform Microwave Spectroscopy at Newcastle University; Eva Gougoula and Nicholas R. Walker, Newcastle University, May 2018

Barriers to Internal Rotation in Methylated Imidazoles Determined by Rotational Spectroscopy; Eva Gougoula and Nicholas R. Walker, Uiversidad del Pais Vasco, September 2018

## Chapter 1. Introduction

Observation of light through prisms traces back to the Roman times. ${ }^{1}$ The first systematic observations of light, however, only took place in the $17^{\text {th }}$ century when optics technology began to evolve. ${ }^{2}$ The idea that white light is comprised by its color components was established with new experiments and improved instrumentation. The main source of light of interest at the time was the sun; soon it was discovered that dark bands exist between the color components of the light emitted by the sun. ${ }^{3,4}$ It was later found that chemical elements absorbed light at the position of the dark bands, suggesting that other chemical constituents can absorb light of specific wavelength, too. As technology advanced, invisible light was discovered, ${ }^{5-7}$ and the representation of the electromagnetic spectrum as known today was constructed, ${ }^{8}$ Quantum mechanical principles were in place to rationalize the observed behavior of light absorbed and emitted by chemical compounds. ${ }^{9}$

The systematic observation of the interaction of electromagnetic radiation emitted or absorbed by matter is known as spectroscopy. Different types of radiation will prompt a different type of response in a molecule, e.g. UV light may be absorbed by a molecule and result in fluorescence emission of visible light. Radiation in the $1-300 \mathrm{GHz}$ frequency region, known as microwave (MW) radiation, which is invisible, is associated with molecular rotations. ${ }^{9}$ Molecular rotations are directly linked to the molecular structure of the rotating molecule. This makes MW spectroscopy a powerful and sensitive tool in structure determination. The technique is structure specific as it can distinguish between species with the same chemical compositions (i.e. methylimidazole isomers, ${ }^{10}$ chapter 6), the same molecular weight (imidazole ${ }^{11}$ and pyrazole ${ }^{12}, 68 \mathrm{~g} \mathrm{~mol}^{-1}$ ) and isotopologues of the same species $\left({ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}\right.$ phosphine carboxamide, chapter 4$)$. Microwave spectroscopy finds applications in molecular structure determination, ${ }^{13,14}$ separation of enantiomers, ${ }^{15-17}$ study of transient and exotic species, ${ }^{18}$ analysis of conformational landscapes, ${ }^{19,20}$ monitoring of molecular processes, ${ }^{21}$ generation of fingerprint spectra for astrochemistry ${ }^{22}$ and benchmarking of quantum chemical calculations. ${ }^{23}$

### 1.1 Brief History of the technique

The first experiment using MW radiation was conducted by Cleeton and Williams ${ }^{24}$ in 1934. The MW spectrum of ammonia was recorded in the $1-4 \mathrm{~cm}^{-1}$ region. The inversion vibrational mode of ammonia was probed using a gas cell and a custom-made vacuum magnetron oscillator to generate MW radiation. During WW2 it became necessary to develop more powerful sources of MW radiation as part of radio detection and ranging (RADAR). Klystron sources began to systematically be used in research experiments after WW2 and a series of experiments around ammonia and other molecules were performed.

The need to study transient and short-lived species led to the implementation of supersonic expansion sources. Advances in electronics and vacuum technology in the 1970's made it possible to perform experiments with pulsed supersonic jets containing the gas sample of interest interrogated by pulses of MW radiation. This technique, ${ }^{25}$ first used by Ekkers and Flygare, offers the advantage of generating internal temperatures as low as a few Kelvin and shifting the population to low energy rotational states. As a result, these low energy rotational transitions are observed with high intensity. Measuring molecular emissions in the time domain and Fourier transforming to the frequency domain greatly improved the spectral resolution and signal to noise of measured spectra. Supersonic expansion also allows for isolation of complexes and clusters that are stable at low temperatures but dissociate at room temperature, and as such makes them accessible to study.

Balle and Flygare introduced a spectrometer ${ }^{26}$ utilizing pulsed supersonic expansion and MW radiation. MW pulses broadcast into a resonant Fabry-Perot cavity and polarize the molecular ensemble in the supersonic jet. The main limitation of that spectrometer is the bandwidth ( $\sim 1 \mathrm{MHz}$ ) that can be scanned at once. In 2008, the Chirped Pulse Fourier transform microwave (CP-FTMW) spectrometer was a breakthrough in the field. ${ }^{27}$ The spectrometer features an arbitrary waveform generator (AWG) which directly creates chirped MW pulses and allows large bandwidths up to 12 GHz to be scanned at a single spectral acquisition. Travelling wave tube (TWT) amplifiers provide sufficient power to polarize across the entire bandwidth with few losses. The CP-FTMW spectrometer at Newcastle University is based on that design and operates in the $2.0-18.5 \mathrm{GHz}$ frequency range. More information on this design will be given in chapter 3 .

Given that microwave spectroscopy is a gas phase technique, the need to study non-volatile molecules made it necessary to reconsider the available experimental methods for gas
phase generation. In the 1950's, ovens were used to generate vapor of species containing refractory metals, ${ }^{28}$ Heated reservoirs ${ }^{29}$ before or right after the pulse valve, allow relatively large molecules to get into the gas phase. This technique requires the molecule of interest to be placed into a reservoir and whilst heated, the carrier gas passes over and seeds the vapor toward the pulse valve. However, this method may not be suitable for biomolecules as they tend to decompose even at low temperatures $\left(50-60^{\circ} \mathrm{C}\right)$ and metals or other solids with high melting points. As an alternative, laser vaporization methods ${ }^{18,30,31}$ may be used that allow rapid gas phase generation of molecules from a solid target without destroying the molecular structure. Pulsed Nd:YAG lasers are the most common ones used for this purpose and there is a number of spectrometers around the world that use this technique. Laser vaporization has allowed for observation of metal containing clusters, ${ }^{18}$ study of aminoacids ${ }^{32,33}$ and other biomolecules, ${ }^{11,31,34}$ weakly bound complexes between biomolecules and other smaller molecules ${ }^{35,36}$ and formation of exotic species ${ }^{37}$ like $\mathrm{C}_{60}$.

### 1.2 Astrochemistry

Historically, space exploration has always been intriguing and the first observations of stellar objects date thousands of years back. In the 1860's, light emitted by stars revealed that the same elements found on the Earth are also components in stellar regions. The extreme conditions of interstellar space led scientists to believe that atomic elements would be the only species that could survive those environments of ionizing radiation and low temperature. Radioastronomy is a theme that emerged in 1970's and has been a breakthrough to our understanding of space and its complexity. The first molecule to be discovered in the interstellar medium (ISM) was the $\mathrm{CH}^{\cdot}$ radical, ${ }^{38}$ detected through an electronic transition at $430 \mathrm{~nm}(700 \mathrm{THz})$. More than 200 molecules have been detected in the ISM, with that number increasing every year; most of these molecules were detected by means of their microwave spectra. The first detection of a polyatomic molecule in the ISM was in 1968 by Cheung and co-workers, ${ }^{39}$ The team discovered ammonia by detection of its microwave spectrum coming from the center of the galaxy.

A crucial part of the process of detecting molecules in the ISM is the generation and understanding of high-quality, microwave molecular laboratory spectra. These spectra are the molecular fingerprints and will drive the assignment of lines measured by radiotelescopes to the correct molecular carrier. Observation of rotational spectral features of a molecular carrier will lead to unambiguous assignment and confirm its presence in a given interstellar environment. Recent detections are concerned with benzonitrile ${ }^{40}$ and urea. ${ }^{41}$ Benzonitrile is the first aromatic molecule to be detected in the ISM, and its detection supports the assumption that polyaromatic hydrocarbons (PAH's) are abundant in space. Generally, it is thought that diffuse interstellar bands ${ }^{42}$ are due to PAH's, however, a definite and explicit assignment is challenging. Detecting PAH's via their MW spectrum has so far been unsuccessful due to their low electric dipole moment. Urea was only recently confirmed after tentative and inconclusive assignments. ${ }^{43}$ Given the importance of urea in biological systems, its discovery in space gives an insight into life formation on earth.

In a typical astronomical measurement, spectral features that remain unassigned are usually present. A challenge that astronomers are faced with when it comes to these features is the lack of laboratory spectroscopic data of the corresponding molecular carriers that may give rise to these features. Simulating the extreme environments of interstellar space with low temperature and low or high density is also challenging for laboratory
molecular spectroscopists. Exploiting techniques like the electrical discharge source used in Hamburg in conjunction with a millimeter-wave spectrometer ${ }^{44}$ and laser vaporization techniques like at Newcastle University may allow for simulation of conditions suitable for ion-neutral or neutral-neutral reactions and potentially identify new candidate molecules.

The microwave spectrum of laser vaporized phosphine carboxamide, ${ }^{45}$ a phosphorus analogue of urea, is discussed in chapter 4. Considering the recent discovery of urea, this molecule may be a potential candidate molecule for interstellar detection. A total of six phosphorus-containing molecules have been detected in space. It is unclear where the phosphorus reservoirs in the ISM are and as such limited information is available on the gas phase chemistry of phosphorus. A remarkable example of the unknown and unexpected chemistry of phosphorus is the recent discovery of phosphine gas in the middle atmosphere of Venus by means of its rotational spectrum. ${ }^{46}$ On Earth, phosphine is entirely associated with biological and anthropogenic activity and other pathways for its formation would likely require high pressures and temperatures and high concentration of $\mathrm{H}_{2}$. The middle atmosphere of Venus does not fulfill these conditions and presence of phosphine suggests it is formed via pathways that have not been considered or via biotic mechanisms. Chapter 4 of this thesis is the beginning of the exploration of organo-phosphorus chemistry in the gas phase. Broadband rotational spectra that extend into the millimeter-wave region may identify reaction products and shed some light on the rich and complex chemistry of phosphorus in the gas phase.

### 1.3 Hydrogen Bonding of Biomolecules (Microsolvation)

The structure of a biomolecule is strongly linked to its properties and biochemical activity. Distinct chemical sites will favor formation of certain intermolecular interactions, the most common one being hydrogen bonding. ${ }^{47}$ Molecules such as amino acids are expected to interact with other molecules like water and other biomolecules in the body. Understanding how larger systems like proteins and lipids interact (conformational and bonding preferences) can be challenging. It is therefore important to establish good understanding around fundamental preferences in bonding and activity by studying the "building blocks" of these larger systems, i.e. imidazole is the building block of histidine, ${ }^{31}$ histamine, ${ }^{48}$ adenine, ${ }^{34}$ and various synthetic drugs. ${ }^{49-52}$

The first studies of intermolecular hydrogen bonds were conducted in the 1970's. The detection of the water dimer ${ }^{53}$ was one of them and it was significant to establish the donoracceptor properties of water on a macroscopic scale by probing an isolated neutral cluster. Since then, larger clusters of pure water ${ }^{13,54-59}$ have been detected by means of gas phase rotational spectroscopy. The fact that water is abundant and essential for life formation steered research to the direction of exploring gas phase metal-water complexes as well as weakly bound complexes between water and biomolecules. Experiments identified complexes between water and metal halides ${ }^{18,60,61}$ and ion metal monohydrates. ${ }^{62}$

MW spectroscopy has been concerned with this field for many years, offering an insight into structure and bonding properties by probing the neutral molecules in an environment free of solvent and lattice effects. This is particularly useful considering that other spectroscopic methods like mass spectrometry and IR dissociation spectroscopy are concerned with the corresponding ion of the molecule of interest. For biomolecules, the surrounding aqueous environment may have a crucial influence on the molecular structure and functionality. This is the so-called solution phase and the molecular behavior in solution may be correlated to the gas phase behavior by means of MW spectroscopy and supersonic expansion methods. Microsolvated complexes of biomolecules, ${ }^{21,63-65}$ i.e. incrementally encapsulating a solute by solvent molecules, may be formed and probed in a supersonic expansion when both molecules of interest are present. MW spectroscopy is able to detect subtle changes in the structure of the biomolecule induced by attachment of one or more water molecules ${ }^{66}$ and vice versa; perturbation in the hydrogen bond network formed between the water molecules induced by the biomolecule.

Formamide is a molecule that can form similar hydrogen bonds as those between amino acids in the backbone of proteins and water. The progressive microsolvation of formamide in the gas phase has been studied with rotational spectroscopy to help understand the effects of intermolecular interactions on protein folding, molecular shape, and conformational equilibrium. Various isomers of the monohydrate of formamide were identified. It was shown that the isomer where cooperative hydrogen bonding leads to a pseudo six-membered ring between the carbonyl and amine sites of formamide and water is the most stable one. The water molecule can act both as a proton donor and acceptor by forming hydrogen bonds through the hydrogen and oxygen atoms, respectively. Incrementally adding water molecules to the microsolvated clusters of formamide (formamide- $\left(\mathrm{H}_{2} \mathrm{O}\right)_{\mathrm{n}}, \mathrm{n}=1,2,3$ ) was shown to result in stronger hydrogen bonds between the oxygen of the carbonyl of formamide and the hydrogen of a water molecule. Similar bond shortening was observed for the amine site too.

The cooperative hydrogen bonding as well as the bifunctional character of water in forming hydrogen bonds will be discussed in chapter 5 in the context of hydrogen bonded complexes between imidazole and water. A previous study with FT-IR spectroscopy in helium identified one isomer of a complex between imidazole and water ${ }^{67}$ in which the water molecule is the hydrogen bond donor. An IR laser spectroscopy study in helium droplets detected two isomers of a water-imidazole complex, ${ }^{68}$ one of them being common in both studies and one where the water is the hydrogen bond acceptor. The bonding manner was identified in both studies; however, due to the limitations of these methods, a precise insight into the length of the hydrogen bond and the orientation of the two molecules with respect to each other is not given. Structural parameters of those complexes are determined directly from the MW spectra of those isomers and discussed in chapter 5 . Monohydrates of various five-membered heteroaromatic rings will also be discussed in chapter 5 .

Probing the initial steps of the microsolvation of a biomolecule is not always straightforward and the majority of studies have been concerned with one, two or three water molecules. However, the first steps of microsolvation in the gas phase will not necessarily give an insight into the structure and function of a microsolvated molecule in the solution phase. Incremental addition of water molecules to a microsolvated cluster is crucial but can be challenging and at risk of compromising the information that can be derived from the rotational structure (rotational resolution may collapse as cluster becomes heavier).

### 1.4 Internal Motions

MW spectroscopy has been an invaluable tool in studying internal motions in molecules and complexes. The internal motions this thesis will be concerned with are internal rotation of $\mathrm{CH}_{3}$ groups attached to a molecular framework ${ }^{69-71}$ (i.e. $N$-methylimidazole, chapter 6) and large amplitude motions (LAM) in the water molecule attached to biomolecules ${ }^{72,73}$ (i.e. water imidazole, chapter 5). Internal motions can couple with the overall molecular rotation and cause certain effects in the MW molecular spectra of a species. Typically, rotational transitions will be split into fine sub-components. The energy difference of these components is sensitive to the potential hindering barrier to the internal motion. It is possible to observed and evaluate these effects with CP-FTMW spectroscopy and thermodynamic methods. ${ }^{9}$ The latter are suitable for molecules with high barriers in the range of $1000 \mathrm{~cm}^{-1}$ and molecules with no dipole moment. However, this is beyond the scope of this thesis and will not be discussed further.

Probing and understanding internal motions in a molecule or complex may give an insight into its structure and the nature of the intra- and inter-molecular interactions, respectively. For example, internal motions at the water subunit of the water-imidazole complex in chapter 5 are manifested as splitting of the rotational transitions indicating a change in the moment of inertia and mass distribution within the complex. Likewise, evaluating barriers to internal rotation of $\mathrm{CH}_{3}$ groups may indicate conformational trends. A good example is the study of thioacetic acid. ${ }^{74}$ A correlation between the barrier to internal rotation the syn-/anti- conformation of the O-H group was reported where the barrier to internal rotation for the latter is approximately 5 times higher than that for the former. Studies have also reported the variation of the barrier to internal rotation in isomers of i.e. methylindole ${ }^{75,76}$ and methylisooxazole. ${ }^{77,78}$ This variation may be expressed as a function of repulsive and attractive interactions between the $\mathrm{CH}_{3}$ group and the asymmetric molecular framework and the degree of aromaticity. Finally, obtaining experimental values for barriers to internal rotation is a way to benchmark and improve the performance of quantum chemical models.

Internal rotation is addressed in chapter 6 in methylimidazole isomers. A correlation between the barrier to internal rotation of the $\mathrm{CH}_{3}$ group and the position on which it substitutes on the imidazole ring was observed. These findings are consistent with studies on other methylated five-membered heteroaromatic rings like methylpyrrole, ${ }^{79,80}$ methythiazole ${ }^{81-83}$ and methyloxazole. ${ }^{69}$ It is observed that the heteroatoms in the ring will
dominate the magnitude of the relative barriers to internal rotation and some staggering variations are seen between equivalent isomers of the different methyl-azoles, e.g. 2methylthiazole ( $V_{3}=35 \mathrm{~cm}^{-1}$ ), 2-methylimidazole ( $V_{3}=123 \mathrm{~cm}^{-1}$ ), methyloxazole ( $V_{3}=$ $252 \mathrm{~cm}^{-1}$ ). In chapter 7, internal rotation in methylimidazole isomers is approached in the context of water attachment and hydrogen bond formation. To our best knowledge, this is the first comparative study of monohydrates of methylated heteroaromatic five-membered rings. The broad trend that was reported for the methylimidazole monomers is also observed for the monohydrates, however, attachment of water hinders internal rotation in 2-methylimidazole while the opposite effect is observed in N -methylimidazole.

### 1.5 Thesis Overview

This thesis will be concerned with microwave spectroscopy of non-volatile, organic molecules containing one or two nitrogen atoms. The first molecule to be discussed (chapter 4) is phosphine carboxamide, ${ }^{45}$ a phosphorus containing analogue of urea. Laser ablation was used to bring phosphine carboxamide into the gas phase and record its microwave spectrum in the $7.0-18.5 \mathrm{GHz}$ frequency range with the CP-FTMW spectrometer at Newcastle University. A van der Waals complex between phosphine carboxamide and argon, which serves as the carrier gas, was also formed and its spectrum was recorded (chapter 4). Imidazole ${ }^{11}$ is an alkaloid featured in many drugs and the building block of adenine, ${ }^{34}$ histamine,,$^{48}$ and histidine. ${ }^{31}$ Laser ablated imidazole formed hydrogen bonded complexes with water (chapter 5) and the internal dynamics and bonding patterns a of these complexes are discussed. Functionalizing imidazole with, for example, a methyl group results in molecules with modified physical and chemical properties. The microwave spectra of methylimidazole isomers (chapter 6) are discussed and an insight into the internal rotation dynamics of the methyl group is given. Both heating and laser ablation methods were used individually to introduce a specific methylimidazole isomer into the gas phase. The monohydrate complexes of methylimidazole (chapter 7) are reported and the barriers to internal rotation are evaluated as a function of hydrogen bond formation after attachment of water to the respective methylimidazole monomer.

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## Chapter 2. Theory

In this chapter, the fundamental concepts of rotational spectroscopy will be discussed. Both classical and quantum mechanical treatments will be considered, from polarization of rotational transitions with microwave radiation to determination of rotational constants followed by determination of molecular properties. The molecules and complexes considered in this thesis are asymmetric rotors (tops), so only brief insights into the theoretical aspects of other types of rotors will be given. This chapter is based on Gordy and Cook's Microwave Molecular Spectra, ${ }^{1}$ Hollas' Modern Spectroscopy ${ }^{2}$ and High-Resolution Spectroscopy $^{3}$ and Townes and Kroto's Molecular Rotation Spectra ${ }^{4}$ books. These are representative and authoritative sources regarding the underpinning theory of rotational spectroscopy.

Analysis of a rotational spectrum relies on quantum mechanical principles. Radiation in the $1-300 \mathrm{GHz}$ region is associated with rotational motions of molecules. When a molecule encounters this radiation, a photon will be absorbed if it is resonant with a rotational transition of that molecule. It is required that molecules possess a permanent dipole moment in order to absorb microwave radiation. The energy of a photon $\left(E_{p}\right)$ is quantized and is given by the expression;

$$
\begin{equation*}
E_{p}=h v=h \frac{c}{\lambda} \tag{Eq.2.1}
\end{equation*}
$$

where $h$ is the Planck constant, $v$ and $\lambda$ are the frequency and wavelength of the light, respectively, and $c$ is the speed of light in vacuum. The experiments in this thesis are concerned with both absorption and emission of microwave light. As it will be described in chapter 3, after the halt of the polarizing radiation that excites molecules from their ground state to higher rotational energy levels, molecular relaxation is detected as a decaying signal in the form of a free induction decay (FID). The advantages of detecting emission instead of absorption of photons have been discussed in the previous chapters.

### 2.1 Classical Mechanics and Moment of Inertia

Quantum mechanical treatment of molecular rotation emerges from fundamental concepts of classical mechanics. Structure determination methods that will be discussed in section 2.10 evaluate molecular structure from the moments of inertia of a molecule which are derived from measured rotational constants. For any molecule, the moment of inertia about anyaxis going through the center of mass may be expressed by the relationship;

$$
\begin{equation*}
I=\sum_{i} m_{i} r_{i}^{2} \tag{Eq.2.2}
\end{equation*}
$$

where $m_{i}$ is any mass point about a given principal axis and $\mathrm{r}_{\mathrm{i}}$ is the distance between $\mathrm{m}_{\mathrm{i}}$ and the center of mass of the molecule. Conventionally, we define three mutually perpendicular axes labeled as $a, b$ and $c$. It follows that for each of the $a$-, $b$ - and $c$-axes, a corresponding moment of inertia $I_{a a}, I_{b b}$ and $I_{c c}$ may be defined by means of equation 2.2. Conventionally, it holds that $I_{c c} \geq I_{b b} \geq I_{a a}$, meaning that the largest mass distribution is observed about the $c$-axis whereas the minimum mass distribution is found about the $a$ axis, with the $b$-axis being the intermediate case.

According to classical mechanics, the angular momentum of a rigid rotating molecule where each atom is considered a point mass is expressed as;

$$
\begin{equation*}
P=\omega \times I \tag{Eq.2.3}
\end{equation*}
$$

where $\omega$ is the angular velocity and $I$ is the moment of inertia tensor as defined in equation 2.2. As the rotor undergoes rotation about its center of mass, each point rotates at the same velocity. The moment of inertia may be expressed in terms of the $a$-, $b$ - and $c$-axes system as a matrix;

$$
I=\left(\begin{array}{ccc}
I_{a a} & I_{a b} & I_{a c}  \tag{Eq.2.4}\\
I_{b a} & I_{b b} & I_{b c} \\
I_{c a} & I_{c b} & I_{c c}
\end{array}\right)
$$

The mutually perpendicular $a$-, $b$ - and $c$-axes are conventionally placed on the center of mass of the rotating molecule, and so the off-diagonal components vanish, leaving the diagonal components known as the principal moments of inertia. It follows that;

$$
I=\left(\begin{array}{ccc}
I_{a a} & 0 & 0  \tag{Eq.2.5}\\
0 & I_{b b} & 0 \\
0 & 0 & I_{c c}
\end{array}\right)
$$

The individual moments of inertia are expressed as;

$$
\begin{align*}
& I_{a a}=\sum_{i} m_{i}\left(b_{i}^{2}+c_{i}^{2}\right)  \tag{Eq.2.6}\\
& I_{b b}=\sum_{i} m_{i}\left(a_{i}^{2}+c_{i}^{2}\right)  \tag{Eq.2.7}\\
& I_{c c}=\sum_{i} m_{i}\left(a_{i}^{2}+b_{i}^{2}\right) \tag{Eq.2.8}
\end{align*}
$$

The individual components of angular momentum are noted as;

$$
\begin{align*}
P_{a} & =\omega_{a a} \times I_{a a}  \tag{Eq.2.9}\\
P_{b} & =\omega_{b b} \times I_{b b}  \tag{Eq.2.10}\\
P_{c} & =\omega_{c c} \times I_{c c} \tag{Eq.2.11}
\end{align*}
$$

The rotational kinetic energy in the principal axes system is;

$$
\begin{equation*}
E_{r}=\frac{1}{2} \omega^{2} I=\frac{1}{2}\left(\frac{P_{a}^{2}}{I_{a a}}\right)+\frac{1}{2}\left(\frac{P_{b}^{2}}{I_{b b}}\right)+\frac{1}{2}\left(\frac{P_{c}^{2}}{I_{c c}}\right) \tag{Eq.2.12}
\end{equation*}
$$

When a torque is applied to a molecule, a molecular rotation is induced and the rate of change of the angular momentum is equal to the applied torque. The Euler equations of motion for a freely rotating body with no torque from the external field are;

$$
\begin{align*}
& \frac{d P_{a}}{d t}+\left(\frac{1}{I_{b b}}-\frac{1}{I_{c c}}\right) P_{b} P_{c}=0  \tag{Eq.2.13}\\
& \frac{d P_{b}}{d t}+\left(\frac{1}{I_{c c}}-\frac{1}{I_{a a}}\right) P_{c} P_{a}=0  \tag{Eq.2.14}\\
& \frac{d P_{c}}{d t}+\left(\frac{1}{I_{a a}}-\frac{1}{I_{b b}}\right) P_{a} P_{b}=0 \tag{Eq.2.15}
\end{align*}
$$

and it follows from these equations that the total kinetic energy remains constant. For linear and symmetric tops, rotation is constant about the symmetry axis. This condition is not true for asymmetric tops, although the total angular momentum is constant and
independent of the coordinate system it is expressed in. Discrimination of linear, symmetric, and asymmetric tops follows in section 2.2.

### 2.2 Types of Rotors

### 2.2.1 Linear Tops

Considering a linear molecule, e.g. AgI, OCS, HCN , it holds that $I_{c c}=I_{b b}>I_{a a} \cong 0$, with the principal axes being mutually perpendicular at the center of mass of AgI, figure 2.1. If the Ag and I atoms are considered as point masses on the $a$-axis, $I_{a a}$ is very small,


Figure 2.1. The linear diatomic silver iodide (AgI). The $a$-inertial axis is aligned with the Ag -I bond resulting in a $I_{a a}$ value of effectively zero.
approaching zero.

### 2.2.2 Symmetric Tops

Symmetric tops may be classified as a prolate or an oblate symmetric top where two of the moments of inertia are equal whilst the third one is non-zero. For a prolate symmetric top, it holds that;

$$
\begin{equation*}
I_{c c}=I_{b b}>I_{a a} \tag{Eq.2.16}
\end{equation*}
$$

An example of a prolate symmetric top is acetonitrile (methyl cyanide) $\mathrm{H}_{3} \mathrm{CCN}$. The $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N}$ bonds of the molecule are aligned with the $a$-inertial axis while the contributions to the $I_{a a}$ made by the $\mathrm{C}-\mathrm{H}$ bonds are negligible.

Benzene is the prototype example of an oblate symmetric top. It follows that for an oblate symmetric top;

$$
\begin{equation*}
I_{a a}=I_{b b}<I_{c c} \tag{Eq.2.17}
\end{equation*}
$$

A prerequisite for a molecule to be classed as a symmetric top is that it has a $C_{n}$ axis where $n>2$. $\mathrm{A} C_{3}$ axis is present within acetonitrile which is aligned with the $a$-inertial axis of the molecule. As for benzene, a $C_{6}$ axis is observed through the aromatic plane, aligned with the $c$-inertial axis.

### 2.2.3 Asymmetric Tops

In the case of asymmetric tops, all principal inertial components are unequal;

$$
\begin{equation*}
I_{c c} \neq I_{b b} \neq I_{c c} \tag{Eq.2.18}
\end{equation*}
$$

The majority of asymmetric tops are known as prolate near-symmetric rotors with;

$$
\begin{equation*}
I_{c c} \approx I_{b b}>I_{a a} \tag{Eq.2.19}
\end{equation*}
$$

An example of prolate near-symmetric rotor is $N$-methylimidazole (chapter 6).

We may also come across molecules such as imidazole (chapter 5) that are classed as oblate near-symmetric tops for which we observe;

$$
\begin{equation*}
I_{c}>I_{b} \approx I_{a} \tag{Eq.2.20}
\end{equation*}
$$

Any set of $x, y, z$ cartesian axes can be placed on a molecule which may or may not coincide with the principal $a$-, $b$-, and $c$-inertial axes. The most common convention is the $I^{r}$ representation where $(x, y, z) \equiv(a, b, c)$. Other possible representations are;

|  | $\mathrm{I}^{\mathrm{r}}$ | $\mathrm{II}^{\mathrm{r}}$ | $\mathrm{III}^{\mathrm{r}}$ | $\mathrm{I}^{\mathrm{1}}$ | $\mathrm{II}^{\mathrm{1}}$ | $\mathrm{III}^{\mathrm{1}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | $b$ | $c$ | $a$ | $c$ | $a$ | $b$ |
| $y$ | $c$ | $a$ | $b$ | $b$ | $c$ | $a$ |
| $z$ | $a$ | $b$ | $c$ | $a$ | $b$ | $c$ |

The representations refer to the axes orientation in the rotational Hamiltonian which will be discussed in the following sections.

### 2.3 Born-Oppenheimer Approximation

The total energy of a diatomic or polyatomic molecule is the sum of its kinetic $T$ and potential energy $V$. The kinetic energy includes contributions made by electronic and nuclear motions. Coulombic repulsions between electrons and between nuclei as well as attractive forces between electrons and nuclei, comprise the potential energy. According to the Born-Oppenheimer approximation, electronic and nuclear motions are treated independent of one another because they occur on different timescales. Nuclei are much heavier than electrons so electronic motions are separated from nuclear motions and nuclei are effectively treated as static. Internal motions of a system and their corresponding energies can also be treated separately. The Hamiltonian for a molecular system describes these internal motions and is written as:

$$
\begin{equation*}
\hat{\mathrm{H}}_{\text {total }}=\hat{\mathrm{H}}_{e l}+\hat{\mathrm{H}}_{v i b}+\hat{\mathrm{H}}_{\text {rot }}+\hat{\mathrm{H}}_{\text {trans }} \tag{Eq.2.21}
\end{equation*}
$$

where el: electronic, vib: vibrational, rot: rotational and trans: translational the relevant Hamiltonians in the overall Hamiltonian. Likewise, the total wavefunction and eingenvalues that describe a molecular system are expressed as:

$$
\begin{equation*}
\psi_{t o t a l}=\psi_{e l} \cdot \psi_{v i b} \cdot \psi_{r o t} \cdot \psi_{t r a n s} \tag{Eq.2.22}
\end{equation*}
$$

and

$$
\begin{equation*}
E_{\text {total }}=E_{e l}+E_{v i b}+E_{\text {rot }}+E_{\text {trans }} \tag{Eq.2.23}
\end{equation*}
$$

respectively.
This work will only be concerned with rotational motions for the electronic and vibrational ground state of molecules for which the time-independent Schrödinger equation will be solved. The time-independent equation can only be solved for one-electron atomic systems. The generalized solution for the time-independent equation for a molecular rotor is;

$$
\begin{equation*}
\hat{\mathrm{H}}_{r o t} \psi_{r o t}=E_{r o t} \psi_{r o t} \tag{Eq.2.24}
\end{equation*}
$$

where $\psi_{\text {rot }}$ is the rotational eigenfunction and $E_{r o t}$ is the eigenvalues of the Hamiltonian.
A Hamiltonian can be formulated to account for internal and large amplitude motions (LAM). The internal rotation Hamiltonian will be discussed in more detail in section 2.9.

### 2.4 The Rigid Rotor Approximation

In quantum mechanics, a torque is applied by a resonant photon $h v$. The classical Hamiltonian represents the total energy of a system and consists of kinetic and potential energy;

$$
\begin{equation*}
H=T+V \tag{Eq.2.25}
\end{equation*}
$$

where $T=\frac{J^{2}}{2 m}$ and $J$ is the total momentum and $m$ is the mass of the system. It was discussed in section 2.2 that the potential energy is not included in the wavefunction of a rotating molecule. In a molecule with $a$-, $b$-, and $c$-inertial axes, the angular momenta in the rotational Hamiltonian are replaced by their relevant angular momentum operators which are formulated to include $\hbar, \hat{P}=-i \hbar \nabla$. The eigenvalues that solve the Hamiltonian operators are the quantized rotational energy levels measured in the microwave spectrum and are specific for a given molecule. The Hamiltonian operator is;

$$
\begin{equation*}
\hat{\mathrm{H}}_{r o t}=\frac{1}{2}\left(\frac{\hat{P}_{a}^{2}}{I_{a a}}+\frac{\hat{P}_{b}^{2}}{I_{b b}}+\frac{\hat{P}_{c}^{2}}{I_{c c}}\right) \tag{Eq.2.26}
\end{equation*}
$$

The case of a simple diatomic performing an end-over-end rotation may be described by the rigid rotor approximation. According to that concept, the two mass point atoms are joined by a weightless, rigid, non-distortable bond. If that bond were to coincide with an inertial axis of that diatomic, i.e. the $a$-axis, then the rotation depends on the mass distribution about that axis. The model can extend to polyatomic molecules performing rotations about the $a$-, $b$-, and $c$-inertial axis which are placed on its center of mass. The quantum mechanical rigid rotor Hamiltonian is also expressed as;

$$
\begin{equation*}
\hat{\mathrm{H}}_{r o t}=A \hat{P}_{a}^{2}+B \hat{P}_{b}^{2}+C \hat{P}_{c}^{2} \tag{Eq.2.27}
\end{equation*}
$$

where $A, B$, and $C$ are the rotational constants specific to each inertial axis and $\hat{P}_{a}, \hat{P}_{b}$, and $\hat{P}_{c}$ are the angular momenta operators. For convenience, the rotational constants are expressed in units of $h$;

$$
A=\frac{h}{8 \pi^{2} I_{a a}}, B=\frac{h}{8 \pi^{2} I_{b b}}, \text { and } C=\frac{h}{8 \pi^{2} I_{c c}}(E q \cdot 2.28)
$$

where $h$ is the Planck constant and $I_{a a}, I_{b b}$, and $I_{c c}$ are the principal moment moments of inertia as described in section 2.1. The rotational constant is inversely proportional to the corresponding moment of inertia.

### 2.5 Ray's Asymmetry Parameter

Ray's asymmetry parameter, $\kappa$, provides a measurement of the asymmetry of a molecule by giving a quantitative insight into how far from the prolate or oblate limit it lies. It is defined as;

$$
\begin{equation*}
\kappa=\frac{2 B-A-C}{A-C} \tag{Eq.2.29}
\end{equation*}
$$

and may take values $-1 \leq \kappa \leq 1$. At the prolate limit, it holds that $\kappa=-1$ and $A>B=$ $C$, whilst for an oblate we have $\kappa=1$ and $A=B>C$ (figure 2.2). At the intermediate case where $\kappa=0$, the molecule exhibits the highest degree of asymmetry.


Figure 2.2. Schematic representations of a prolate (rugby ball) and an oblate (frisbee) symmetric top.

### 2.6 Rotational Transitions and Energy Levels

Generally, the energy of a transition between subsequent energy levels is described as;

$$
\begin{equation*}
E_{1}-E_{2}=h v \tag{Eq.2.30}
\end{equation*}
$$

which is equal to the energy of the resonant photon that excites that transition.
Within the rigid rotor approximation, the eigenvalues of the rotational energy levels that are solutions to the time-independent Schrödinger equation are given by the relationship;

$$
\begin{equation*}
E_{r}=\frac{h^{2}}{8 \pi^{2} I} J(J+1) \tag{Eq.2.31}
\end{equation*}
$$

where $h$ is the Planck constant, the moment of inertia $I=\mu r^{2}$ with $\mu=\frac{m_{1} m_{2}}{m_{1}+m_{2}}$ being the reduced mass of the diatomic and $J=0,1,2, \ldots$ is the rotational quantum number and describes the total angular momentum in units of $h / 2 \pi$. In microwave spectroscopy, frequency units $(\mathrm{Hz}, \mathrm{MHz}, \mathrm{GHz}$ converted from energy by dividing by $h$ ) are used to describe the different energy levels $E(J)$;

$$
\begin{equation*}
E(J)=\frac{E_{r}}{h}=\frac{h}{8 \pi^{2} I} J(J+1)=B J(J+1) \tag{Eq.2.32}
\end{equation*}
$$

Allowed rotational transitions for both emission and absorption spectra comply with the selection rule;

$$
\begin{equation*}
\Delta J= \pm 1 \tag{Eq.2.33}
\end{equation*}
$$

meaning photons can be emitted or absorbed between subsequent rotational energy levels. It is also crucial that the molecules of interest possess a permanent dipole moment $(\mu \neq 0)$ in order to absorb a photon. For asymmetric rotors, rotational emission transitions will be described by the notation;

$$
\begin{equation*}
J^{\prime} \rightarrow J^{\prime \prime} \tag{Eq.2.34}
\end{equation*}
$$

which indicates a change in the angular momentum of the rotating molecule. Single prime " $'$ " indicates the upper state and double prime " " " the lower state.

For symmetric and asymmetric tops, the energy levels become more complex compared to those of a linear molecule. It is necessary to introduce the quantum number $K$ which describes the projection of the total angular momentum along an axis of symmetry. For a prolate top, i.e. methyl cyanide, the vector of the angular momentum $P$ may orientate in
any direction. The expression for the energy levels of a symmetric top including a term that accounts for $K$ is;

$$
\begin{equation*}
E(J, K)=B J(J+1)+(A-B) K^{2} \tag{Eq.2.35}
\end{equation*}
$$

For an oblate symmetric top, the energy expression becomes;

$$
\begin{equation*}
E(J, K)=B J(J+1)+(C-B) K^{2} \tag{Eq.2.36}
\end{equation*}
$$

Due to the $K^{2}$ term in equations 2.35 and 2.36, the values $K$ may take are $K=$ $0, \pm 1, \pm 2, \ldots, \pm J$ and the $K$ levels are doubly degenerate. For asymmetric molecules, the degeneracy is lifted and the above expressions are modified as;

$$
\begin{equation*}
E(J, K) \cong B_{b a r} J(J+1)+\left(A-B_{b a r}\right) K^{2} \tag{Eq.2.37}
\end{equation*}
$$

and

$$
\begin{equation*}
E(J, K) \cong B_{b a r} J(J+1)+\left(C-B_{b a r}\right) K^{2} \tag{Eq.2.38}
\end{equation*}
$$

for a near-prolate and a near-oblate top, respectively. $B_{b a r}$ is defined as $\frac{1}{2}(B+C)$ and $\frac{1}{2}(A+B)$, respectively. This thesis will be concerned with near-prolate tops. The rotational emission transitions will be hereby labelled as;

$$
\begin{equation*}
J_{K_{-1}^{\prime} K_{1}^{\prime}}^{\prime} \rightarrow J_{K_{-1} K_{1}^{\prime \prime}}^{\prime \prime} \tag{Eq.2.39}
\end{equation*}
$$

$K_{-1}$ and $K_{1}$ are labels linking the energy levels to the prolate and oblate limits, essentially describing the intermediate case of an asymmetric top. The $K$ levels are no longer degenerate, and their energy difference tends to decrease with increasing value of $K_{-1}$. Selection rules of allowed rotational transitions of an asymmetric top are listed in table 2.1. Figure 2.3 is a schematic representation of the $a$-type rotational energy levels of an asymmetric top at the prolate and oblate limit as a function of the molecule's asymmetry $\kappa$.

The asymmetric Hamiltonian may be rearranged and expressed as a function of $\kappa$;

$$
\begin{equation*}
\hat{\mathrm{H}}_{r o t}=\frac{1}{2}(A+C) \hat{P}^{2}-\frac{1}{2}(A-C) \widehat{H}_{\kappa} \tag{Eq.2.40}
\end{equation*}
$$

where $\widehat{H}_{\kappa}=\hat{P}_{a}^{2}+\kappa \hat{P}_{b}^{2}-\hat{P}_{c}^{2}$.
The rotational Hamiltonian for an asymmetric top is typically expressed as a matrix, followed by diagonalization. When the matrix element of the rotational Hamiltonian are known, the rotational energy levels can be found which are the eigenvalues. Depending on
the orientation of the electric dipole moment, whether that is along the $a$-, $b$ - or $c$-inertial axes, the respective type of transition will be yielded, namely $a$-, $b$ - or $c$-type transitions. Selection rules and transitions are shown in table 2.1.

Table 2.1. Selection rules for transitions of asymmetric-top molecules.

| Dipole Component | Type | $\Delta J^{a}$ | $\Delta K_{-1}$ | $\Delta K_{1}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mu_{a} \neq 0$ | $a$-type | $0, \pm 1$ | $0, \pm 2, \ldots$ | $\pm 1, \pm 3, \ldots$ |
| $\mu_{b} \neq 0$ | $b$-type | $0, \pm 1$ | $\pm 1, \pm 3, \ldots$ | $\pm 1, \pm 3, \ldots$ |
| $\mu_{c} \neq 0$ | $c$-type | $0, \pm 1$ | $\pm 1, \pm 3, \ldots$ | $0, \pm 2, \ldots$ |

${ }^{\text {a }} \Delta J=1$ and 0 correspond to R - and Q -branch transitions, respectively. Transitions with $\Delta K_{-1}$ and $\Delta K_{1} \geq 2$ are usually not observable in MW spectroscopy. A detailed list of selection rules may be found in the work of Cooke and Ohring. ${ }^{5}$


Figure 2.3. Correlation diagram of the energy levels of an asymmetric top at the prolate and oblate end. The energy levels are expressed as a function of the asymmetry parameter $\kappa$.

### 2.7 The Distortable Rotor and the Reduced Hamiltonian

Within the rigid rotor approximation, atoms are considered as point masses held together by rigid, weightless bonds. Real molecules undergoing rotation will experience distortion in their bonds and angles because of centrifugal forces. These restoring forces also give rise to the structural differences between equilibrium and zero-point structures. The effects of centrifugal distortion become more complicated as the molecular networks becomes more complex. In microwave spectroscopy, the effects of centrifugal distortion are depicted on the position of rotational transitions which may become perturbed. However, as it will be seen in the Hamiltonian for a distortable rotor, for lower $J$ transitions, the effects of centrifugal distortion only comprise a small portion of the rotational energy so the deviations from rigid rotor behavior may be subtle.

The energy levels of a semi-rigid diatomic rotor can be expressed by modification of equation 2.31 and addition of centrifugal distortion terms that correct the energy. This is written as;

$$
\begin{equation*}
E(J)=B J(J+1)-D J^{2}(J+1)^{2}+H J^{3}(J+1)^{3}+\cdots \tag{Eq.2.41}
\end{equation*}
$$

where $D$ and $H$ are the quartic and sextic order centrifugal distortion constants, respectively.

The quantum number $K$ which is necessary to describe the energy levels of symmetric and asymmetric tops was introduced in section 2.6. The rotational transitions arising from the projection of the angular momentum on the symmetry axis are doubly degenerate for symmetric tops. The degeneracy is lifted in the case of asymmetric tops and transitions with $K=1,2,3 \ldots$ are split into two components and their energy differences typically decreases with increasing $K$.

For asymmetric tops, there are two reduced, quantum mechanical Hamiltonians, namely Watson's A- and S-reduced Hamiltonians, where A- stands for asymmetric top and S- for symmetric top. These Hamiltonians consider centrifugal distortion forces and their effect on the total rotational energy. The advantage of the reduced Hamiltonian is that it allows for least square fitting of rotational transitions and any parameters that are only poorly determined may be removed from the expansion. The A-reduction which contains the rotational Hamiltonian and terms that account for the centrifugal distortion is written as;

$$
\begin{align*}
H^{A}=1 / 2\left(B^{A}\right. & \left.+C^{A}\right) J^{2}+\left(A^{A}-1 / 2\left(B^{A}+C^{A}\right)\right) J_{z}^{2}+1 / 2\left(B^{A}+C^{A}\right)\left(J_{x}^{2}-J_{y}^{2}\right)+\Delta_{J} J^{4} \\
& -\Delta_{J} K J^{2} J_{z}^{2}-\Delta_{K} J_{z}^{4}-2 \delta_{J} J^{2}\left(J_{x}^{2}-J_{y}^{2}\right)-\delta_{K}\left(J_{z}^{2}\left(J_{x}^{2}-J_{y}^{2}\right)+\left(J_{x}^{2}-J_{y}^{2}\right) J_{z}^{2}\right)+\Phi_{J} J^{6} \\
& +\Phi_{J K} J^{4} J_{z}^{2}+\Phi_{K J} J^{2} J_{z}^{4}+\Phi_{K} J_{z}^{6}+\cdots \tag{Eq.2.42}
\end{align*}
$$

where $J_{x}, J_{y}$, and $J_{z}$ are the angular momentum vectors along the principal inertial axes and $J^{2}=J_{x}+J_{y}+J_{z}$.

The S-reduction is written as;

$$
\begin{align*}
H^{S}=1 / 2\left(B^{S}\right. & \left.+C^{S}\right) J^{2}+\left(A^{S}-1 / 2\left(B^{S}+C^{S}\right)\right) J_{z}^{2}+1 / 4\left(B^{S}-C^{S}\right)\left(J_{+}^{2}-J_{-}^{2}\right)-D_{J} J^{4} \\
& -D_{J} K J^{2} J_{z}^{2}-D_{K} J_{z}^{4}-2 \delta_{1} J^{2}\left(J_{+}^{2}-J_{-}^{2}\right)-\delta_{2}\left(J_{+}^{4}-J_{-}^{4}\right)+H_{J} J^{6}+H_{J K} J^{4} J_{z}^{2} \\
& +H_{K J} J^{2} J_{z}^{4}+H_{K} J_{z}^{6}+\cdots \tag{Eq.2.43}
\end{align*}
$$

where $J_{+}^{2}+J_{-}^{2}=2\left(J_{x}^{2}-J_{y}^{2}\right)$.
Both A- and S-Hamiltonians are used throughout this thesis and it will be indicated which one was used for each molecule. Typically, the S-reduction is more suitable for asymmetric top that approach the oblate or prolate limit, i.e. $\kappa \rightarrow 1$ or -1 . The A-reduction is more appropriate when the asymmetry of a molecule is high, i.e. $\kappa \rightarrow 0$.

Terms beyond the sextic are often omitted in microwave spectroscopy as these terms have a more significant effect in millimeter-wave and THz spectroscopy. The effect of the sectic and octic terms is more profound with higher $J$.

### 2.8 Hyperfine Structure- Nuclear Quadrupole Coupling

The rotational spectra of the molecules that will discussed in this thesis exhibit hyperfine structure due to the presence of one or more nuclei with non-spherical distribution of nuclear charges. This type of distribution generates the nuclear electric quadrupole moment, $e Q$, and an electric field gradient (EFG) on that nucleus. The hyperfine structure that will be observed here arises through coupling of the nuclear electric quadrupole moment of a nucleus with spin $I \geq \frac{1}{2}$ with the EFG of the oscillating electric field. In the semi-rigid Hamiltonians used in this thesis, this interaction is expressed as;

$$
\begin{equation*}
H_{Q}=\frac{1}{6} Q(X): \nabla E(X) \tag{Eq.2.44}
\end{equation*}
$$

where $Q$ and $\nabla E$ are the electric quadrupole moment and electric field tensors of a nucleus X with $I \geq \frac{1}{2}$, respectively. This interaction is not observed for nuclei with spherical distribution of nuclear charges with $I=0$ or $1 / 2$. When more than one quadrupolar nuclei are present, additional terms are included in the Hamiltonian.


Figure 2.4. Schematic representation of coupling between angular momentum $J$ and nuclear spin $I$ resulting in the total angular momentum $F$.

Considering a rotating molecule with one quadrupolar nucleus in an electric field where the nuclear spin $I$ couples to the angular momentum of the molecular rotation $J$ which results in the total angular momentum $F$. A graphic representation of the coupling interaction is given in figure 2.4.

$$
\begin{equation*}
F=J+I \tag{Eq.2.45}
\end{equation*}
$$

The resulting quantum numbers $I, J$ and $F$ are related in the following manner;

$$
\begin{equation*}
F=J+I, J+I-1, J+I-2, \ldots \ldots,|J-I| \tag{Eq.2.46}
\end{equation*}
$$

which is an expression for the total angular momentum.
We also have $M_{F}$ which may adopt values $M_{F}=F, F-1, F-2, \ldots,-F$.
Selection rules for allowed hyperfine transitions in rotational emission spectra are $\Delta J=1$, $\Delta F=0, \pm 1$, and $\Delta I=0$.

In rotational spectroscopy, for a coupling nucleus X in an asymmetric top the coupling (eQq) components are labelled as;

$$
\begin{align*}
\chi_{a a} & =e Q q_{a a}  \tag{Eq.2.47}\\
\chi_{b b} & =e Q q_{b b}  \tag{Eq.2.48}\\
\chi_{c c} & =e Q q_{c c} \tag{Eq.2.49}
\end{align*}
$$

These are the diagonal components of the recurrent three-by-three matrix;

$$
\chi=\left(\begin{array}{lll}
\chi_{a a} & \chi_{b a} & \chi_{c a}  \tag{Eq.2.50}\\
\chi_{a b} & \chi_{b b} & \chi_{c b} \\
\chi_{a c} & \chi_{b c} & \chi_{c c}
\end{array}\right)
$$

for which the Laplace condition holds;

$$
\begin{equation*}
\chi_{a a}+\chi_{b b}+\chi_{c c}=0 \tag{Eq.2.51}
\end{equation*}
$$

The off-diagonal components $\chi_{a b}, \chi_{a c}, \chi_{c b}, \ldots$ are often small and only very poorly determined with rotational spectroscopy, particularly for nuclei with small quadrupole moments. Where off-diagonal terms are necessary to be used for generating diagonalized components (see section 2.8.2) in this thesis, these will be calculated ab initio or with DFT. Information about the electronic environment in different molecules may be obtained by the measured values of $\chi_{a a}, \chi_{b b}$ and $\chi_{c c}$, which are sensitive to subtle changes in electronic distributions, i.e. between structural isomers. The measured values of $\chi_{a a}, \chi_{b b}$ and $\chi_{c c}$ are typically more sensitive to low $J$ transitions as the hyperfine lines tend to be blended at higher $J$.

### 2.8.1 Molecules with two or more Quadrupolar Nuclei

The hyperfine structure of molecular transitions becomes more complicated in the case where two quadrupolar nuclei are present within a molecule or a complex. The majority of molecules and complexes that will be discussed in this thesis possess two quadrupolar
nuclei, in particular, two N nuclei with $I=1$. It was explained above that additional terms are included in the Hamiltonian to account for the coupling interactions. The total angular momentum, $J$, is now coupled by $I_{1}$ and $I_{2}$ which are the nuclear spins of two quadrupolar nuclei which result in $F_{1}$ and $F$.


Figure 2.5. Schematic representation of coupling between the angular momentum $J$ and the nuclear spin on two quadrupolar nuclei, $I_{1}$ and $I_{2}$, resulting in the total angular momentum $F$.

### 2.8.2 Principal Nuclear Axes

Often, the measured values of $\chi_{a a}, \chi_{b b}$ and $\chi_{c c}$ do not provide sufficient information for a direct comparison of the electronic environment of nuclei in different molecules. This is because these components are referenced against the $a$-, $b$-, and $c$-inertial axes which are unique for each molecule. A common reference system is necessary where a set of mutually perpendicular axes $x, y$, and $z$, which are also the axes of the field gradient, are placed on each quadrupolar nucleus. The resulting diagonalized coupling components are now $\chi_{x x}$, $\chi_{y y}$ and $\chi_{z z}$ with all the rest of the components being equal to zero;

$$
\chi=\left(\begin{array}{ccc}
\chi_{z z} & 0 & 0  \tag{Eq.2.52}\\
0 & \chi_{y y} & 0 \\
0 & 0 & \chi_{z z}
\end{array}\right)
$$

The transformation should rely on the following relationships;

$$
\begin{gather*}
\chi_{a a}=\chi_{x x} \cos ^{2} \theta_{x a}+\chi_{y y} \cos ^{2} \theta_{y a}+\chi_{z z} \cos ^{2} \theta_{z a}  \tag{Eq.2.53}\\
\chi_{b b}=\chi_{x x} \cos ^{2} \theta_{x b}+\chi_{y y} \cos ^{2} \theta_{y b}+\chi_{z z} \cos ^{2} \theta_{z b}  \tag{Eq.2.54}\\
\chi_{c c}=\chi_{x x} \cos ^{2} \theta_{x c}+\chi_{y y} \cos ^{2} \theta_{y c}+\chi_{z z} \cos ^{2} \theta_{z c}  \tag{Eq.2.55}\\
35
\end{gather*}
$$

however, these equations cannot be solved directly. It is necessary to have a value for at least one off-diagonal component $\chi_{a b}, \chi_{a c}, \chi_{c b}, \ldots$ but as described above, these typically cannot be determined from the rotational hyperfine structure. A calculated value of $\chi_{a b}$ may be used instead.

In the case where a coupling tensor coincides with a bond axis or an inertial axis, for example, for the $z$-axis it holds that $\chi_{x x}=\chi_{y y}=-\frac{1}{2} \chi_{z z}$, then there is only one dependent constant. The above equations 2.53-2.55 are expressed as;

$$
\begin{align*}
\chi_{a a} & =-\frac{1}{2} \chi_{z z}\left(3 \cos ^{2} \theta_{z a}-1\right)  \tag{Eq.2.56}\\
\chi_{b b} & =-\frac{1}{2} \chi_{z z}\left(3 \cos ^{2} \theta_{z b}-1\right)  \tag{Eq.2.57}\\
\chi_{c c} & =-\frac{1}{2} \chi_{z z}\left(3 \cos ^{2} \theta_{z c}-1\right) \tag{Eq.2.58}
\end{align*}
$$

The molecules and complexes discussed in this thesis possess a plane of symmetry. The axis that goes through that plane is the c-axis (or the $a$-axis when it comes to Ar van der Waals complexes). That axis will be colinear with a principal axis of the field gradient or coupling. Then it holds that;

$$
\begin{align*}
& \chi_{a a}=\chi_{x x} \sin ^{2} \theta_{z a}+\chi_{z z} \cos ^{2} \theta_{z a}  \tag{Eq.2.59}\\
& \chi_{b b}=\chi_{x x} \cos ^{2} \theta_{z a}+\chi_{z z} \sin ^{2} \theta_{z a} \tag{Eq.2.60}
\end{align*}
$$

This method is implemented in Kisiel's program QDIAG which will be used throughout this thesis. The program is available from the PROSPE website. The measured values of $\chi_{a a}, \chi_{b b}$ and $\chi_{c c}$ and a calculated value of $\chi_{a b}$ are evaluated to generate $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$.

### 2.9 Internal Rotation

It is common for molecules that contain groups with 3-fold symmetry, i.e. $\mathrm{CH}_{3}$ groups, to exhibit internal rotation of that group coupling to the overall rotation, provided that the surrounding energy is sufficient to surmount the barrier height to internal rotation. The potential energy surface of a $\mathrm{CH}_{3}$ rotating internally can be expressed as a periodic function of $\alpha$, which repeats over $120^{\circ}$ intervals, $2 \pi / N$ where $N$ is the $N$-fold symmetry of the rotating group which is equal to 3 in the case of $\mathrm{CH}_{3}$. It can be expressed as;

$$
\begin{equation*}
V(\alpha)=\frac{V_{3}}{2}(1-\cos 3 \alpha)+\frac{V_{6}}{2}(1-\cos 6 \alpha)+\cdots \tag{Eq.2.61}
\end{equation*}
$$

This thesis will be concerned with molecules with 3-fold barriers so the higher terms vanish retaining expression 2.61 to;

$$
\begin{equation*}
V(\alpha)=\frac{V_{3}}{2}(1-\cos 3 \alpha) \tag{Eq.2.62}
\end{equation*}
$$

The barrier to a three-fold internal rotation will hereafter be denoted as $V_{3}$. The $V_{3}$ barrier to internal rotation was calculated for $N$-methylimidazole at the B3LYP(D3BJ)/aug-ccPVTZ level and the shape of the sinusoidal hindering potential is shown in figure 2.6.


Figure 2.6. Calculated representation of the $V_{3}$ hindering potential in $N$-methylimidazole. Identical minima are repeated over $120^{\circ}$ rotations of the (H-C6-N1-C2) dihedral angle.

The torsional energy levels for a system with internal rotation of a three-fold group are given by;

$$
\begin{equation*}
-F \frac{d^{2} U(\alpha)}{d \alpha}+\left[\frac{V_{3}}{2}(1-\cos 3 \alpha)-E\right] U(\alpha)=0 \tag{Eq.2.63}
\end{equation*}
$$

where $F=\frac{\hbar^{2}}{2 I_{r}}$ is the rotational constant and $I_{r}=\frac{I_{i} I_{r}}{I_{i}+I_{r}}$ the reduced mass of internal rotormolecular framework, $E$ is the total energy of the system and $U(\alpha)$ the periodic wavefunction of internal rotation. In order to find the relative torsional levels, we may consider two limiting cases; i) very low barrier resulting in essentially free internal rotation $\left(V_{3} \rightarrow 0\right)$ and ii) very high barrier with a rigid internal rotor $\left(V_{3} \rightarrow \infty\right)$.

For $V_{3} \rightarrow 0$, expression 2.63 is simplified to ;

$$
\begin{equation*}
\frac{d^{2} U(\alpha)}{d \alpha}+\frac{1}{F} E U(\alpha)=0 \tag{Eq.2.64}
\end{equation*}
$$

and

$$
\begin{equation*}
U(\alpha)-A e^{i m \alpha}=A(\cos (m \alpha)+i \sin (m \alpha)) \tag{Eq.2.65}
\end{equation*}
$$

where $A$ is a normalization factor and $m=0, \pm 1, \pm 2, \pm 3, \ldots$ is the internal rotation quantum number. The energy is given by;

$$
\begin{equation*}
E=F m^{2} \tag{Eq.2.66}
\end{equation*}
$$

and it follows that torsional states are doubly degenerate except for $m=0$.
For $V_{3} \rightarrow \infty$, internal motions will be restricted to low energy oscillations about the minima of the potential well. The torsional levels approximate those of a harmonic oscillator with frequencies;

$$
\begin{equation*}
v=\frac{3}{2 \pi}\left(\frac{V_{3}}{2 I_{r}}\right)^{1 / 2} \tag{Eq.2.67}
\end{equation*}
$$

The limiting case of a rigid internal rotor is beyond the scope of this thesis.
At the free rotor limit, each torsional state $v$ is three-fold degenerate. At the intermediate case of finite barrier, quantum mechanical tunnelling effects lift the degeneracy, and a splitting is induced. Since the barrier is finite, the probability of tunnelling through the barrier is also finite. Tunnelling through the potential barrier results in splitting of the threefold degenerate torsional levels into an $A$-state $(m=0)$ and a doubly degenerate $E$-state ( $m= \pm 1$ ).

The Hamiltonian for an asymmetric molecule with a three-fold internal rotor is written as;

$$
\begin{equation*}
\mathcal{H}=H^{A}+H_{I R} \tag{Eq.2.68}
\end{equation*}
$$

where $H^{A}$ is Watson's A-reduced Hamiltonian and $H_{I R}$ is the internal rotation Hamiltonian defined as;

$$
\begin{equation*}
H_{I R}=F\left(\hat{P}_{a}-\hat{P}\right)^{2}+V(\alpha) \tag{Eq.2.69}
\end{equation*}
$$

Two methods were used to approach internal rotation in this thesis; the principal axes method (PAM) and the internal axes method (IAM), the main difference being the reference system used in each one. In the PAM, the principal axes of the molecule of interest are used as the reference system. The advantage is that the components of the moments of inertia remain diagonalized. It is required that the local $C_{3}$ axis of the $\mathrm{CH}_{3}$ group is co-linear or almost co-linear with one of the principal axes of the molecule. In the IAM, the $\mathrm{C}_{3}$ axis of the $\mathrm{CH}_{3}$ group is chosen as one of the reference axes and the polar coordinates are chosen such that internal rotation-rotation coupling is minimized.

### 2.9.1 Principal Axes Method (PAM)

The PAM ${ }^{1}$ was used as complementary approach to the barriers to internal rotation in methylimidazole isomers and is described in detail in chapter 6 . The method is generally more appropriate for molecules with low $V_{3}$ barriers and molecules where vibrational contributions are negligible at the zero-point. It is also important that the local $C_{3}$ axis of the internal rotor is aligned or almost aligned with one of the principal inertial axes of the molecule. The method evaluates how the measured rotational constants determined through fitting of $A$-state transitions deviate from the limiting case of free internal rotation with $V_{3} \rightarrow 0$ or fixed internal rotor $V_{3} \rightarrow \infty$ and estimates the actual $V_{3}$ barrier to internal rotation.

### 2.9.2 Internal Axes Method (IAM)

The IAM ${ }^{1}$ is implemented in the program XIAM ${ }^{6}$, available from the PROSPE website ${ }^{7}$. This method will be the predominant tool to analyze internal rotation in this thesis. The Hamiltonian implemented in XIAM is based on the one described in section 2.9 and the complete form is discussed here ${ }^{6}$. Unlike in the PAM, the local $\mathrm{C}_{3}$ axis of the $\mathrm{CH}_{3}$ group as a reference and the angles between that and the principal inertial axes of the molecule are of interest. The polar coordinates are defined as $\delta$ and $\varepsilon$, which are the angles between the $\mathrm{C}_{3}$ axis and the $a$-inertial axis and between the $b$-axis and the projection of $\mathrm{C}_{3}$ onto the $b c$ plane, respectively.

### 2.10 Structure determination methods

Experimentally measured rotational constants give an insight into the molecular structure of a molecule or complex. In section 2.5 , it was shown that Ray's asymmetry parameter gives a quantitative measure of the asymmetry of an asymmetric top molecule by evaluating the $A, B$, and $C$ rotational constants. In sections 2.1 and 2.4 it was discussed that the measured rotational constants are inversely proportional to the moment of inertia around the corresponding inertial axis. It will be shown in section 2.10.1 that the moments of inertia may be evaluated to calculate planar moments that give a more straight-forward insight into the mass distribution. It is possible to determine the precise position of an atom within a molecule by measuring the rotational constants of the molecule with an atom replaced by a heavier or lighter isotope, i.e. ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$. The Kraitchman method (2.10.2) evaluates changes in the moments of inertia caused by single isotopic substitution and requires no assumptions about the molecular structure. The effective structure (2.10.3) can deal with multiple atoms substituted by their heavier isotopes at once; however, it is necessary to make assumptions about the molecular structure when there is not sufficient isotopic information about each atom in a molecule.

### 2.10.1 Planar (Second) Moments and Inertial Defect

It has been shown how the rotational constants relate to the principal moments of inertia of a molecule, which are a direct measure of mass distribution. Often, a more intuitive, initial insight into the structure of a molecule or complex that allows for more direct comparisons is obtained through the evaluations of planar (or second) moments ${ }^{8} P_{a a}, P_{b b}$, and $P_{c c}$. These are related to the principal moments of inertial via the expressions;

$$
\begin{align*}
& P_{a a}=\sum_{i} m_{i} a_{i}^{2}=\left(I_{b b}+I_{c c}-I_{a a}\right) / 2  \tag{Eq.2.70}\\
& P_{b b}=\sum_{i} m_{i} b_{\mathrm{i}}^{2}=\left(I_{a a}+I_{c c}-I_{b b}\right) / 2  \tag{Eq.2.71}\\
& P_{c c}=\sum_{i} m_{i} c_{\mathrm{i}}^{2}=\left(I_{a a}+I_{b b}-I_{c c}\right) / 2 \tag{Eq.2.72}
\end{align*}
$$

Conversion relies on the $\left(h / 8 \pi^{2}\right) N_{A}$ factor which relates the rotational constants $A, B$, and $C$ (in MHz) to the principal moments of inertia $I_{a a}, I_{b b}$ and $I_{c c}$ (in $\mathrm{u} \AA^{2}$ ) and to subsequently to $P_{a a}, P_{b b}$, and $P_{c c}\left(\right.$ in u $\AA^{2}$ ), where $N_{A}$ is Avogadro's number.

The inertial defect $\Delta$ is often used as a measure of the planarity of a molecule or complex. It is defined as;

$$
\begin{equation*}
\Delta=I_{c c}-I_{a a}-I_{b b}=-P_{c c} \tag{Eq.2.73}
\end{equation*}
$$

For a planar molecule at equilibrium, $\Delta=0$. Given that this thesis will be concerned with molecules at the zero-point, deviations from zero are expected because of low-lying vibrations. In general, in plane vibrations have a positive contribution to $\Delta$ whilst out-ofplane vibrations result in negative values of $\Delta$. The planar molecules with one $\mathrm{CH}_{3}$ group that does not perform internal rotation, the inertial defect is expected to be approximately $3.2 \mathrm{u} \AA^{2} . \Delta$ may assist with determination of heights of barriers to internal rotation in molecules with $\mathrm{CH}_{3}$ groups (PAM).

### 2.10.2 Substitution Structure $\left(r_{s}\right)$ and Kraitchman Equations

Single isotopic substitution of an atom in a molecule, allows for determination of the atomic coordinates of that atom in the parent molecule in the principal $a$-, $b$ - and $c$-axis system. The atomic coordinates are evaluated with Kraitchman's equations ${ }^{9,10}$ which are implemented in the program KRA. The equations can be specified for linear, symmetric, and asymmetric rotors by evaluating the measured zero-point rotational constants. The resulting structure is called the $r_{s}$ (s: substitution) structure. The calculations consider changes in the moments of inertia caused by isotopic substitution and only the relative magnitudes of the coordinates are calculated. The method does not account for rotationvibration effects, typically resulting in the $r_{s}$ structure being closer to equilibrium. Costain's errors ${ }^{10,11}$ can be calculated by means of $\delta z=0.0015 /|z|$, which are expressed as a fractional uncertainty of the magnitude of the coordinate, where $|z|$ is the magnitude of the relative coordinate. The method may perform poorly when determining the position of atoms close to the center of mass or an inertial axis by returning imaginary numbers.

The Kraitchman method assumes that the molecular structure does not change upon isotopic substitution. As it will be discussed later, this is not true for H/D substitution where an elongation of the bond-length is observed with D . The Kraitchman equations are;

$$
\begin{align*}
& |a|=\left[\frac{\Delta P_{a}}{\mu}\left(1+\frac{\Delta P_{b}}{I_{a}-I_{b}}\right)\left(1+\frac{\Delta P_{c}}{I_{a}-I_{c}}\right)\right]^{1 / 2}  \tag{Eq.2.74}\\
& |b|=\left[\frac{\Delta P_{b}}{\mu}\left(1+\frac{\Delta P_{c}}{I_{b}-I_{c}}\right)\left(1+\frac{\Delta P_{a}}{I_{b}-I_{a}}\right)\right]^{1 / 2}  \tag{Eq.2.75}\\
& |c|=\left[\frac{\Delta P_{c}}{\mu}\left(1+\frac{\Delta P_{a}}{I_{c}-I_{a}}\right)\left(1+\frac{\Delta P_{b}}{I_{c}-I_{b}}\right)\right]^{1 / 2} \tag{Eq.2.76}
\end{align*}
$$

where $\quad \Delta P_{a}=\frac{1}{2}\left(-\Delta I_{a}+\Delta I_{b}+\Delta I_{c}\right), \quad \Delta P_{b}=\frac{1}{2}\left(-\Delta I_{b}+\Delta I_{c}+\Delta I_{a}\right)$, and $\Delta P_{c}=\frac{1}{2}\left(-\Delta I_{c}+\right.$ $\Delta I_{a}+\Delta I_{b}$ ) and $\Delta I_{a}=I_{a}^{\prime}-I_{a}, \Delta I_{b}=I_{b}^{\prime}-I_{b}$, and $\Delta I_{c}=I_{c}^{\prime}-I_{c}$, where $\mu$ is the mass difference between the parent and the isotopically substituted molecule, $I_{a}, I_{b}, I_{c}$ and $I_{a}^{\prime}$, $I_{b}^{\prime}, I_{c}^{\prime}$ are the moments of inertia, respectively. The quantities $|a|,|b|$ and $|c|$, represent the atom coordinates along the $a-, b$-, and $c$-axis.

### 2.10.3 Effective Structure ( $r_{0}$ )

The effective $r_{0}$ structure is calculated by least square fitting of structural parameters to the experimentally determined moments of inertia derived from the zero-point rotational constants of the available isotopologues. The method does not consider changes that may be induced to the structure by isotopic substitution or large amplitude motions. The method is implemented in STRFIT ${ }^{12}$ and a detailed description of the method and program may be found in reference 12. The starting geometry of the molecule of interest is input as a $z$-matrix. Assumptions for the structure need to be made when there is not sufficient amount of isotopic information.

### 2.11 Quantum Chemical Calculations

A brief description of the quantum chemical methods that were used for this thesis is given here. All calculations were performed with the GAUSSIAN09 package. ${ }^{13}$ The performance of the methods is benchmarked against experimental results in chapters 4-7. A complete description of the methods and interpretation of the performance is beyond the scope of this thesis.

In rotational spectroscopy, particularly for complex asymmetric rotors, quantum chemical calculations greatly assist with spectral analysis. A typical broadband rotational spectrum consists of hundreds or even thousands of spectral lines. Molecules in the ground vibrational state co-exist as a gas phase mixture and are probed simultaneously. As a result, the spectral patterns usually overlap and identifying them is not straight forward. Quantum chemical calculations provide a starting point for the $A, B$ and $C$ rotational constants of a molecule and when combined with the appropriate dipole moment component, the relevant energy levels can be estimated, identified in the spectra and quantum numbers can be assigned. Quantum chemical calculations assist with estimation of energetic barriers, i.e. calculating the $V_{3}$ barrier to internal rotation in methylimidazole isomers in chapter 6 . Conformations beyond the global minimum of a molecular carrier can be investigated by examining local minima of a potential energy surface. In the case where a fully experimental structure is not available, i.e. in chapter 6 in methylimidazole isomers where no experimental data is available for the position of the hydrogen atoms, their position is based on their calculated equilibrium structure. Finally, vibrational modes can be identified which may indicate whether the structure of interest is a global or local minimum, or give an insight into internal motions (wag and torsion of the water subunit in chapter 5) and predict the centrifugal distortion constants.

For this thesis, Density Functional Theory (DFT) and ab initio calculations were performed. The DFT functional of Becke, Lee-Yang-Parr (B3LYP) ${ }^{14.17}$ is based on a combination of the exact Hartree-Fock functional and electron-electron exchange correlation to describe a molecular system. The method treats the molecular structure as a system of non-interacting electrons as a function of density. The energy is minimized such that the true ground state density is found. The B3LYP functional is used in conjunction with D3BJ empirical correction ${ }^{15,18,19}$ that accounts for dispersion interactions by avoiding repulsive interatomic forces. The long-range corrected functional $\omega$ B97X-D ${ }^{20}$ which includes empirical correction for dispersion interactions is also used. The ab initio second
order Møller-Plesset perturbation theory (MP2) was also used. The method considers electron correlation effects and as such dispersion interactions are accounted for.

Each functional must be used in conjunction with a basis set, which is made up by linear combination of functions which represent the orbitals in a molecular system. Dunning type basis sets, ${ }^{21-23}$ augmented with functions that account for core electron correlation (aug-cc$\mathrm{pVnZ}, \mathrm{n}=2,3$ ) are used here. Ahlirichs' Def2-TZVP basis set ${ }^{24}$ is also used; the valence shells are described by three functions whilst only one is used for the inner shells.

The exact functional-basis set combinations are indicated in each chapter for each molecular system.

### 2.12 Spectral Analysis and Fitting

Spectral analysis is performed with Watson's PGOPHER. ${ }^{25}$ Watson's A- and S-reduced Hamiltonians ${ }^{26}$ are implemented in PGOPHER. Rotational constants, centrifugal distortion constants up to the octic and nuclear quadrupole coupling constants can be determined through least square fitting of transition frequencies. The program allows for interactive viewing of measured broadband spectra alongside a simulation that is based on rotational constants calculated as described in section 2.4. Quantum numbers are assigned to measured transition frequencies and the spectroscopic parameters are least-squares fitted. It is crucial to use as few constants as possible for as many transition frequencies as possible with experimental accuracy of a few kHz . As a rule of thumb, the accuracy of the fit should be approximately $1 / 10$ of the linewidth of a well resolved line at full width at half maximum. However, this will be somewhat dependent on the molecule, the number of fitted transitions, internal motions, and hyperfine splitting.

PGOPHER is not programmed to deal with internal motions like internal rotation. For the problem of internal rotation, the XIAM program is used where simultaneous fitting of $A$ and $E$-states is possible. The A- and S-reduced Hamiltonians are implemented in XIAM and the fitting procedure is essentially the same as with PGOPHER; however, no graphical interface is available with XIAM.

### 2.13 References

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## Chapter 3. Experimental Methods

### 3.1 The CP-FTMW Spectrometer at Newcastle University

In this chapter a detailed description of the CP-FTMW spectrometer at Newcastle University ${ }^{1-3}$ will be provided. The instrument is designed to record broadband rotational spectra in a highly automated manner. The design of the spectrometer is based on an original design by Pate and co-workers ${ }^{4}$ with some modifications and additions. The spectrometer operates in the 2.0 to 18.5 GHz frequency range alongside an Arbitrary Waveform Generator (AWG) which is used for frequency signal generation. The two bands, $2.0-8.0 \mathrm{GHz}$ and $7.0-18.5 \mathrm{GHz}$ are covered in two different setups which can be interchanged by modification of the microwave circuit. A detailed description and a schematic of the circuit are given in the sections to follow. A bespoke laser ablation source using a pulsed laser is also installed in our spectrometer.

Advances in microwave spectroscopy have relied upon technological advances and the need to record spectra of transient and short-lived species. In 1934, Cleeton and Williams ${ }^{5}$ recorded the absorption spectrum of ammonia in the $1-3 \mathrm{~cm}$ region using continuous radiation. That was one of the first microwave spectroscopy experiments to be performed with such short wavelengths. In 1975, Ekkers and Flygare ${ }^{6}$ reported a microwave spectrometer that operated using short microwave pulses from Travelling-Wave Tube Amplifiers (TWTA) as opposed to continuous sample irradiation. Their design also featured time domain measurements which offered significant improvements in the signal to noise of molecular signals.

As vacuum technology evolved, in 1981, Balle and Flygare ${ }^{7}$ implemented a pulse valve molecular source allowing molecules of interest to adiabatically expand into a vacuum chamber enclosing a Fabry-Perot cavity. The gas pulse is followed by a short microwave pulse resonating in the cavity which polarizes a frequency band, typically approximately 1 MHz bandwidth. Detection of molecular emissions after the halt of the polarizing pulse is also performed in the time domain and Fourier transformed to the frequency domain rotational spectrum. The spectrometer designed by Pate and co-workers ${ }^{4}$ was introduced in 2008 and allowed to scan large bandwidths of up to 12 GHz in a single acquisition shot using chirped microwave pulses. The Fabry-Perot cavity of the Balle and Flygare spectrometer is replaced by microwave horn antennas.

Given that the design of the CP-FTMW spectrometer at Newcastle University is based on existing setups, the experimental cycle consists of a sequence of events with the insertion of gas phase molecules into the vacuum chamber being the first one in line. If the molecules of interest are solid at room temperature $\left(\sim 20^{\circ} \mathrm{C}\right)$, a laser pulse can follow which will rapidly vaporize molecules into the gas phase. A microwave excitation pulse polarizes the gas phase molecules, and their molecular emissions are recorded at the detection end after the halt of the polarizing pulse. Typically microwave pulses broadcast through horn antennas and perpendicularly to the direction of the expanding gas. An exception to that is the spectrometer described by Finneran et al. in which the microwave pulse travels coaxially to the gas sample. ${ }^{8}$


Figure 3.1. Schematic of the various events in the experimental cycle. Note that the protective switch remains open for the duration of the chirped pulse and before and after the pulse.

### 3.2 Supersonic expansion

In this work, the term supersonic expansion refers to a gas or gas mixture expanding into a vacuum chamber at a speed greater than that of sound. Supersonic expansion allows efficient conversion of enthalpy to direct mass flow, which generates an environment of rotationally cooled species ( $\sim 2-3 \mathrm{~K}$ ) free of solvent and lattice effects. Low internal temperature results in population of low energy states which significantly simplifies the spectral patterns we observe. An outstanding example that highlights the benefits of rotational cooling was discussed by Smalley and co-workers. ${ }^{9}$ In optical spectroscopy, matrix isolation experiments are common and allow study of complex molecules. However, the matrix can induce perturbations in the spectra and information carried in the rotational structure is lost. Supersonic expansion methods allowed for observation of the fluorescence absorption spectrum of $\mathrm{NO}_{2}$ with individually resolved vibronic and rovibronic bands identifiable in the spectrum.

As the supersonic jet propagates, the molecular velocities can exceed that of sound resulting in supersonic speeds with $M>1$, where $M$ is the Mach number describing the ratio of the speed of the expanding jet to the local speed of sound. ${ }^{10}$ As the gas expands, the collision free zone or zone of silence is approached, and molecular collisions are effectively halted. At that point, the jet has reached its lowest internal temperature and optimal conditions for the sample to interact with the microwave pulse are provided. Measurements under high vacuum conditions could elongate the collision free zone and position it directly between the two horn antennae (approximately 30 cm from the orifice of the pulse valve which is described below) for efficient radiation-sample interrogation. The vacuum system is described in detail in section 3.4.

A pulsed valve (Parker General Valve, series 9) is employed for supersonic expansion throughout this thesis. The valve opening time ( $800-1000 \mu \mathrm{~s}$ ) and repetition rate ( $1-2 \mathrm{~Hz}$ ) are controlled by a valve driver (Parker, IOTA ONE, Micro fluidic valve driver). Gas expands through the 0.7 mm orifice of the valve and into the vacuum chamber. Typically, an inert carrier gas such as He , Ne or Ar is kept at high backing pressure and acts as a means of cooling the expanding jet.

The interactions between molecules and inert gas atoms in a supersonic expansion can be complicated. Switching between carrier gases can have a drastic effect on the temperature of the expanding jet and therefore affect the population of species for different rotational states. In the spectra, this is depicted as a change in the signal strength of rotational transitions. The effect of the carrier gas on conformational relaxation was examined in conformational isomers of trans-urocanic acid. ${ }^{11}$ The four possible conformers of transurocanic acid are observed when neon is used as the carrier gas. The relative intensity of rotational transitions of the conformers is analogous to their calculated energies. The high energy conformers relax into a more stable configuration when neon is substituted by argon. However, the relative energy of the conformers is not the only factor that influences the relative intensity, i.e. dipole moment, power and duration of polarizing pulse (section 3.12).


Figure 3.2. Supersonic expansion schematic (not to scale).

Relaxation is a result of efficient cooling of molecular species in the supersonic expansion. Molecular species that are high in energy may relax into a more stable configuration due to energy transfer through inelastic collisions with the inert carrier gas atoms. Energy that is equal to the energy difference between a high energy configuration and a relaxed configuration may be redistributed internally in the molecule or absorbed by the carrier gas atoms. Typically, the heavier the carrier gas, the more efficient the cooling may become, with krypton being able to relax molecules with high energy barriers. Following this basis, helium and neon would be the choice of carrier gas in order to study high energy conformers, excited and meta-stable species.

In some cases, during the collisional process, molecules may interact with inert gas atoms. During supersonic expansion, mixed weakly-bound complexes of the molecules of interest and an inert gas atom can be "frozen" out and isolated. The energy required for complex formation is absorbed by the unreacted carrier gas atoms. Adiabatic cooling allows for weakly-bound complexes ${ }^{12}$ such as the $\mathrm{Ar}{ }^{\cdots} \mathrm{AgI}$ and the phosphine carboxamide ${ }^{*} \mathrm{Ar}$ complexes (chapter 4), to be isolated and spectroscopically characterized. It is also common to observe complexes formed between the molecules of interest and other molecules that may be present in the supersonic expansion, i.e. the imidazole-water complex (chapter 5) and the methylimidazole water complexes (chapter 7).

The maximum velocity of an expanding inert gas is determined by the relationship;

$$
\begin{equation*}
u_{\max }=\sqrt{\frac{2 C_{p} T_{0}}{m}} \tag{Eq.3.1}
\end{equation*}
$$

where $C_{p}=\frac{5}{2} R$ is the constant-pressure molar heat capacity, $T_{0}$ is the temperature of the gas reservoir (in our case, room temperature $\sim 20-21^{\circ} \mathrm{C}$ ) and $m$ is the molar mass of the molecules. The maximum velocity of Ar is calculated to be $5.5231 \times 10^{4} \mathrm{~cm} \mathrm{~s}^{-1}$ which is greater than that of sound, $3.34 \times 10^{4} \mathrm{~cm} \mathrm{~s}^{-1}$.

For the experiments described here, a free pulsed jet expansion was used where an inert carrier gas (Ar) is kept at a high backing pressure (2-7 bar) at one end and expands into a high vacuum chamber (low pressure $10^{-6}-10^{-7}$ mbar).

### 3.3 Heated Reservoirs and Band Heaters



Figure 3.3. General pulse valve and bespoke reservoir that attaches onto the face plate of the valve. Gas expands through the 0.7 mm orifice. (Design 1)

A bespoke heated reservoir that attaches onto the face plate of the pulse valve can be used for the study of liquid samples, as seen in figure 3.3. Molecules can be seeded directly into the flow of the expanding jet of the inert gas. The reservoir provides high control over the amount of sample that is used during an experiment and this will be further discussed in the chapters to follow when where heavy water $\mathrm{D}_{2} \mathrm{O}$ and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ were used.

The initial design (Design 1) of the reservoir is displayed in figure 3.3. The face plate of a general pulse valve was modified by the mechanical workshop at Newcastle university so that the four holes ( $\sim 0.05 \mathrm{~mm}$ in diameter) that serve for seeding molecules into the gas flow are surrounding the orifice. A brass reservoir was machined so that it can be mounted on the modified face plate. The orifice channel on the brass reservoir is exactly in line with the orifice on the face plate so that supersonic expansion can be achieved despite the modifications and additions. An o-ring is placed around the reservoir so that the face platereservoir assembly can be pressurized without any gas or sample leaks. A schematic representation of sample seeding into the carrier gas flow is illustrated in figure 3.5.

It was necessary to rebuild the reservoir due to significant wear and tear damage to the oring groove on the brass part. High pressures in the reservoir caused the walls of the groove
to bend and eventually break leading to sample leaks. For the advanced reservoir design (Design 2), it was crucial not to place any o-rings on the brass parts. Instead, the o-ring was placed on the face plate. Design 2 of the reservoir and face plate are displayed in figure 3.4. This version of the reservoir combined with a band heater was used to improve the recorded spectrum of $N$-methylimidazole, as discussed in chapter 7. It was seen that filling the reservoir with glasswool before placing the liquid $N$-methylimidazole in, significantly extended the sample lifetime and allowed for long measurements ( $\sim 72 \mathrm{~h}$ ) without replacing the sample in reservoir.


Figure 3.4. The modified faceplate and reservoir assembly. The o-rings are placed on the steel faceplate instead of on the brass reservoir.


Figure 3.5. Schematic representation of the reservoir function illustrating how the sample (red dots) is seeded into the expanding jet of argon (purple dots). The dashed lines trace from the openings of the faceplate and onto the reservoir. (a) the pressurized argon buffer is in the gas line behind the reservoir. The sample is at 1 atm in the reservoir. (b) the reservoir is pressurized, and the sample is mixed with the argon buffer. (c) the argonsample mix expands into the vacuum chamber.

### 3.4 Diffusion Pump and Vacuum Chamber

Gas phase measurements and supersonic expansion require a high vacuum chamber. The chamber is built from a stainless steel six-way cross with ISO 250 ports. The horn antennas attach on both sides of the chamber as shown in figure 3.6 while the vacuum system connects to the bottom port. The gas feedthrough to the pulse valve, the laser ablation source (section 3.5) and their power supplies are found on the back flange. A viewport on the front flange allows monitoring of the experiment and easy access to the chamber's interior. High vacuum ( $\sim 10^{-6}-10^{-7} \mathrm{mbar}$ ) is achieved by use of a water-cooled diffusion pump (Edwards Diffstak 250) alongside two rotary mechanical pumps (Edwards EH250 and EM240). The pressure inside the chamber is constantly monitored by two pressure gauges (Pirani gauge, Edwards APG100 and Magnetron gauge) as it is crucial that it remains low so that the supersonic jet is cooled down efficiently. The chamber's interior is layered with microwave absorbent polyurethane foam to minimize background reflections interfering with molecular signals.


Figure 3.6. Front on schematic representation of the vacuum chamber. The transmission and detection horn antennas are found on both sides of the chamber.

### 3.5 Laser Ablation Source and Rod Preparation

Rapid gas phase generation of solid compounds is achieved by employing a pulsed nanosecond Nd:YAG laser (Photonics Solutions, Continuum, Minilite II) and a bespoke laser ablation source. The laser beam is focused on a rotating target rod which contains the molecules of interest and vaporizes material without destroying the molecular structure. The rod is positioned approximately $2-3 \mathrm{~mm}$ from the orifice of the pulse valve. A motor and a switch ensure that the rod is rotating and translating so that material from all over its length is exploited. A fresh surface of material is exposed to every laser pulse which was shown to increase the intensity of molecular signals. The target rods are prepared by grinding the solid samples of interest and mixing them with a small amount of metal powder (e.g Cu ) which acts as a binder. The mixtures are then pressed into 5 or 13 mm diameter rods by a hydraulic bench press.

It was discovered that mixing in a small amount of desiccant such as $\mathrm{MgSO}_{4}$ with hygroscopic and low melting point ( $\sim 30-45{ }^{\circ} \mathrm{C}$ ) substances significantly increases the lifetime and quality of the rods. The melting point of the tautomeric mixture of 4(5)methylimidazole (Sigma-Aldrich, $98 \%$ ) is $44-47{ }^{\circ} \mathrm{C}$. The mixture was also moderately hygroscopic which made it impossible to press into a rod. Exposure to air and mixing with Cu powder turned the mixture into a paste. Besides Cu powder, $\mathrm{MgSO}_{4}$, which has a high affinity for water, was used to bind the rod. Figure 3.7 shows the rod (A) containing 4(5)methylimidazole: Cu powder: $\mathrm{MgSO}_{4}$ (1:1:1 by mass) attached on the bespoke laser ablation source. Important parts of the ablation source are also labelled. The ablation source attaches onto the back flange of the vacuum chamber. The pulse valve attaches behind the block and the target rod so that the gas can expand through the orifice of the block (B) and efficiently entrain laser vaporized material into the supersonic jet.

The motor (C) (Faulhaber, DC 1524024 SR) is found at the top of the source and translates the rod downwards until it reaches its limit and hit the switch (D) which will change the direction of translation and rotation. A bespoke power supply box, referred to as Laser Ablation Controller, is shown in figure 3.8 and allows control over the rotation speed ( F ) of the rod and reverse translation timings. Three control modes (G) referring to the length of the rod, short ( $<2 \mathrm{~cm}$ ), medium ( $>2 \mathrm{~cm},<3 \mathrm{~cm}$ ) and large ( $>3 \mathrm{~cm}$ ) are implemented and alongside the time dial $(\mathrm{H})$ the reverse translation duration is controlled. Reverse translation can also be induced by pressing the start button (I) and paused by the stop button, a particularly useful function that allows fine optimization of the ablation source.

The laser beam (E, red dashed line) approaches the sample rod from the side and perpendicularly to the direction of the expanding gas.


Figure 3.7. The bespoke laser ablation source attached on the back flange of the vacuum chamber. A: Rotating target rod, B: 0.7 mm orifice for gas expansion, C: DC motor, E: Pulsed laser beam.


Figure 3.8. The laser ablation controller.

Recent modifications of the laser ablation source include the use of the fundamental harmonic ( $1064 \mathrm{~nm}, 42 \mathrm{~mJ} /$ pulse, 10 ns ) of the pulsed Nd:YAG laser. Previous laser ablation experiments within the group exclusively exploited the $2^{\text {nd }}$ harmonic ( $532 \mathrm{~nm}, 15$ $\mathrm{mJ} / \mathrm{pulse}, 10 \mathrm{~ns}$ ). It was shown that the 1064 nm wavelength could provide good conditions for organic complex formation and significantly boost molecular signals, for example, imidazole (chapter 5) and 4(5)-methylimidazole (chapter 6). The signal to noise ratio of the 4(5)-methylimidazole spectrum was improved by approximately a factor of 100 when the 1064 nm wavelength was used. It is not clear whether the wavelength doubling or the increase in output power have the most profound effect on the signal intensity. A test where the laser power is adjusted to approximately $15 \mathrm{~mJ} /$ pulse, equal to the power output of the $2^{\text {nd }}$ harmonic, is necessary to answer that question. A portion of the spectrum is shown in figure 3.9 and some improved molecular signals are marked with asterisks (purple asterisk: 4-methylimidazole, green asterisk: 5-methylimidazole).


Figure 3.9. (top panel) The spectrum collected when vaporizing a rod made of 4(5)methylimidazole: $\mathrm{Cu}: \mathrm{MgSO}_{4}$ (1:1:1 ratio) with the 1064 nm of the pulsed $\mathrm{Nd}: Y A G$ laser. (bottom panel) The spectrum collected using the same rod composition with 532 nm wavelength. Some transitions for 4-methylimidazole and 5-methylimidazole are marked with purple and green asterisks, respectively. The scale on the $y$-axis is the same for both panels and the intensity units are arbitrary.

### 3.6 Excitation Circuit

### 3.6.1 The 7.0-18.5 GHz region

A chirped pulse spanning between 12.0 and 0.5 GHz is generated by a $20 \mathrm{GS} / \mathrm{s}$ AWG (Tektronix AWG7102) and passes through a low pass filter (Lorch, 12.2 GHz ) and a triple balance mixer (MITEQ, TBO 440LWI-R). The chirped pulse is mixed against a 19 GHz reference signal provided by a Phase Locked Dielectric Resonant Oscillator (Herley CTI, PDRO, XPDRO-14373). The resulting higher frequency sideband ( $31.0-19.5 \mathrm{GHz}$ ) is filtered out (K\&L Microwave, 3C60-19000/T100-O/O). Only the lower frequency band between 7.0 and 18.5 GHz which passes through a pre-amplifier (MITEQ, AMF-5F-080018-14-10P-R) can reach a 300 W Travelling-Wave Tube Amplifier (TWTA). Attenuation prior to amplification is required to protect the TWTA from high input signals. The chirped pulse broadcasts through a horn antenna (ATM 750-442-C3) to polarize the molecular ensemble formed by supersonic expansion inside the vacuum chamber.

### 3.6.2 The 2.0-8.0 GHz region

A chirped pulse spanning between 2.0 and 8.0 GHz is generated by a $20 \mathrm{GS} / \mathrm{s}$ AWG. No mixing is required, and the chirped pulse is attenuated and sent directly to the TWTA for amplification. It subsequently broadcasts via the horn antenna into the vacuum chamber. The PDRO and low pass filters are removed from the circuit.

### 3.7 Sample polarization

The excitation microwave pulse propagates perpendicularly to the flow direction of the supersonic expanding jet that contains the molecules of interest. The oscillating electric field of the microwave photons couples the electric field gradient of the polar molecules and energy is provided to induce molecular resonant rotations. The sample is polarized for $1 \mu$ s half-way between the horn antennas which are placed approximately 50 cm apart, as displayed in figure 3.6. The horn antennas are fixed in the vacuum chamber and do not require adjustment during measurements in either frequency range.

### 3.8 Detection Circuit

### 3.8.1 The 7.0-18.5 GHz region

Molecular emissions are detected in the form of a free induction decay (FID) after the pause of the microwave excitation pulse. The FID's are recorded by a second horn antenna. A pin diode limiter (ACLM-4539C6R1K) and a pin diode switch (Arra H87538OD) which only remains open during the collection of the FIDs, are used to protect the detection end from powerful microwave pulses. Molecular signals are amplified by a low noise amplifier (MITEQ, AMF-5F-08001800-14-10P-R). Given the frequency range of the oscilloscope ( $0.0-12.5 \mathrm{GHz}$ ), mixing prior to digitization is required at the detection end too. Mixing against the 19 GHz reference provided by the PDRO proceeds via a triple balance mixer and a low pass filter eliminates frequencies above 12 GHz . The input signal $12.0-0.5 \mathrm{GHz}$ is digitized by a $100 \mathrm{GS} /$ s oscilloscope (Tektronix DPO72304XS). The first $20 \mu$ s of the FID are digitally recorded in the time domain and then Fourier transformed to the frequency domain spectrum.

### 3.8.2 The 2.0-8.0 GHz region

The same principles mentioned above apply for the detection circuit of the $2.0-8.0 \mathrm{GHz}$ range, but mixing is not required. Thus, the PDRO and low pass filters are removed from the detection end of the microwave circuit.

### 3.9 Nyquist Limit and Sampling

The bandwidth that is detectable by the oscilloscope in a single experimental cycle is dependent on the sampling rate and the Nyquist limit. ${ }^{13}$ Sampling refers to the conversion of a continuous signal to a discrete signal. A sample is a datapoint of the resulting wavefunction. The maximum bandwidth that the oscilloscope is required to cover is 11.5 GHz . To achieve this bandwidth, the oscilloscope is set to operate at a sampling rate of 25 GS/s at most. This is referred to as the Nyquist frequency which is approximately half of the sampling rate. The sampling rate could be increased; however, this would compromise the digitizing and Fourier Transform speed.

### 3.10 Triggers and Timings (Fast Frame Acquisition Mode)

Fine control over the timings and duration of the different events of the experimental cycle is important in order to obtain high quality spectra and protect the spectrometer from irreversible damage. Timings are controlled by two delay generators, A (Quantum Composers, 9520 Series) and B (Quantum Composers, 9518 Series) and the AWG. These instruments provide high accuracy and phase stability in the time domain with less than 50 ps and 30 ps phase jitters, respectively.

The valve driver is triggered by Channel A of delay generator A which is set on internal trigger and that determines the $T_{0}$ point of the experiment. Typically, the duration of the gas pulse is determined by the inert gas in which the molecules of interest are seeded. In the case of Ar and Ne, the pulse duration is approximately $2 \mu \mathrm{~s}$. The AWG is triggered for $51 \mu \mathrm{~s}$ by Channel B of the same delay generator approximately $1400 \mu \mathrm{~s}$ after $T_{0}$. To assist generation of intense molecular signals, the trigger delay to the AWG can be adjusted and it depends on i) the valve tension (i.e. how tight the valve is and how much gas flows through it), and ii) whether it is a laser ablation experiment. Usually, in a laser ablation experiment the trigger to the AWG is further delayed so that more time is allowed for the supersonic jet to interact with the laser plasma. The Q-Switch of the Nd:YAG is triggered for $100 \mu$ s by channel C, $1300 \mu$ s after $T_{0}$ and, as in Channel B, the delay can be adjusted with respect to the valve tension. As a rule of thumb, $100-400 \mu$ s are allowed between the two trigger pulses. The flashlamps are controlled by Channel D and triggered $164 \mu \mathrm{~s}$ before the Q-Switch which was found to be the optimal delay for maximum laser power output.

The delay generator B is triggered externally by Channel 1 of the AWG (master trigger) operating at interleaved mode to exploit its sampling rate ( $20 \mathrm{GS} / \mathrm{s}$ ) to the full. Channel A of delay generator $B$ controls the opening times of the pin diode switch which must remain open during the high-power excitation pulse to protect the oscilloscope from damage. The switch remains opens for $2 \mu \mathrm{~s}$ with a $0.75 \mu \mathrm{~s}$ delay relative to the master trigger. A $1.5 \mu$ s trigger pulse is sent to the TWT by Channel B with $1 \mu$ s delay. When the switch is closed $2.75 \mu \mathrm{~s}$ after the master trigger, the first channel of the oscilloscope is triggered by Marker 1 of the AWG to collect a $20 \mu$ sID.

Molecules in the supersonic jet remain in the collision free zone for approximately $200 \mu \mathrm{~s}$. Considering the duration of the excitation pulse and the FID, the oscilloscope's fast frame
operation mode can be used. Each gas pulse can be polarized eight times, each followed by an FID collection. The AWG sends eight trigger pulses to delay generator B and to the oscilloscope which collects eight frames of FID's. The FIDs are co-added in the time domain and Fourier transformed to the frequency domain spectrum using a highresolution window provided by Tektronix. Spectra are saved at given real time intervals by a Python script.

The pulsing rate of the valve and thus the repetition rate of the experiment is typically 2 Hz , which can be controlled by delay generator A . The maximum repetition rate that can be achieved is 4.5 Hz and this is limited by the pumping speed and the sampling rate of the oscilloscope.

### 3.11 Linewidths and Resolution ( $x$-axis)

The linewidths and resolution of the frequency domain spectra are dependent on several factors. The linewidth at full width half maximum (FWHM) of the line intensity is inversely proportional to the FID duration. Given that the FID is recorded for $20 \mu \mathrm{~s}$ the resulting linewidths should be in the range of $50-60 \mathrm{kHz}$. It should be considered that the molecules travel inside the vacuum chamber and are not treated as stationary points. Phase jitters in the time domain in the range of 30 ps can also induce line broadening. Finally, the Fourier transform methods should be considered. Throughout this thesis, high resolution and Kaisser-Bessel windows were used, each offering different advantages. Sharper lines and accuracy in peak position is offered by the high-resolution window which also provides an increase in spectral resolution by approximately 10 kHz . The latter provides a better baseline resolution and allows to distinguish between molecular signals and noise. A decrease in spectral resolution is observed by broadening the FWHM by approximately 10 kHz . Considering all these factors, the reported linewidths are approximately 100 kHz . Typically, the error associated with recorded lines is approximately $10 \%$ of the linewidth. These arguments are only true for well isolated and well resolved lines, excluding effects that can be induced by presence of quadrupolar nuclei, i.e. nitrogen and deuterium which are known to cause hyperfine splittings, sometimes in the range of only a few kHz .

Accuracy in the measured transition frequencies and phase coherence in the time domain is provided by a Rb-clock (SRS FS725) to which the AWG, the PDRO and the oscilloscope are phase locked. The Rb -clock provides a 10 MHz reference signal with $\pm 5 \times 10^{-11} \Delta \mathrm{f} / \mathrm{f}$ accuracy.

### 3.12 Spectral Intensity ( $y$-axis)

It was discussed earlier that signal intensity of e.g. conformers may be reflected through their relative energies. The intensity of measured lines is also proportional to the square of the dipole moment of the molecule responsible for a molecular signa1 ${ }^{13,14}$. In CP-FTMW the intensity units in the $y$-axis are arbitrary. Conclusions about relative intensities of different species in the spectra can be drawn, however, insufficient information is provided so no arguments can be made regarding number density of a molecular species in the molecular ensemble.

In chapter 2, it was discussed that molecules are required to possess a permanent electric dipole to be studied with rotational spectroscopy. Intensities also depend on the population of the lower state of a transition. The ratio of the population between two states is given by;

$$
\begin{equation*}
\frac{N_{J}}{N_{0}}=(2 J+1) \exp \left(-\frac{E_{J}}{k T}\right) \tag{Eq.3.2}
\end{equation*}
$$

where $N_{0}$ is the number of molecules at equilibrium and $N_{J}$ the number of molecules in a rotationally excited state.

Intensity of measured lines also depends on the power of the polarizing pulse and the pulse duration. This traces to a concept know as fast passage which arises when a frequency or range of frequencies are swept in a time relatively short to the dephasing time, i.e. FID. Chirped pulses must maintain phase coherence so that molecular emissions are also phase coherent and can be averaged in the time domain, as explained earlier. McGurk et al. ${ }^{15}$ and Dreizler ${ }^{16}$ approached molecular polarization by a chirped pulse by solving the optical Bloch equations modified to describe the electric dipole moment, equivalent to unpaired electrons in NMR. The molecular ensemble can be approximated as a two-level system of $N$ molecules which undergo macroscopic polarization. The total component of the macroscopic dipole moment of the ensemble may be denoted as $\dot{P}$ and consists of two components, $P_{r}$ and $P_{i} . P_{r}$ is aligned with the direction of the electric field of the chirped pulse and $P_{i}$ is $\pi / 2$ phase separated. The populations of the two states are denoted as $N_{a}$ and $N_{b}$, respectively, with $\Delta N=N_{a}-N_{b}$. A dephasing time is associated with each of $N_{a}$ and $N_{b}$; these are $T_{1}$ and $T_{2}$. The Bloch equations, tailored to describe chirped pulse excitation followed by relaxation, are;

$$
\begin{gather*}
P_{r}+\left(\omega_{0}-\omega\right) P_{i}+\frac{P_{r}}{T_{2}}=0  \tag{Eq.3.3}\\
P_{i}-\left(\omega_{0}-\omega\right) P_{r}+k \varepsilon \frac{\hbar}{4} k \Delta N+\frac{P_{i}}{T_{2}}=0  \tag{Eq.3.4}\\
\frac{\hbar}{4} k \Delta N-k \varepsilon P_{i}+\frac{\hbar \Delta N-\Delta N_{0}}{4}=0 \tag{Eq.3.5}
\end{gather*}
$$

where $k=2 \mu_{a b} / \hbar$ with $\mu_{a b}$ being a matrix element of the dipole moment operator of a Hamiltonian ${ }^{\text {A }}$ that includes the time-dependent perturbation element of the MW field and $2 \varepsilon$ being the MW field amplitude.

Assuming that the experiment is concerned with fast passage phenomena, the MW pulse duration, $t_{p}$, will be much shorter than $T_{1}$ and $T_{2}$ relaxation times. Then equations 3.3-3.5 can be approximated to;

$$
\begin{gather*}
P_{r}+\Delta \omega P_{i}=0  \tag{Eq.3.6}\\
P_{i}-\Delta \omega P_{r}+k^{2} \varepsilon \frac{\hbar}{4} \Delta N=0  \tag{Eq.3.7}\\
\frac{\hbar}{4} \Delta N-\varepsilon P_{i}=0 \tag{Eq.3.8}
\end{gather*}
$$

If $P_{r}=0$ and $P_{i}=0$, it gives a solution to equations 3.6-3.8. It was shown that the maximum signal for a transition can be obtained for a resonant MW pulse is;

$$
\begin{equation*}
k \varepsilon t_{p}=(2 n+1) \pi / 2 \quad n=1,2, \ldots \tag{Eq.3.9}
\end{equation*}
$$

The electric field of a chirped pulse is given by;

$$
\begin{equation*}
E(t)=E_{\max } e^{i\left(\omega_{0} t_{p}+\frac{1}{2} \alpha t_{p}^{2}\right)} \tag{Eq.3.10}
\end{equation*}
$$

where $E_{\max }$ is the maximum strength of the polarizing pulse, $\alpha$ is the sweep rate, and $\omega_{0}$ is the initial frequency. The frequency range of the pulse, $\Delta \omega$, is proportional to the pulse duration, $t_{p}$;

$$
\begin{equation*}
\Delta \omega=\alpha t_{p} \tag{Eq.3.11}
\end{equation*}
$$

The signal intensity can be expressed as a function of the sweep rate, $\alpha$;

[^0]\[

$$
\begin{equation*}
\text { Signal } \propto \omega \mu^{2} E_{\max } \Delta N_{0}\left(\frac{\pi}{\alpha}\right)^{\frac{1}{2}} \tag{Eq.3.12}
\end{equation*}
$$

\]

where $\omega$ is the frequency, $\mu$ is the electric dipole moment, $E_{\max }$ is the maximum strength of the polarizing pulse, and $\Delta N_{0}$ is the population difference between states. ${ }^{17-19}$

In comparison to previous techniques such as that developed by Balle and Flygare, CPFTMW requires more peak power to polarize a molecular ensemble. The Farby-Perot cavity of the Balle-Flygare spectrometer creates a resonance with the polarizing MW pulse that amplifies the signal to cover the bandwidth of approximately 1 MHz . The large bandwidth that is covered by CP-FTMW spectrometers requires alternative high-power sources such as TWT amplifiers discussed earlier.

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## Chapter 4. Spectrum of Phosphine Carboxamide and its Van der Waals <br> Complex with Argon

### 4.1 Introduction

Primary phosphines are a class of chemicals with potential versatile applications in the synthesis of functionalized phosphorus compounds. The $\mathrm{P}-\mathrm{H}$ bonds in primary phosphines can be extremely reactive allowing a number of compounds to be accessed ${ }^{1}$. However, primary phosphines, particularly those with low molecular weight, are notorious for being difficult to handle. Air sensitivity, noxious character, high toxicity, spontaneous combustion, and unpleasant, garlic-like odor are namely a few of the reasons why there is only a limited number of phosphorus-functionalized compounds.

In 2013, Jupp and Goicoechea ${ }^{2}$ reported the synthesis of a primary phosphine that exhibits remarkable air and moisture stability. The compound, namely phosphine carboxamide (PCA) figure 4.2, is a phosphorus containing analogue of urea and thiourea arising from reaction of ammonium salts with 2-phosphaethynolate ions. Typically, the stability of primary phosphines arises from bulky groups surrounding the $-\mathrm{PH}_{2}$ group or electronic effects stabilizing the lone pair of phosphorus. However, it was shown that the stability of PCA may arise due to a large bandgap between HOMO and LUMO and mixing of $\pi$ orbitals. NMR studies suggest an essentially planar arrangement in the carboxamide subunit with significant lone pair delocalization over the carbonyl and amide sites. Some minor delocalization is observed on the phosphine site with minimal interactions between


Figure 4.1. Schematic representation of the resonance canonicals of PCA.


Figure 4.2. The structure of PCA and its structural analogues, urea and thiourea. Absence of a $\mathrm{C}_{2}$ axis in PCA highlights the asymmetry of the molecule.
the phosphine lone pair and the carbonyl carbon. The resonance canonicals and chemical composition of PCA are depicted in figure 4.1.

Phosphorus is a biochemically significant element found in phospholipids, DNA, RNA and cell membranes. ${ }^{3,4}$ It is the $18^{\text {th }}$ most abundant element in the interstellar medium (ISM), behind carbon, nitrogen and oxygen. ${ }^{5}$ Knowledge around the gas phase chemistry of P is limited but it is thought that P is formed at massive star regions and thrown into the ISM through supernovae explosions. ${ }^{5}$ Up to date, a total of six P-containing compounds ${ }^{6-}$ ${ }^{11}$ have been detected in the ISM by means of their rotational spectrum, including PN, CP, HCP, PO, CCP and $\mathrm{PH}_{3}$, in chronological detection order, in circumstellar envelopes around evolved stars. Only PN was detected at hot and dense regions of interstellar clouds ${ }^{6}$ like Orion-KL and SgrB2. Formation of these compounds is yet to be fully comprehended but would likely require large activation energies involving endothermic and bond cleavage reactions of larger molecules.

These compounds account for a very small percentage of the total cosmic P suggesting that the rest of P is elsewhere or in a different form, i.e. condensed onto ice grains or in meteorites in the solid state. The main source of P in some meteorites is in the form of minerals like $(\mathrm{Fe}, \mathrm{Ni})_{3} \mathrm{P}$ (schreibersite) and phosphoric acids. Also, $\mathrm{PH}_{3}$ is detected in the atmospheres of Jupiter and Saturn ${ }^{12-14}$ whilst $\mathrm{P}^{+}$has been detected in diffuse clouds. ${ }^{15}$ Given the limited number of confirmed P sources, it is no surprise that much research still needs to be done in order to unravel the gas phase chemistry of P compounds.

Unlike $\mathrm{P}, N$-containing molecules are abundant in the ISM compared to P and significant steps have been made towards understanding the chemical reactions behind their formation. Linear unsaturated nitriles ${ }^{16,17}$ are amongst the most common N -bearing molecules in the ISM. More complex molecules such as formamide ${ }^{18}$ and N methylformamide ${ }^{19}$ have also been detected in both the ISM and comets and these are thought to play an important role in life formation on Earth. Urea (figure 4.2) was unambiguously detected in the ISM in 2019 by Belloche and co-workers ${ }^{20}$ at SgrB 2 by means of its rotational spectrum after a number of inconclusive studies. ${ }^{21}$ Given that N and P are both group 15 elements, it is worth exploring whether more P -analogues of $N$-bearing compounds are detectable in the ISM. Here, we wish to bring PCA, a urea analogue, to the attention of astronomers and astrochemists as a possible interstellar P-containing candidate molecule.

Microwave spectroscopy studies of urea ${ }^{22-25}$ and thiourea ${ }^{26}$ allowed for interstellar detection of the former ${ }^{20}$ and precise structure determination of both molecules in the gas phase. A planar arrangement between the heavy atoms O, C, N1 and N2 and S, C, N1 and N2, respectively, is reported for both molecules. A slightly pyramidal configuration is observed at the $-\mathrm{NH}_{2}$ sites resulting in an overall $\mathrm{C}_{2}$ point group for both urea and thiourea. ${ }^{27}$ Solid phase urea and thiourea, however, are planar with $\mathrm{C}_{2 \mathrm{v}}$ geometry. A rigidly pyramidal configuration is adopted around the $-\mathrm{PH}_{2}$ site of PCA, according to NMR and crystallography studies, giving rise to the asymmetry of the molecule. As in urea and thiourea, a planar $\mathrm{O}, \mathrm{C}, \mathrm{N}$ and P heavy atoms skeleton is reported for PCA.

A recent study by Mullaney et al. reported the formation of a hydrogen bonded complex between urea and isocyanic acid following laser ablation of urea in a supersonic expansion. ${ }^{28}$ Thermal decomposition of urea results in formation of ammonia and isocyanic acid. ${ }^{29}$ It is therefore suggested that isocyanic acid was generated as a side product of laser ablation of urea. It is reported that PCA will decompose to $\mathrm{PH}_{3}$ and isocyanic acid when heated to $55-60^{\circ} \mathrm{C}$. Given that neither $\mathrm{PH}_{3}$ nor isocyanic acid ${ }^{30-33}$ have any detectable transitions in the frequency range covered by the CP-FTMW spectrometer at Newcastle University, it is not possible to say whether these products are formed as a result of laser ablation of PCA.

In this chapter, the microwave spectrum of three isotopologues of PCA (parent, ${ }^{13} \mathrm{C},{ }^{15} \mathrm{~N}$ ) are reported and spectroscopically characterized for the first time. The spectrum of a van der Waals complex between PCA and Ar was also recorded simultaneously and is reported
and characterized here. Typically, an Ar atom will coordinate with a molecule at the site where the largest electronic density is found. A plethora of such Ar complexes with both aromatic and non-aromatic molecules ${ }^{34-41}$ have been studied with microwave spectroscopy. These systems can be exceptionally interesting giving rise to complex internal dynamics and given the symmetric charge distribution around Ar, they may assist with experimental benchmarking of quantum chemical calculations. Here, we explore the geometry of the PCA $\cdots \mathrm{Ar}$ complex and compare the non-covalent interaction to that of urea $\cdots \mathrm{Ar}$ and thiourea $\cdots \mathrm{Ar}$ (unpublished work by Mullaney et al.).

### 4.2 Experimental

The microwave spectra of PCA and PCA ${ }^{\prime}$ Ar were recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range. PCA was synthesized and provided by the group of Professor Jose M. Goicoechea at the University of Oxford and was used with no further purification. At ambient conditions, it is a white crystalline solid and, according to the Goicoechea group, decomposes at approximately $55-60{ }^{\circ} \mathrm{C}$. To avoid decomposition due to heating, the preferred method of gas phase generation of PCA is laser ablation. Given that PCA is a non-commercial compound, limited information is known around its toxicity and other health hazards. The main concern around it was its behavior under high pressures applied by the hydraulic bench press used for solid sample preparation as described in chapter 3 .

Conversations around safety and handling of primary phosphines were held with Dr Lee Higham (Newcastle University) prior to any experiments in order to assess and minimize risks. Initially, to avoid potential release of toxic $\mathrm{PH}_{3}, \mathrm{PCA}$ was transferred from a glass sealed ampule into a Young flask and kept under a gentle $\mathrm{N}_{2}$ flow. PCA powder was gently mixed with Zn powder (Sigma-Aldrich, ACS reagent, $\geq 99.9 \%$, granular) in $1: 1$ by mass ratio and deposited on a solid Teflon core ( 5 mm diameter) covered in PVA glue (no dilution with water). The above method of sample preparation generated the initial spectrum of PCA and allowed for assignment of a significant number of molecular transitions. However, the PCA and Zn mix fell off the Teflon core within 10-15 minutes of laser ablation.

An alternative approach to sample preparation was taken where several 5 mm diameter rods containing PCA and Zn in an approximate $1: 1$ by mass ratio were prepared into a dye mold and pressing with the hydraulic bench press. A total of approximately 900 mg of PCA was available in three batches of 300 mg in vacuum sealed ampules. A total of five test rods were prepared, each containing approximately $18,60,100,140$ and 300 mg of PCA mixed with an equal amount of Zn . Given that PCA was a brand-new substance for our lab, the purpose of iteratively increasing its amount in the solid rod was to minimize any risks that might arise during sample preparation. Pressing of solid substances is the preferred method of generating solid rods for laser ablation.

To further mitigate the risks that may be imposed during sample preparation, the hydraulic bench pressed was moved into a fume cupboard. The pressing chamber was purged with $\mathrm{N}_{2}$ prior, during and after sample pressing. The 5 mm dye mold was kept connected to a vacuum exhaust prior, during and for a few minutes after pressing to remove any $\mathrm{PH}_{3}$. It
was found that with this method, it is safe to apply $\sim 2$ tons of pressure to a mixture containing approximately 300 mg of PCA and 300 mg of Zn .

### 4.3 Density Functional Theory

Geometry optimizations of PCA and PCA $\cdots \mathrm{Ar}$ were performed. The starting geometry of PCA is according to the proposed structure. The B3LYP functional was used in conjunction with Dunning's aug-cc-pVTZ and D3BJ dispersion correction. The optimized geometries of PCA and PCA $\cdots \mathrm{Ar}$ are displayed in figure 4.3 and the calculated spectroscopic parameters are in table 4.1. Atomic coordinates for the complete calculated geometry are given in appendix A .


Figure 4.3. Calculated geometries of PCA and PCA $\cdots \mathrm{Ar}$ at the B3LYP(D3BJ)/aug-ccpVTZ level. The principal inertial axes are indicated as $a, b$, and $c$ and the total dipole moment components $\mu$ expand from positive to negative partial charge.

Table 4.1. Calculated spectroscopic parameters at the B3LYP(D3BJ)/aug-cc-pVTZ level.

|  | PCA | PCA $\cdots \mathrm{Ar}$ |
| :---: | :---: | :---: |
| $A_{e}(\mathrm{MHz})^{\mathrm{a}}$ | 10604 | 3405 |
| $B_{e}(\mathrm{MHz})$ | 4550 | 1280 |
| $C_{e}(\mathrm{MHz})$ | 3255 | 1119 |
| $\chi_{a a}(N)(\mathrm{MHz})^{\mathrm{b}}$ | 2.0561 | -3.429 |
| $\chi_{b b}(N)-\chi_{c c}(N)(\mathrm{MHz})$ | 6.3238 | -0.766 |
| $\chi_{a b}(\mathrm{MHz})$ | -0.1719 | 2.0228 |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|(D)^{\mathrm{c}}$ | $0.2,3.6,0.8$ | $0.9,0.1,3.7$ |

${ }^{\text {a }}$ Calculated rotational constants at equilibrium $A_{e}, B_{e}$ and $C_{e}$.
${ }^{\mathrm{b}}$ Calculated nuclear quadrupole coupling constants $\chi_{a a}(N)$ and $\chi_{b b}(N)-\chi_{c c}(N)$.
${ }^{c}$ Calculated dipole moments along the $a$-, $b$ - and $c$-inertial axes.

### 4.4 Spectral analysis

### 4.4.1 Phosphine Carboxamide (PCA)

The jet-cooled microwave spectrum of PCA was recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range over the course of 50k FID's under the conditions described in section 4.2 and is displayed in figure 4 . Several intense features are immediately observable alongside tens of less intense lines which are visible upon magnification of the spectrum. Examining the DFT calculated geometry (figure 3), PCA is a near-prolate asymmetric-top with the total dipole moment vector orienting from the carbonyl carbon to the direction of the amine group. The main dipole moment component is calculated to be closely aligned with the $b$ inertial axis of the molecule suggesting that the most intense lines will be ascribed to $R$ and $Q$-branch, b-type transitions of the patterns $J_{1, J^{\prime}-1}^{\prime} \rightarrow J_{0, J^{\prime \prime}}^{\prime \prime}$ and $J_{2, J-2} \rightarrow J_{1, J-1}$, respectively. These transitions were identified and exhibit hyperfine structure consistent with the presence of a N nucleus ( $I=1$ ) within PCA. The transitions were fit to Watson's A-reduced Hamiltonian ${ }^{42}$ in the $I^{r}$ representation as implemented in Western's Pgopher ${ }^{43}$. The overall Hamiltonian can be expressed as follows;

$$
\mathcal{H}=\mathcal{H}_{\mathrm{R}}-\frac{1}{6} \mathcal{Q}(\mathrm{~N}): \nabla \mathrm{E}(\mathrm{~N})
$$

where $\mathcal{H}_{\mathrm{R}}$ is the energy operator for a semi-rigid asymmetric top carrying information on the rotational and centrifugal distortion constants. The nuclear quadrupole moment dyadic is expressed as $\boldsymbol{Q}$ and $\nabla \mathbf{E}$ is the electric field gradient dyadic describing the coupling of the electric field gradient at the N nucleus with the applied electric field. The Hamiltonian has been discussed in detail chapter 2 . The initial fit of the most intense transitions allowed for detection of several more $b$-type, as well as some $a$ - and $c$-type transitions. A total of 99 hyperfine components were fit to yield the rotational constants $A_{0}, B_{0}$ and $C_{0}$, quartic centrifugal distortion constants $\Delta_{J}, \Delta_{J K}, d_{J}$ and $d_{K}$, and nuclear quadrupole coupling constants $\chi_{a a}(N)$ and $\chi_{b b}(N)-\chi_{c c}(N)$ of table 4.4. The experimentally determined constants are in good agreement with the calculated constants. The values and the magnitude of the obtained centrifugal distortion constants are comparable to those determined for urea and thiourea which are structural analogues of PCA. Observation of $c$-type transitions is consistent with the proposal that a rigidly pyramidal configuration is


Figure 4.4. The broadband microwave spectrum of PCA recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range over the course of 50k FID's under the conditions described in the experimental section and the apparatus described in chapter 3. Some intense transitions of PCA are labelled with the appropriate quantum numbers. The black asterisk highlights a detectable transition for the $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$.
adopted around the P atom leading the phosphine protons to point out of the $a b$-plane defined by the $\mathrm{O}, \mathrm{C}, \mathrm{N}$ and P atoms of PCA. $C$-type transitions were not reported in the spectra of urea and thiourea, consistent with the presence of a $\mathrm{C}_{2}$ axis aligned with the carbonyl and the proposal of syn and anti $-\mathrm{NH}_{2}$ groups resulting in cancelation of the relative dipole moment component. The barrier to inversion to planarity at the $-\mathrm{PH}_{2}$ site was calculated to be $112.7 \mathrm{~kJ} \mathrm{~mol}^{-1}$ which cannot be surmounted at the temperature of the supersonic expansion (approximate rotational temperature is 2 K ).

Transitions for $\mathrm{HC}_{3} \mathrm{~N}, \mathrm{CH}_{3} \mathrm{CN}$ and $\mathrm{CH}_{2}=\mathrm{CHCN}$ (vinyl cyanide) ${ }^{44-46}$ are also identified and these fragments are potentially side products of laser ablation of PCA in the solid target. Some transitions for the $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ are also readily identified with references to relevant
literature. ${ }^{47}$ The spectra were examined for the presence of other P-bearing species such as $\mathrm{HPCO}, \mathrm{HC}_{3} \mathrm{P}$ and $\mathrm{HC}_{5} \mathrm{P}$ which have previously been studied with rotational spectroscopy ${ }^{48-50}$ but none of them could confidently be identified. Species of astrochemical importance such as PN, CP, HCP, PO and CCP do not yield any transitions in the frequency range covered by the Newcastle University Spectrometer so no conclusions can be drawn on whether these may be formed

The most intense peaks of parent PCA were observed with a signal to noise $(\mathrm{S}: \mathrm{N})$ ratio of 480:1. This allowed for observation of the ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of PCA in their natural isotopic abundance, $1.1 \%$ and $0.4 \%$, respectively. Transitions of the ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of PCA were fitted with Watson's A-reduced Hamiltonian as described for the parent PCA. The centrifugal distortion constants were kept fixed at the values determined for the parent PCA and $\chi_{a a}(N)$ and $\chi_{b b}(N)-\chi_{c c}(N)$ were determined for ${ }^{13} \mathrm{C}$.


Figure 4.5. The $1_{11} \rightarrow 0_{00}$ transition of PCA parent isotopologue. Positive trace is a portion of the experimental spectrum and negative trace in red is the simulation produced with Pgopher.

Given that ${ }^{15} \mathrm{~N}$ is not a quadrupolar nucleus ( $I=1 / 2$ ), hyperfine structure was not observed for that isotopologue. Isotopic shifts in rotational constants will be evaluated in order to determine atomic coordinates of the C and N atoms within PCA and subsequently determine a partial structure of gas phase PCA in section 4.5.1.


Figure 4.6. The $3_{12} \rightarrow 3_{03}$ transition of PCA parent isotopologue. Positive trace is a portion of the experimental spectrum and negative trace in red is the simulation produced with Pgopher.


Figure 4.7. Expanded portion of the spectrum of PCA recorded over the course of 50k FID's. The $1_{11} \rightarrow 0_{00}$ transition of parent PCA and its ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues are simulated in red, green and purple, respectively. The transitions for ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ are shifted according to predicted isotopic shifts. The intensities are also consistent with their relative isotopic abundances. The lines around 13800 MHz (no simulation at the negative trace) remain unassigned and may be attributed to species formed during laser ablation and supersonic expansion or contamination.

Table 4.2. Experimentally determined spectroscopic parameters generated by fitting the transition frequencies of PCA to Watson's A-reduced Hamiltonian with Pgopher. The percentage deviation from the calculated values for some parameters are shown in the third column.

|  | PCA | $\%$ |
| :---: | :---: | :---: |
| $A_{0}(\mathrm{MHz})$ | $10581.3997(11)^{\mathrm{a}}$ | $0.21 \%$ |
| $B_{0}(\mathrm{MHz})$ | $4598.54643(50)$ | $-1.07 \%$ |
| $C_{0}(\mathrm{MHz})$ | $3275.00784(44)$ | $-0.62 \%$ |
| $\Delta_{J}(\mathrm{kHz})$ | $1.295(12)$ | - |
| $\Delta_{J K}(\mathrm{kHz})$ | $6.949(87)$ | - |
| $d_{J}(\mathrm{kHz})$ | $0.398(11)$ | - |
| $d_{K}(\mathrm{kHz})$ | $5.01(16)$ | - |
| $\chi_{a a}(N)(\mathrm{MHz})$ | $1.8974(39)$ | $7.72 \%$ |
| $\chi_{b b}(N)-\chi_{c c}(N)(\mathrm{MHz})$ | $5.8660(69)$ | $7.24 \%$ |
| $\chi_{a b}(\mathrm{MHz})$ | $[-0.1719]^{\mathrm{b}}$ | - |
| $\Delta_{0}\left(u \AA^{2}\right)^{\mathrm{c}}$ | $-3.34689(2)$ | - |
| $P_{c c}\left(u \AA^{2}\right)^{\mathrm{c}}$ | $1.67345(1)$ | - |
| $\kappa^{\mathrm{c}}$ | $-0.6377039(2)$ | - |
| $N^{\mathrm{d}}$ | 99 | - |
| $\sigma_{R M S}(\mathrm{kHz})^{\mathrm{e}}$ | 7.6 | - |

${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
${ }^{\mathrm{b}}$ The off-diagonal $\chi_{a b}$ quadrupole component in square brackets is fixed to its DFT calculated value for the optimized geometry of PCA.
${ }^{\mathrm{c}}$ Derived parameters. Inertial defect $\Delta_{0}=I_{c}-I_{b}-I_{c}$, planar moment $P_{c c}=-\frac{1}{2} \Delta_{0}$ and Ray's asymmetry parameter $\kappa=\frac{2 B_{0}-A_{0}-C_{0}}{A_{0}-B_{0}}$ derived by evaluating the ground state rotational constants determined for PCA.
${ }^{d}$ Number of total hyperfine components included in the fit.
${ }^{\mathrm{e}}$ Root mean square deviation of the fit.

Table 4.3. Experimentally determined spectroscopic parameters generated by fitting the transition frequencies of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of PCA to Watson's A-reduced Hamiltonian with Pgopher.

|  | PCA $^{13} \mathrm{C}$ | PCA $^{15} \mathrm{~N}$ |
| :---: | :---: | :---: |
| $A_{0}(\mathrm{MHz})$ | $10580.6658(15)^{\mathrm{a}}$ | $10332.8805(23)$ |
| $B_{0}(\mathrm{MHz})$ | $4586.87320(84)$ | $4535.9236(11)$ |
| $C_{0}(\mathrm{MHz})$ | $3269.02618(84)$ | $3219.3326(11)$ |
| $\Delta_{J}(\mathrm{kHz})$ | $[1.295(12)]^{\mathrm{b}}$ | $[1.295(12)]$ |
| $\Delta_{J K}(\mathrm{kHz})$ | $[6.949(87)]$ | $[6.949(87)]$ |
| $d_{J}(\mathrm{kHz})$ | $[0.398(11)]$ | $[0.398(11)]$ |
| $d_{K}(\mathrm{kHz})$ | $[5.01(16)]$ | $[5.01(16)]$ |
| $\chi_{a a}(N)(\mathrm{MHz})$ | $1.884(17)$ | - |
| $\chi_{b b}(N)-\chi_{c c}(N)(\mathrm{MHz})$ | $5.866(20)$ | - |
| $\chi_{a b}(\mathrm{MHz})$ | $\{-0.1719\}^{\mathrm{c}}$ | - |
| $N^{\mathrm{d}}$ | 18 | 6 |
| $\sigma_{R M S}(\mathrm{kHz})^{\mathrm{e}}$ | 8.4 | 6.7 |

${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
${ }^{b}$ Numbers in square brackets are fixed to the values determined for the parent PCA.
${ }^{c}$ The off-diagonal $\chi_{a b}$ quadrupole component in square brackets is fixed to its DFT calculated value for the optimized geometry of PCA.
${ }^{d}$ Number of total hyperfine components included in the fit.
${ }^{\mathrm{e}}$ Root mean square deviation of the fit.

### 4.4.2 The PCA $\cdots$ Ar complex

After assignment of the spectrum of PCA and its ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues and the fragmentation side-products, several lines remain unassigned at a $\mathrm{S}: \mathrm{N}$ ratio of approximately $20: 1$. The observed patterns for these lines suggest that their molecular carrier will be heavier than PCA. Additionally, considering their hyperfine structure, it is likely that the molecular carrier will contain PCA and some other lighter molecule. Given that the signal intensity for $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ is low whereas argon is abundant in the supersonic expansion, this chapter will proceed on the basis that a complex between PCA and Ar is responsible for the origin of these lines. Structural analysis and evalution of rotational constants and nuclear quadrupole coupling will support this assumption in the sections to follow. Typically, presence of $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ in a spectrum, with reference to previously measured transitions ${ }^{47}$, may result in the formation of complexes containing water (see chapter 7).

The calculated geometry of the PCA"Ar complex is a near prolate asymmetric top. Given the symmetric electron distribution of an Ar atom, it will typically interact with a molecule at the site where the most $\pi$-electron density is located. In PCA, Ar can coordinate above or below the plane defined by the $\mathrm{O}, \mathrm{C}, \mathrm{N}$ and P atoms. As a result, the inertial axes are positioned on the center of mass in the manner shown in figure 4.3. The $a$-axis is now going through the plane of PCA and is almost co-linear with the non-covalent bond between PCA and Ar. The strongest dipole moment component is expected to lie closely to the $c$ inertial axis and thus yield $c$-type transitions of the $J_{1, J^{\prime-1}}^{\prime} \rightarrow J_{0, J^{\prime \prime}}^{\prime \prime}$ series. Assignement of transitions was assisted by the rotational constants calculated at the B3LYP(D3BJ)/aug-cc-pVTZ level in table 4.1. Transitions were fitted to Watson's A reduced Hamiltonian as implemented in Pgopher and the form of the Hamiltonian was described earlier. Rotational constants $A_{0}, B_{0}$ and $C_{0}$, quartic centrifugal distortion constants $\Delta_{J}, \Delta_{J K}, \Delta_{K}, d_{J}$ and $d_{K}$, and nuclear quadrupole coupling constants $\chi_{a a}(N)$ and $\chi_{b b}(N)-\chi_{c c}(N)$ were determined and summarized in table 4.4. An expanded portion of the spectrum of PCA $\cdots \mathrm{Ar}$ is shown in figure 4.8. The calculated rotational constants deviate by approximately $3-5 \%$ from the experimentally determined ones. The magnitude and the values of the centrifugal distortion constants are relatively large compared to those for the PCA monomer, consistent with the presence of a non-covalent bond between PCA and Ar. They are also comparable to those determined for urea $\cdots \mathrm{Ar}$ and thiourea $\cdots \mathrm{Ar}$ (unpublished work by J. C. Mullaney et al.)


Figure 4.8. The $4_{13} \rightarrow 3_{03} c$-type transition of the PCA $\cdots \mathrm{Ar}$ complex. Upward trace (black) is the expanded portion of the experimental spectrum and downward trace (purple) is the simulated transition.

Table 4.4. Experimentally determined spectroscopic parameters generated by fitting the transition frequencies of PCA"Ar to Watson's A-reduced Hamiltonian with Pgopher.

|  | PCA $\cdots \mathrm{Ar}$ | $\%^{\mathrm{f}}$ |
| :---: | :---: | :---: |
| $A_{0}(\mathrm{MHz})$ | $3502.8520(10)^{\mathrm{a}}$ | $-2.87 \%$ |
| $B_{0}(\mathrm{MHz})$ | $1226.93915(45)$ | $4.15 \%$ |
| $C_{0}(\mathrm{MHz})$ | $1080.55182(70)$ | $3.44 \%$ |
| $\Delta_{J}(\mathrm{kHz})$ | $4.4561(48)$ | - |
| $\Delta_{J K}(\mathrm{kHz})$ | $29.283(26)$ | - |
| $\Delta_{K}(\mathrm{kHz})$ | $-1.228(98)$ | - |
| $d_{J}(\mathrm{kHz})$ | $0.6776(25)$ | - |
| $d_{K}(\mathrm{kHz})$ | $11.51(13)$ | - |
| $\chi_{a a}(N)(\mathrm{MHz})$ | $-3.3338(99)$ | $2.78 \%$ |
| $\chi_{b b}(N)-\chi_{c c}(N)(\mathrm{MHz})$ | $-0.396(16)$ | $69.54 \%$ |
| $\chi_{a b}(\mathrm{MHz})$ | $[2.0286]$ | - |
| $\Delta_{0}\left(u \AA^{2}\right)^{\mathrm{c}}$ | $-88.47207(34)$ | - |
| $P_{c c}\left(u \AA^{2}\right)^{\mathrm{c}}$ | $44.23604(17)$ | - |
| $\kappa^{\mathrm{c}}$ | $-0.8791336(7)$ | - |
| $N^{\mathrm{d}}$ | 76 | - |
| $\sigma_{R M S}{ }^{\mathrm{e}}$ | 11.6 | - |

${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
${ }^{\mathrm{b}}$ The off-diagonal $\chi_{a b}$ quadrupole component in square brackets is fixed to its DFT calculated value for the optimized geometry of PCA $\cdots$ Ar.
${ }^{\mathrm{c}}$ Derived parameters. Inertial defect $\Delta_{0}=I_{c}-I_{b}-I_{c}$, planar moment $P_{c c}=-\frac{1}{2} \Delta_{0}$ and Ray's asymmetry parameter $\kappa=\frac{2 B_{0}-A_{0}-C_{0}}{A_{0}-B_{0}}$ derived by evaluating the ground state rotational constants determined for PCA $\cdots \mathrm{Ar}$.
${ }^{d}$ Number of total hyperfine components included in the fit.
${ }^{e}$ Root mean square deviation of the fit.
${ }^{\mathrm{f}}$ Percentage deviations of experimental and calculated constants as $\frac{A_{\text {calc }}-A_{\text {exp }}}{A_{\text {exp }}} \times 100$

### 4.5 Structure Determination

### 4.5.1 Geometry Interpretation of PCA

The asymmetry of PCA is evaluated in terms of Ray's asymmetry parameter which was defined in chapter 2 by means of equation 2.30. A value of $-0.6377039(2)$ is obtained, consistent with the earlier assumption that PCA lies relatively close to the prolate limit. An insight into the gas phase structure of PCA can be provided by considering the planar (or second) moments. These can be calculated by means of equation 2.70 . The degree of planarity in PCA can be evaluated by $P_{c c}$, as well as by the inertial defect $\Delta_{0}=I_{c}-I_{b}-I_{c}$ (and therefore $P_{c c}=-\frac{1}{2} \Delta_{0}$ because of equation 2.73). For a planar molecule at equilibrium, the value of $\Delta_{0}$ will be zero (and subsequently, $P_{c c}=0$ ). Generally, in-plane vibrations at the zero-point will have a positive contribution to $\Delta_{0}$ whilst out-of-plane vibrations (and mass distribution) result in a negative $\Delta_{0}$ value.

For PCA, evaluating the rotational constants summarized table 4.3 by means of equation 2.72, we obtain a $P_{c c}$ value of $1.67345 \mathrm{u} \AA^{2}$. This value primarily arises by the $\mathrm{PH}_{2}$ protons, supporting the previously observed geometry where a rigidly pyramidal configuration is adopted at the P atom. The barrier to inversion at the $\mathrm{PH}_{2}$ site was calculated to be 112.7 $\mathrm{kJ} \mathrm{mol}{ }^{-1}\left(9421 \mathrm{~cm}^{-1}\right)$. Isotopic substitution with ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ does not significantly affect the value of $P_{c c}$ which is consistent with the proposal that the heavy atoms $\mathrm{O}, \mathrm{C}, \mathrm{N}$ and P lie close to the $a b$-inertial plane. The $P_{c c}$ values for the PCA analogues, urea and thiourea, are respectively $0.21285(8) \mathrm{u} \AA^{2}$ and $0.05749(6) \mathrm{u} \AA^{2}$ consistent with a planar geometry around the heavy atoms. In the solid state, the urea and thiourea monomers are planar at each $\mathrm{NH}_{2}$ group with overall $\mathrm{C}_{2 \mathrm{v}}$ symmetry. However, in the gas phase, the lowest energy conformers have a $\mathrm{C}_{2}$ symmetry with a pyramidal arrangement at each $\mathrm{NH}_{2}$ group with the protons pointing at opposite sides of the heavy atoms plane. An alternative low-energy conformer with $\mathrm{C}_{s}$ symmetry is also possible. The $\mathrm{NH}_{2}$ protons are pointing at the same side of the plane but with a low barrier to inversion at the $\mathrm{NH}_{2}$ resulting in the planar $\mathrm{C}_{2 v}$ conformer. Given the lack of data on deuterated isotopologues of PCA, it is not possible to establish the actual position of the $\mathrm{NH}_{2}$ and $\mathrm{PH}_{2}$ protons.

Table 4.5. Structural parameters derived by evaluating the ground state rotational constants PCA, urea and thiourea.

|  | PCA | Urea | Thiourea |
| :---: | :---: | :---: | :---: |
| $\kappa$ | $-0.63770354(28)^{\mathrm{a}}$ | $0.702936(4)$ | $-0.5280918(13)$ |
| $\Delta_{0}\left(\mathrm{u} \AA^{2}\right)$ | $-3.34685(4)$ | $-0.42571(16)$ | $-0.11499(11)$ |
| $P_{c c}\left(\mathrm{u} \AA^{2}\right)$ | $1.673427(21)$ | $0.21285(8)$ | $0.05749(6)$ |
| $c$-type ${ }^{\mathrm{b}}$ | yes | no | no |

${ }^{2}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\mathrm{b}}$ Absence or presence of c-type transitions in the spectra is indicated by yes or no, respectively.

Considering the ground state rotational constants given in tables 4.2 and 4.3 for PCA and its ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues, we can obtain structural information on the geometry of PCA. Upon ${ }^{13} \mathrm{C}$ isotopic substitution, the shift in rotational constants, particularly for $A_{0}$ is small, suggesting that C is positioned very close to the center of mass of PCA. The shifts in rotational constants caused by ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopic substitution allow for calculation of the atomic $r_{s}$ coordinates of the C and N atoms in PCA using Kraitchman's structure determination method ${ }^{51-53}$ described in section 2.10.2. The method is implemented in the program KRA which is available from the PROSPE website. ${ }^{54}$ The $r_{s}$ coordinates derived from the ground state rotational constants of the available isotopologues are shown in table 4.6 alongside their fractional uncertainties expressed as Costain errors ${ }^{55}$ in parentheses to account for the semi-rigid rotor behavior and vibration-rotation effects. The method can only generate the absolute values of the coordinates and for that reason the signs were implied by the DFT calculated geometry of PCA. Good agreement is observed between $r_{s}$ and DFT calculated $r_{e}$ coordinates. The C atom is positioned very close to the center of mass of PCA so the magnitudes of its atomic coordinates are small, consistent with the small shift in rotational constants caused by ${ }^{13} \mathrm{C}$ isotopic substitution. The $c$-coordinate of the N atom is calculated to be an imaginary number, suggesting that the N atom essentially lies in the $a b$-inertial plane, and it was therefore set to zero.

Table 4.6. Calculated ( $r_{e}$ ) and experimentally determined $\left(r_{s}, r_{0}\right)$ atomic coordinates of the C and N atoms of PCA.

|  |  | $\mathrm{C}(2)$ |  |  | $\mathrm{N}(3)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a / \AA$ | $b / \AA$ | $c / \AA$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| $r_{e}$ | -0.5503 | -0.0837 | 0.0207 | -1.2301 | 1.0934 | -0.0082 |
| $r_{s}$ | $-0.5311(28)$ | $-0.055(27)$ | $0.018(84)$ | $-1.2306(12)$ | $1.0941(14)$ | $0.0^{*}$ |
| $r_{0}$ | $-0.57078(95)$ | $-0.0667(16)$ | $-0.0131(9)$ | $-1.238(52)$ | $1.086(27)$ | $-0.0348(2)$ |

Despite the limited amount of isotopic data, it is possible to partially evaluate the gas phase structure of PCA by making some structural assumptions. These assumptions are based on the $r_{s}, r_{e}$ and X-ray structure of $\mathrm{PCA}^{2}$ as well as on the gas phase structure of urea at the zero-point. ${ }^{22-24}$ The partial effective $r_{0}$ structure of PCA is determined using Kisiel's STRFIT ${ }^{56}$ available from the PROSPE website. The $r_{0}$ method, as described in section 2.10.3, proceeds through least-squares fitting of the experimental moments of inertia of the various isotopologues of PCA to a structure. The input $z$-matrix was constructed assuming the $r_{s}$ bond length of the $(N-C)$ bond of PCA which is evaluated to be $1.346(23) \AA$. Given the structural similarities between PCA and urea, the carbonyl bond length was set to that determined for the gas phase urea at the zero-point. Likewise, the values for the $\angle(O-C-N)$ angle and the $r(N-H)$ bonds were set to the values for urea. The $\angle(O-C-N-P)$ dihedral angles was set to its DFT value $174.5^{\circ}$. The respective dihedral in urea and thiourea is $180^{\circ}$. Some subtle deviation from planarity is expected for PCA given the asymmetry and the low charge delocalization over the $P$ center increasing the $\mathrm{sp}^{3}$ character at the phosphine site. Finally, the $r(P-H)$ bond lengths were based on their DFT values rather than X-ray values; shortening of these bonds is expected due to crystal packing effects.

The $z$-matrix described above allows for determination of the $r_{0}(N-C)$, $\angle(N-C-P)$ and $\angle(N-C-O)$ structural parameters of PCA. These are summarized in Appendix A, table A3 alongside some $r_{s}, r_{e}$ and X-ray data for PCA and some geometrical parameters for urea and thiourea determined with microwave spectroscopy. The experimentally determined $r_{0}$ parameters are consistent with the $r_{e}$ geometry of PCA as well as with the X-ray structure. As it is expected, the X-ray value for the $r(N-C)$ bond is somewhat smaller than its $r_{s}$ and $r_{0}$ value, possibly due to crystal and lattice effects.

The structures of urea and thiourea have been established by microwave spectroscopy ${ }^{22-26}$ and X-ray crystallography. ${ }^{27}$ Both molecules exhibit $\mathrm{C}_{2}$ symmetry in the gas phase with the two $\mathrm{NH}_{2}$ groups adopting a pyramidal configuration at the N atom at the zero-point. The main $\mathrm{C}_{2}$ axis goes down the $\mathrm{C}=\mathrm{O}$ bond resulting in the two N atoms being equivalent within each molecule. However, isotopic experiments with D indicated that the H atoms are not equivalent with one other, ruling out a possible planar structure and supporting the argument that a syn- and anti- configuration is adopted by each $\mathrm{NH}_{2}$ group. Isotopic experiments with D-enriched PCA are pending and these will confirm the orientation of the protons in the $\mathrm{NH}_{2}$ and $\mathrm{PH}_{2}$ sites

### 4.5.2 Geometry Interpretation of $P C A \cdots A r$

To interpret the geometry of the PCA $\cdots$ Ar complex, it will be assumed that the structure of the PCA subunit remains unchanged upon complexation. This is a common approach that has been adopted for similar complexes reported in previous works cited here. ${ }^{57-59}$ The polar coordinates, $R_{c m}, \vartheta$ and $\varphi$, depicted in figure 4.9 are employed and these are referenced with respect to the principal axes of PCA which will be denoted as $\alpha, \beta$ and $\gamma$, corresponding to the $a, b$ and $c$-axes, respectively. $R_{c m}, \vartheta$ and $\varphi$ are defined as the distance between the centers of mass of PCA and Ar, the angle between a vector along $R_{c m}$ and the $\alpha$-axis of PCA and the angle between the $\beta$-axis of PCA and the projection of $R_{c m}$ on the $\beta \gamma$-plane of PCA, respectively. The program RGDFIT ${ }^{59}$ available from the PROSPE website ${ }^{54}$ was used to calculate the coordinates of the Ar atom within the frame of reference by fitting the rotational constants of PCA and PCA $\cdots \mathrm{Ar}$ to a set of moments of inertia. The program calculates the position of the Ar atom by adding a point mass to the PCA monomer so that the coordinates of the added atom can be reproduced by the moments of inertia resulting from the rotational constants of PCA and PCA $\cdots$ Ar. The limitation of the program is that rotation-vibration effects are not accounted for so for this reason, Costain errors will be calculated based on the final geometry.

Given that inertial tensors are invariant over a $180^{\circ}$ rotation about a principal inertial axis, ${ }^{53}$ four possible sets of solutions are generated all of which can reproduce the experimentally determined zero-point rotational constants of PCA and PCA $\cdots$ Ar. This traces back to the Kraitchman method where only the relative magnitudes of each coordinate are generated. The four possible solutions are collected in table 4.8. Two of them can be ruled out by simple geometry considerations. The two sides of the heavy atoms plane of PCA are not equivalent due to the rigidly pyramidal arrangement at the $\mathrm{PH}_{2}$ site. Solutions 3 and 4 require the Ar atoms to coordinate at the side of the plane where the $\mathrm{PH}_{2}$ protons are directed. Considering the possible distance between Ar and the $\mathrm{PH}_{2}$ protons, this distance is approximately $2 \AA$ which would account for a relatively short van der Waals interaction. Solution 2 can also be ruled out as it requires the Ar atom to coordinate almost directly above the P atom. As it will be discussed later, the electronic density over the P site is low so based on trends observed in other Ar-containing complexes, this position is not favorable for Ar coordination. This is consistent with the proposal made by Goichoechea et al. that the $\mathrm{PH}_{2}$ site exhibits more $\mathrm{sp}^{3}$ character and lower delocalization of electronic charges, ${ }^{2}$


Figure 4.9. Calculated geometries of PCA and PCA ${ }^{\prime}$ Ar. Definition of the $\alpha-, \beta$-, and $\gamma$ axes of PCA (panel i) and definition of the polar coordinates $R_{C M}, \vartheta$ and $\varphi$ in PCA $\cdots \mathrm{Ar}$ with respect to the axes of PCA (panel ii).

Table 4.7. The possible solutions for the position of the Ar atom with respect to the inertial axes framework of PCA.

|  | $R_{c m}(\AA)$ | $\vartheta\left({ }^{\circ}\right)$ | $\varphi\left({ }^{\circ}\right)$ |
| :---: | :---: | :---: | :---: |
| $R_{c m}, \vartheta, \varphi$ | 3.67813 | 17.493 | 36.973 |
| $R_{c m}, \vartheta, \pi+\varphi$ | 3.67813 | 17.493 | 216.973 |
| $R_{c m}, \pi-\vartheta, 2 \pi-\varphi$ | 3.67813 | 162.507 | 323.027 |
| $R_{c m}, \pi-\vartheta, \pi-\varphi$ | 3.67813 | 162.507 | 143.027 |
|  | $\alpha(\AA)$ | $\beta(\AA)$ | $\gamma(\AA)$ |
| Ar | 0.88328 | 0.66494 | 3.50804 |
|  | -0.88328 | -0.66494 | 3.50804 |
|  | 0.88328 | -0.66494 | -3.50804 |
|  | -0.88328 | 0.66494 | -3.50804 |

The position of Ar with respect to the inertial axes of the PCA monomer may also be rationalized by considering the fitted nuclear quadrupole coupling constants of table 4.2 and 4.4 and the diagonalized components in terms of principal nuclear axes. These are discussed in detail in section 4.6 and are summarized in table 4.9. In order to derive structural information from the coupling of the monomer and that of the Ar complex, we need to assume that changes in the electric field gradient at the N nucleus caused by complexation are negligible. Examining the fitted nuclear quadrupole coupling constants of PCA and PCA $\cdots \mathrm{Ar}$, the $\alpha$-axis of PCA is almost co-linear with the $c$-axis of PCA $\cdots \mathrm{Ar}$, $\chi_{a a}^{P C A}(N)=1.8974 \cong \chi_{c c}^{A r}(N)=1.8649 \mathrm{MHz}$. From the values of the diagonalized components, it follows that the $x$-nuclear axis on N is almost colinear with the $\alpha$-axis of PCA and the $c$-axis of PCA $\cdots$ Ar. From the rotation matrix, the angle between the $z$-axis (on the N ) and the $a$-axis of PCA $\cdots \mathrm{Ar}$ is $21(4)^{\circ}$. The complementary angle between the vector along $R_{\mathrm{CM}}$ and the $\alpha$-axis is within the uncertainty of that value. This is in support of the proposal that the Ar coordinates above or below the plane of PCA. However, given that the rotation matrix depends on the calculated values of $\chi_{a b}(N)$ for PCA and PCA $\cdots \mathrm{Ar}$, this approach will eventually be inconclusive regarding the exact position of Ar since there is no experimental $\chi_{a b}(N)$ values available.


Figure 4.10. The $R_{C M}$ length in the PCA $\cdots \mathrm{Ar}$, urea $\cdots \mathrm{Ar}$ and thiourea $\cdots \mathrm{Ar}$ indicated as a dashed line.

The $R_{C M}$ length in PCA $\cdots \mathrm{Ar}$, urea $\cdots \mathrm{Ar}$ and thiourea $\cdots \mathrm{Ar}$ are displayed in figure 4.10. The differences in that coordinate between the three complexes is mainly due to the position of the center of mass in each of PCA, urea and thiourea. This distance is significantly longer in PCA *Ar due to the center of mass of PCA being between the C and P atoms. Given the high symmetry of urea and thiourea, the center of mass is placed very close to the C in each molecule.

### 4.6 Nuclear Quadrupole Coupling Constants of PCA and PCA $\cdots \mathrm{Ar}$

The ${ }^{14} \mathrm{~N}$ nucleus, with nuclear spin $I=1$, in PCA is responsible for the hyperfine splitting of the rotational transitions in both PCA and PCA $\cdots$ Ar. Upon rotation, the electric field gradient (efg) at the ${ }^{14} \mathrm{~N}$ nucleus couples the efg of the oscillating electric field resulting in the said hyperfine splitting. The nuclear quadrupole coupling constants $\chi_{a a}(N)$ and $\left[\chi_{b b}(N)-\chi_{c c}(N)\right]$ determined for PCA and PCA $\cdots \mathrm{Ar}$ can be used as a probe to detect changes that may occur in the electronic environment around the ${ }^{14} \mathrm{~N}$ nuclei. These changes may be induced by, for example, Van der Waals forces between PCA and Ar or as it has been shown by Pinacho and co-workers in the case of ethylcarbamate, ${ }^{60}$ as a result of progressive hydration and hydrogen bonding cooperativity. Complete determination of all nuclear quadrupole coupling components, both diagonal and off-diagonal components, can provide an insight into the electric field gradient at a given quadrupolar nucleus. However, often, only the diagonal components can be determined experimentally as the off-diagonal ones are usually small and thus only poorly determined.

The experimentally measured nuclear quadrupole constants of PCA and PCA AA are shown in tables 4.2 and 4.4, respectively. These are referenced in the principal inertial axes system, therefore direct comparisons of the quadrupole coupling of the ${ }^{14} \mathrm{~N}$ nucleus in PCA and PCA $\cdots \mathrm{Ar}$ cannot be made since the inertial axes are differently oriented. A common reference system needs to be implemented where a set of mutually perpendicular axes (principal nuclear axes), $x, y, z$, are placed on the ${ }^{14} \mathrm{~N}$ nucleus. The principal nuclear quadrupole coupling components $\chi_{a a}(N), \chi_{b b}(N)$ and $\chi_{c c}(N)$ are diagonalized such that the $\chi_{x x}(N), \chi_{y y}(N)$ and $\chi_{z z}(N)$ components are generated along the $\mathrm{x}, \mathrm{y}, \mathrm{z}$ axes, respectively, using the program QDIAG, available from the PROSPE website. ${ }^{54}$ This method has been discussed in detail in chapter 2 and the relative equations used for the transformations are 2.59 and 2.60.

Planarity around the heavy atoms $\mathrm{O}, \mathrm{C}, \mathrm{N}$ and P of PCA is established by the structure determination methods discussed earlier and previous X-ray crystallography data. In PCA, the out-of-plane $c$-axis is parallel to one of the principal nuclear axes on the ${ }^{14} \mathrm{~N}$ atom whilst the $a$ - and $b$-inertial axes are rotated by an angle of $\phi$. However, in PCA $\cdots \mathrm{Ar}$, the inertial axes are rearranged as shown in figure 4.1 meaning that the $a$-axis goes through the plane of PCA within the complex. It follows that the $z$-nuclear axis on N is parallel to the $c$-axis of PCA and to the $a$-axis of PCA $\cdots \mathrm{Ar}$.

The nuclear quadrupole coupling constants in terms of principal nuclear axes $\chi_{x x}(N)$, $\chi_{y y}(N)$ and $\chi_{z z}(N)$ for PCA and PCA $\cdots \mathrm{Ar}$ are shown in table 4.9. Assuming that changes to the efg on the N nucleus of PCA caused by attachment of Ar are negligible, the results reliably indicate that the assignment of PCA and PCA $\cdots \mathrm{Ar}$ as molecular carriers is correct. Negligible changes to the efg of quadrupolar nuclei upon Ar attachment have also been discussed for other complexes. ${ }^{59,61}$ The main differences between the diagonalized nuclear quadrupole coupling components in PCA and PCA $\cdots \mathrm{Ar}$ mainly arise from low lying vibrations consistent with the weak van der Waals forces.

Table 4.8. The diagonalized nuclear quadrupole coupling constants $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ for PCA, urea and thiourea and their van der Waals complexes with Ar.

|  | PCA | Urea | Thiourea |
| :---: | :---: | :---: | :---: |
| $\chi_{x x}(N)$ | $1.764(42)^{\mathrm{a}}$ | $1.715(54)$ | $1.635(99)$ |
| $\chi_{y y}(N)$ | $2.118(42)$ | $2.174(54)$ | $2.433(99)$ |
| $\chi_{z z}(N)$ | $-3.8817(40)$ | $-4.0889(29)$ | $-4.0684(28)$ |
| $\eta^{\mathrm{b}}$ | $0.092(15)$ | $0.112(19)$ | $0.196(34)$ |
|  | PCA $\cdots \mathrm{Ar}$ | Urea $\cdots \mathrm{Ar}$ | Thiourea $\cdots \mathrm{Ar}$ |
| $\chi_{x x}(N)$ | $1.8649(94)$ | $1.676(54)$ | $1.843(84)$ |
| $\chi_{y y}(N)$ | $2.21(33)$ | $2.149(86)$ | $1.922(20)$ |
| $\chi_{z z}(N)$ | $-4.08(33)$ | $-3.825(95)$ | $-3.776(78)$ |
| $\eta$ | $0.085(81)$ | $0.124(27)$ | $0.021(23)$ |

${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\mathrm{b}}$ The asymmetry parameter calculated as $\eta=\frac{\chi_{x x}(N)-\chi_{y y}(N)}{\chi_{z z}(N)}$ implies the nuclear axes orientation ${ }^{53}$.

The diagonalized nuclear quadrupole coupling constants are further explored for urea and thiourea and their Ar complex analogues (urea ${ }^{*} \mathrm{Ar}$ and thiourea $\cdots \mathrm{Ar}$ unpublished work by Mullaney et al.). The calculated values of $\chi_{a b}$ for PCA, urea and thiourea are -0.1719 , 0.2227 and -0.3971 MHz , respectively, at the B3LYP(D3BJ)/aug-cc-pVTZ level. For their Ar complexes these values are $2.0286,-0.6235$ and -0.9176 MHz . The values of the $\chi_{x x}$ and $\chi_{y y}$ components for PCA, urea and thiourea do not vary significantly across the series and the level of precision is relatively high, particularly for the out-of plane $\chi_{z z}$ component. For PCA and urea, the values of the $\chi_{x x}$ and $\chi_{y y}$ components are within the standard
deviation of one another, highlighting the similarities in the electronic environment around the N nucleus between the two molecules. These similarities may arise from the chemical composition of the amide site in both PCA and urea as well as the established planarity around the $\mathrm{N}, \mathrm{C}$ and O atoms. For thiourea, an increase is observed for the $\chi_{y y}$ component which may be consistent with the presence of 3p-orbitals in the valence shell of S resulting in a better charge delocalization. However, the values of $\chi_{x x}$ and $\chi_{y y}$ are less accurately determined when compared to PCA and urea so no further conclusions can be drawn by looking at $\chi_{x x}$ and $\chi_{y y}$ alone. Of course, the values of the $\chi_{x x}$ and $\chi_{y y}$ for PCA, urea and thiourea are somewhat dependent on the chosen value of $\chi_{a b}$ upon which the rotation is reliant. However, the value of $\chi_{a b}$ is consistently calculated to be small across the three molecules and a standard deviation of $25 \%$ of its calculated value was assumed when the axes rotations were performed.

The value of the $\chi_{z z}$ component of PCA is determined to be significantly smaller than that of urea and thiourea. This may be explained by electron density being donated by the $2 \mathrm{p}_{z}$ orbital on N into the $\sigma^{*}$ orbitals of the $\mathrm{P}-\mathrm{H}$ bonds on the phosphine group due to partial orbital overlap. To support this argument, an orbital population analysis was performed for the 2 p orbitals on N for PCA, urea and thiourea following the Townes-Dailey model ${ }^{62}$ and the equations used are given and explained in other works, ${ }^{63,64}$ where $2 p_{z}$ is the lone pair orbital. The model also allows for calculation of the ionic character of the $\mathrm{N}-\mathrm{H}$ and $\mathrm{N}-\mathrm{C}$ bonds, labelled as $i_{\sigma}(\mathrm{NH})$ and $i_{\sigma}(N C)$, respectively, as well as the covalent character of the $\mathrm{N}-\mathrm{C}$ bond, $\pi_{c}(N C)$. The results of the analysis are summarized in table 4.10. The equations were used as reported in previous studies.

Table 4.9. Some parameters calculated for PCA, urea and thiourea by consideration of their nuclear quadrupole coupling constants.

|  | PCA | Urea | Thiourea |
| :---: | :---: | :---: | :---: |
| $\chi_{z z}(\mathrm{MHz})$ | $-3.8817(40)$ | $-4.0889(29)$ | $-4.0684(28)$ |
| $\delta$ | $2.36(40) \%$ | $3.06(51) \%$ | $5.32(93) \%$ |
| $i_{\sigma}(N H)$ | 0.32 | 0.32 | 0.38 |
| $i_{\sigma}(N C)$ | 0.29 | 0.28 | 0.30 |
| $\pi_{c}(N C)$ | 0.22 | 0.19 | 0.13 |
| $2 p_{x}$ | 1.31 | 1.30 | 1.34 |
| $2 p_{y}$ | 1.32 | 1.32 | 1.38 |
| $2 p_{z}$ | 1.78 | 1.81 | 1.87 |

The lowest lone pair orbital population is observed for PCA supporting the assumption that electron density may be donated into the $\sigma$-orbitals of the $\mathrm{P}-\mathrm{H}$ bonds on the phosphine group. The highest covalent character for the $\mathrm{N}-\mathrm{C}$ bond, $\pi_{c}(N C)$, is also observed for PCA suggesting that the electron density concentrated at the amide site is high. The comparably highly populated orbitals on the N of thiourea are consistent the with the increase in the values of at $\chi_{x x}$ and $\chi_{y y}$ as discussed earlier.

The extent of electron transfer from the N atom toward the $\pi$-system may be evaluated by means of Goldstein's parameter, ${ }^{46,53,65} \delta$, following the expression;

$$
\delta=\frac{2}{3} \frac{\chi_{x x}-\chi_{y y}}{e Q q_{n 10}}
$$

where $e Q q_{n 10}$ is the contribution of a single $p$-electron to the total nuclear quadrupole coupling. It has been determined that $e Q q_{n 10}$ for the N nucleus it is equal to -10 MHz . The Goldstein parameter may be rationalized as the difference in electron density between the $p_{x}$ and $p_{y}$ orbitals on $N$. The $N$ lone pair in the $p_{z}$ orbital is delocalized over the $\pi$ system of PCA as seen in the resonance canonicals in figure 4.1. It follows that $\delta$ is defined as the electron density deficit in the $p_{y}$ orbital with respect to a fully occupied by a lone pair orbital. The value of $\delta$ may give an insight into the double bond character of the $\mathrm{N}-$ C bond and subsequently into the degree of electron delocalization across PCA.

For PCA, the value of $\delta$ is calculated to be $2.36 \%$ which is the smallest value across the PCA, urea, thiourea series suggesting that the N-C bond in PCA has low double bond character. The electron delocalization across PCA is relatively low with the phosphine group having minimal contribution to the resonance canonicals as it was also discussed by Goichoechea et al ${ }^{2}$. The electron density is shared across the O and N of the amide group. This argument is in harmony with the high degree of covalent character $\pi_{c}(N C)$ in PCA when compared to urea and thiourea. The highest double bond character is observed for the $\mathrm{N}-\mathrm{C}$ bond in thiourea with that of urea being the intermediate case.

It must be noted that these analyses may only provide an initial insight into the orbital populations and the bond properties in PCA, urea and thiourea. These results will be dependent, to a certain extent, on the selected off-diagonal terms $\chi_{a b}$ calculated for each molecule. This determines the rotation of the quadrupole axes which in turn will determine the values of $\chi_{x x}$ and $\chi_{y y}$. As DFT methods mainly consider charges in the valance shell of an atom and the value of $\chi_{a b}$ arises from unequal distribution of nuclear charges, the accuracy of this value will be affected. Even though an uncertainty of $25 \%$ was given to $\chi_{a b}$, it is likely that its value will be somewhat dependant on the level of theory used to calculate it. It should also be noted that these analyses were primarily developed for halogen-bearing molecules, i.e. $\mathrm{H}-\mathrm{Cl}, \mathrm{H}-\mathrm{Br}$ etc, for which the off-diagonal $\chi_{a b}$ components vanish and therefore the analysis depends on purely experimental data. ${ }^{53}$

### 4.7 Conclusions

The microwave spectra of three isotopologues of PCA (parent, ${ }^{13} \mathrm{C},{ }^{15} \mathrm{~N}$ ) and the van der Waals complex PCA"Ar were recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range with the CPFTMW spectrometer at Newcastle University. Rotational constants, centrifugal distortion constants and nuclear quadrupole coupling constants are determined experimentally for both PCA and PCA $\cdots$ Ar. Rotational constants were evaluated to generate the $r_{s}$ atomic coordinates of C and N for gas phase PCA and to determine the position of Ar with respect to the PCA skeleton. It is remarkable that a steeply pyramidal configuration is adopted at the $-\mathrm{PH}_{2}$ site with the two H atoms pointing out of the plane defined by the heavy atoms of PCA. The electronic charge distribution around the N nucleus in PCA was explored and compared to that of its structural analogues, urea and thiourea. A concentration of electronic charge around the amide site of PCA is observed with the phosphine site having minimal contributions to delocalization of charges. The N-C bond in PCA was shown to have low double bond character when compared to urea and thiourea. PCA is one of a few examples of primary air-stable phosphines and its stability may arise from a large HOMO-LUMO gap and mixing of $\pi$-orbitals.

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## Chapter 5. Bifunctional Hydrogen Bonding of Imidazole with Water Explored by Rotational Spectroscopy and DFT Calculations

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### 5.1 Introduction

Imidazole $\left(\mathrm{C}_{3} \mathrm{H}_{4} \mathrm{~N}_{2}\right)$, figure 5.1, is a five-membered heteroaromatic ring that is an important building block of fundamental biomolecules such as the nucleobase adenine and the amino-acid histidine. Histidine's imidazole subunit can interact with hemoglobin ${ }^{1}$ via either the pyrrolic (N1) or pyridinic (N3) nitrogen, acting as either a proton donor or acceptor, respectively. Anti-cancer agents such as cis-Pt drugs bind to DNA's guanine or adenine while stabilized by secondary interactions via the pyridinic nitrogen of the imidazole subunit ${ }^{2}$. Due to the presence of a basic nitrogen atom (N3) within the ring, imidazole, alongside thiazole and oxazole, also belongs to the class of alkaloids. ${ }^{3}$ This may partially account for their diverse biochemical activity, meaning they can be found in antibiotics, ${ }^{4}$ antifungal, ${ }^{5}$ antithyroid ${ }^{6}$ and anti-HIV ${ }^{7}$ medication among others. Rationalizing the various possible binding sites of imidazoles is crucial to our understanding of their properties and biochemical activity.


Figure 5.1. The imidazole monomer. Heavy atoms are numbered following the convention for aromatic molecules.

The structure of crystalline imidazole has been established through neutron ${ }^{8}$ and X-ray diffraction. ${ }^{9,10}$ Alternating linkages between the pyrrolic and the pyridinic nitrogen of individual imidazole molecules were observed in the crystal structure. The gas phase structure of isolated imidazole was determined by microwave spectroscopy. ${ }^{11,12}$ Microwave spectroscopy also allows for structure determination of gas phase complexes that contain imidazole interacting with some other smaller molecule. ${ }^{13,14}$ The imidazole dimer was studied by Mullaney et al. ${ }^{13}$ The two imidazole monomers interact through an intermolecular hydrogen bond between the pyrrolic nitrogen of one monomer and the pyridinic nitrogen of the other monomer. The observed molecular geometry and the presence of an intermolecular hydrogen bond is consistent with that described for crystalline solid imidazole.

The stepwise hydration of various aromatic molecules in the gas phase has been studied extensively with microwave spectroscopy. Monohydrates of N -containing aromatic molecules including pyrrole ${ }^{15}\left(\mathrm{C}_{4} \mathrm{H}_{5} \mathrm{~N}\right)$, thiazole ${ }^{16}\left(\mathrm{C}_{3} \mathrm{H}_{3} \mathrm{OS}\right)$, isoxazole ${ }^{17}\left(\mathrm{C}_{3} \mathrm{H}_{3} \mathrm{NO}\right)$, indole ${ }^{18}\left(\mathrm{C}_{8} \mathrm{H}_{7} \mathrm{~N}\right)$, pyridine ${ }^{19}\left(\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}\right)$, pyrazine ${ }^{20}\left(\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{~N}_{2}\right)$, pyrimidine ${ }^{21}\left(\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{~N}_{2}\right)$, pyridazine ${ }^{22}\left(\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{~N}_{2}\right)$, and triazine ${ }^{23}\left(\mathrm{C}_{3} \mathrm{H}_{3} \mathrm{~N}_{3}\right)$ have been studied with microwave spectroscopy giving an insight into the first step of their solvation in water. Unlike in pyrazole $\left(\mathrm{C}_{3} \mathrm{H}_{4} \mathrm{~N}_{2}\right)$, the pyridinic and the pyrrolic nitrogen of imidazole are spatially arranged so that they do not immediately affect each other. It follows that an individual water molecule may interact with either the pyridinic or the pyrrolic nitrogen site but not with both simultaneously. The binding site where the first water molecule interacts, and the intermolecular interaction type are determined by the chemical environment of the aromatic molecule. For example, a hydrogen bond is formed between the H on the pyrrolic nitrogen and the O of water in the $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole and the $\mathrm{H}_{2} \mathrm{O} \cdots$ indole complexes ${ }^{15,18}$ with the pyrrolic nitrogen being the proton donor. In each of pyridine ${ }^{19}$, pyrazine ${ }^{20}$, pyrimidine, ${ }^{21}$ pyridazine ${ }^{22}$ and triazine, ${ }^{23}$ a hydrogen bond is observed with the pyridinic nitrogen accepting a proton from an individual water molecule.

Imidazole and water are both ubiquitous in biology and biochemistry so rationalizing the preferred binding modes between the two is crucial. IR spectroscopy in He-nanodroplets suggest a $1: 1$ ratio between the binding modes in the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid isomers. ${ }^{24}$ A more recent study with IR spectroscopy ${ }^{25}$ probing complexes formed between imidazole and water within a free jet expansion failed to detect the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid isomer. The
observation was interpreted as a result of that isomer not being kinetically stable in a free jet and effectively relaxing into imid $\cdots \mathrm{H}_{2} \mathrm{O}$. Further gas phase IR experiments ${ }^{26}$ probing benzimidazole and water identified two isomers, benzim $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ benzim, where water is a proton donor and a proton acceptor, respectively. In this chapter, the simultaneous isolation of two isomers of a complex between imidazole and water, imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$, probed in a free jet expansion is reported for the first time. The microwave spectra of both isomers in the $7.0-18.5 \mathrm{GHz}$ frequency range are reported and analyzed. Isotopologues containing D and ${ }^{18} \mathrm{O}$ are also considered in order to confirm the assignment of molecular carriers and to determine structural parameters regarding the $\mathrm{H}_{2} \mathrm{O}$ subunit in both isomers. Large amplitude motions associated with the $\mathrm{H}_{2} \mathrm{O}$ subunit in the $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ isomer are modelled and discussed.

### 5.2 Experimental Details

This is the first experiment that was performed after the implementation of the fundamental 1064 nm harmonic in the laser ablation source. Imidazole was used as a test molecule to examine if laser ablation was possible with that wavelength. Imidazole (Sigma-Aldrich, $\geq 99.5 \%$ ) mixed with silver iodide (ACROS Organics ${ }^{\mathrm{TM}}$, $99 \%$ ) in a $1: 1$ by mass ratio and pressed into a 13 mm cylindrical rod. Argon gas was kept at a constant pressure of 7 bar. No deliberate actions were taken to introduce water into the experiment; water may be present within the gas lines, the solid sample itself or the adsorbed on the walls of the vacuum chamber or pulse valve.

### 5.3 Quantum Chemical Calculations

Geometry optimizations of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ were performed. The optimized geometries are shown in figure 5.2. The B3LYP functional in conjunction with dispersion correction D3BJ, was initially used alongside Dunning's aug-cc-pVTZ basis set. Geometry optimizations were subsequently performed with the $\omega$ B97X-D functional and quadrupole- $\zeta$ aug-cc-pVQZ basis set with tight convergence criteria. Grimme's D2 dispersion correction is included in the functional. Calculated values of rotational constants and dipole moment components are presented in Table 5.1. The complete set of DFT-calculated atomic coordinates is presented in Table A3 and A4 of appendix A. For $\mathrm{H}_{2} \mathrm{O}$ imid, one-dimensional potential energy surfaces (PES) were scanned to describe large amplitude motions for two internal coordinates. These respectively probe the torsional and wagging motions of $\mathrm{H}_{2} \mathrm{O}$ with respect to the imidazole ring and are presented in Section 6.5. These PES calculations were kindly performed by Dr Daniel J. Cole at Newcastle University. Calculated rotational constants ( $A_{\mathrm{e}}, B_{\mathrm{e}}$ and $C_{\mathrm{e}}$ ), dipole moment components $\left(\left|\mu_{a}\right|,\left|\mu_{b}\right|\right.$ and $\left.\left|\mu_{c}\right|\right)$ and relative energies of the two complexes are summarised in Table 5.1. Structural parameters calculated at the $\omega$ B97X-D/aug-cc-pVQZ level will be used in the comparisons to follow due to its strong performance across a wide range of benchmark tests.


Figure 5.2. Equilibrium geometries of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid calculated at the $\omega$ B97XD/aug-cc-pVQZ level of theory. The electric dipole moment components are propagated from positive to negative charge.

Table 5.1. Spectroscopic parameters calculated for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid at the B3LYP(D3BJ)/aug-cc-pVTZ and $\omega$ B97X-D/aug-cc-pVQZ levels of theory.

| B3LYP(D3BJ)/aug-cc-pVTZ |  |  |
| :---: | :---: | :---: |
|  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |
| $A_{\mathrm{e}}(\mathrm{MHz})^{\text {a }}$ | 9522.83 | 9524.35 |
| $B_{\mathrm{e}}(\mathrm{MHz})^{\text {a }}$ | 1788.40 | 1677.16 |
| $C_{e}(\mathrm{MHz})^{\text {a }}$ | 1512.19 | 1435.68 |
| $\chi_{a \boldsymbol{a}}(\mathbf{N 1})(\mathrm{MHz})$ | 1.1920 | 0.8152 |
| $\chi_{\boldsymbol{b} \boldsymbol{b}}-\chi_{c c}(\mathbf{N 1})(\mathrm{MHz})$ | 3.8580 | 3.4511 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | -0.0939 | -0.0755 |
| $\chi_{a a}(\mathrm{~N} 3)(\mathrm{MHz})$ | -3.7828 | -2.2672 |
| $\chi_{\boldsymbol{b} \boldsymbol{b}}-\chi_{\boldsymbol{c} \boldsymbol{c}}(\mathbf{N} 3)(\mathrm{MHz})$ | -0.4900 | -2.6799 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | 1.1492 | -2.9629 |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | \| $5.3\|,\|1\|,\|1.2\|$ | $\|6.4\|,\|1.2\|,\|0\|$ |
| $\Delta E\left(\mathrm{~cm}^{-1}, \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | 0, 0 | 263, 3.15 |
| $\omega$ B97X-D/aug-cc-pVQZ |  |  |
|  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |
| $A_{\mathrm{e}}(\mathrm{MHz})^{\text {a }}$ | 9608 | 9570.97 |
| $B_{\mathrm{e}}(\mathrm{MHz})^{\text {a }}$ | 1778.24 | 1695.37 |
| $C_{e}(\mathrm{MHz})^{\text {a }}$ | 1507.59 | 1449.96 |
| $\chi_{a a}(\mathbf{N 1})(\mathrm{MHz})$ | 1.1446 | 0.8388 |
| $\chi_{\boldsymbol{b} \boldsymbol{b}}-\chi_{\boldsymbol{c} \boldsymbol{c}}(N 1)(\mathrm{MHz})$ | 3.7922 | 3.2956 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | 0.1337 | 0.1110 |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | -3.8686 | -2.0030 |
| $\chi_{\boldsymbol{b} \boldsymbol{b}}-\chi_{c c}(\mathrm{~N} 3)(\mathrm{MHz})$ | -0.7299 | -3.3344 |
| $\chi_{a b}(\mathbf{N 3})(\mathrm{MHz})$ | -1.1681 | 3.0535 |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | \| $5.3\|,\|1.1\|,\|1.2\|$ | $\|6.2\|,\|0.6\|,\|0\|$ |
| $\Delta E\left(\mathrm{~cm}^{-1}, \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | 0, 0 | 606, 7.25 |

${ }^{\mathrm{a}}$ Calculated equilibrium $A_{\mathrm{e}}, B_{\mathrm{e}}$ and $C_{\mathrm{e}}$ rotational constants..

### 5.4 Spectral Analysis

The initial geometries used for the DFT calculations were generated based on the geometry of previously studied complexes like pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole. A detailed conformational analysis for the two complexes imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid was not necessary given the well-established geometry of both imidazole and $\mathrm{H}_{2} \mathrm{O}$ and the presence of chemically distinct coordination sites available for H -bonding on imidazole. The optimized equilibrium geometry of both imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid appears to be a near-prolate asymmetric top where all the heavy atoms lie in the plane defined by the imidazole ring. The total electric dipole moment component is calculated to be almost colinear with the $a$-inertial axis in both isomers.

The jet-cooled rotational spectrum recorded under the experimental conditions described earlier is displayed in figure 5.3. The most intense transitions are readily identified based on previous studies and are ascribed to the imidazole monomer. ${ }^{11,12}$ Transitions of (imid) ${ }_{2}$, imid $\cdots \mathrm{Ar}, \mathrm{AgI}$ and $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ were also assigned with reference to previous studies. ${ }^{13,14,27,28}$ Products of fragmentation of imidazole and subsequent gas phase chemical reactions are also present in the spectra. These include $\mathrm{HC}_{3} \mathrm{~N}, \mathrm{HC}_{5} \mathrm{~N}, \mathrm{HC}_{7} \mathrm{~N}, \mathrm{CH}_{3} \mathrm{CN}, \mathrm{ICN}, \mathrm{IC}_{3} \mathrm{~N}$, $\mathrm{C}_{4} \mathrm{H}_{3} \mathrm{~N}$ (methylcyanoacetylene), $\mathrm{C}_{4} \mathrm{H}_{3} \mathrm{~N}$ (cyanoallene) and $\mathrm{C}_{3} \mathrm{H}_{2} \mathrm{~N}$ (vinyl cyanide). ${ }^{29-37}$ The observation of fragmentation products is unsurprising and has previously been reported and described. ${ }^{13,38,39}$


Figure 5.3. Broadband microwave spectrum between 7.0 and 18.5 GHz recorded over 240 k FID's under the experimental conditions described in Section 5.2.

Several transitions remain unassigned and these are consistent with expectations for the spectra of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ and imid $\cdots \mathrm{H}_{2} \mathrm{O}$. The transitions exhibit hyperfine splitting confirming the presence of two distinct N nuclei within the molecular carriers of these spectra. These transitions were fit to Watson's S-reduced Hamiltonian ${ }^{40,41}$ in the $\mathrm{I}^{\mathrm{r}}$ representation for a semi-rigid asymmetric top as implemented in Pgopher ${ }^{42}$;

$$
H=H_{\mathrm{R}}-\frac{1}{6} \mathbf{Q}(\mathrm{~N} 1): \nabla \mathbf{E}(\mathrm{N} 1)-\frac{1}{6} \mathbf{Q}(\mathrm{~N} 3): \nabla \mathbf{E}(\mathrm{N} 3)
$$

Here, two different nuclear quadrupole moment dyadics $\mathbf{Q}$ and electric field gradient dyadics $\nabla \mathbf{E}$ to account for the presence of two distinct quadrupolar nuclei. The rotational constants $A_{0}, B_{0}$ and $C_{0}$, centrifugal distortion constants $D_{J}$ and $D_{J K}$ for the parent isotopologue of both imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid are included in the $H_{\mathrm{R}}$ and their values are summarized in table 5.2. The diagonalized components of the nuclear quadrupole coupling tensor $\chi_{a a}$ and $\left(\chi_{b b}-\chi_{c c}\right)$ for both N1 and N3 in each isomer are also summarized in table 5.9. When fitting the transitions for imid $\cdots \mathrm{H}_{2}{ }^{18} \mathrm{O}$, imid $\cdots \mathrm{H}_{\mathrm{b}} \mathrm{OD}_{\mathrm{nb}}$ and the $0^{+}$state of HDO $\cdots$ imid it was necessary to include additional centrifugal distortion term, $d_{1}$, to generate a satisfactory fit. The detailed form of the Hamiltonian was given in chapter 2.

Rotational transitions were initially assigned to the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ complex based on the consistence between DFT calculated and fitted rotational constants. The spectroscopic parameters determined through fitting several $a$-type transitions with $\Delta J=1$ and $\Delta K=0$ with Watson's S-reduced Hamiltonian are summarized in table 5.2. Previous studies of pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$, isoxazole $\cdots \mathrm{H}_{2} \mathrm{O}$ and pyrazine $\cdots \mathrm{H}_{2} \mathrm{O}$ complexes, among others, report the presence of two different tunneling states arising from large amplitude motions associated with the $\mathrm{H}_{2} \mathrm{O}$ subunit within the complexes. Such splittings were not observed for the imid$\cdot \cdot \mathrm{H}_{2} \mathrm{O}$ complex, being consistent with the results ${ }^{21,43}$ reported for 2-fluoropyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ and pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$. Observation of only $a$ - and $b$-type transitions and absence of $c$-type transitions for all observed isotopologues of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is consistent with the planarity of the complex.

Further examination of the recorded spectra led to independent assignment of two different sub-states, denoted as $0^{-}$and $0^{+}$, of the spectrum with the molecular carrier being the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid complex. The rotational constants and centrifugal distortion constants
determined for these sub-states are also displayed in table 5.2. These parameters do not vary significantly between the two sub-states suggesting subtle rearrangement of masses. A statistical weight ratio of approximately $3: 1$ is observed for most transitions assigned for the $0^{-}$and $0^{+}$sub-states, respectively. A set of $0^{-}$and $0^{+}$sub-states with $3: 1$ statistical weight was reported in the spectra for $\mathrm{H}_{2} \mathrm{O} \cdots$ indole and $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole and thus supporting the initial assignment that the molecular carrier of these spectra is the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid complex.

Table 5.2. Experimentally determined spectroscopic parameters fitted to Watson's Sreduced Hamiltonian for each of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid.

|  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ |  |
| :---: | :---: | :---: | :---: |
|  |  | $0^{-}$ | $0^{+}$ |
| $\boldsymbol{A}_{\mathbf{0}}$ (MHz) | 9502.79(43) ${ }^{\text {a }}$ | 9436.97(54) | 9520.99(26) |
| $\boldsymbol{B}_{0}(\mathrm{MHz})$ | 1826.3929(13) | 1663.0101(11) | 1662.91298(73) |
| $\boldsymbol{C}_{\mathbf{0}}(\mathrm{MHz})$ | 1531.9303(10) | 1421.1251(13) | 1420.74502(72) |
| $\boldsymbol{D}_{\boldsymbol{J}}(\mathrm{kHz})$ | 1.269(20) | 0.487(18) | 0.2349(96) |
| $\boldsymbol{D}_{\boldsymbol{J K}}(\mathrm{kHz})$ | 63.03(21) | 49.77(25) | 59.20(15) |
| $\chi_{a \boldsymbol{a}}(\mathrm{~N} 1)(\mathrm{MHz})$ | 1.143(19) | 0.923(75) | 0.916(45) |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 1)-\chi_{c \boldsymbol{c}}(\mathrm{~N} 1)\right](\mathrm{MHz})$ | 3.712(56) | 3.80(46) | 4.07(23) |
| $\chi_{\boldsymbol{a} a}(\mathrm{~N} 3)(\mathrm{MHz})$ | -2.889(21) | -1.932(71) | -1.859(44) |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 3)-\chi_{\boldsymbol{c} \boldsymbol{c}}(\mathrm{N} 3)\right](\mathrm{MHz})$ | -1.07(11) | -2.66(44) | -2.47(25) |
| $\kappa^{\text {b }}$ | -0.926115(4) | -0.939648(4) | -0.9402073(31) |
| $\boldsymbol{P}_{\boldsymbol{a b}}\left(\mathrm{u} \AA^{2}\right)$ | 276.7053(12) | 302.9729(15) | 303.2656(13) |
| $\boldsymbol{P}_{\boldsymbol{b} \boldsymbol{b}}\left(\mathrm{u} \AA^{2}\right)$ | 53.1839(12) | 52.6377(15) | 52.4401(13) |
| $\boldsymbol{P}_{\boldsymbol{c} \boldsymbol{c}}\left(\mathrm{u} \AA^{2}\right)$ | -0.0029(12) | 0.9141(15) | 0.6391(13) |
| $\Delta_{0}\left(\mathrm{u} \AA^{2}\right)$ | 0.0059(24) | -1.8282(31) | -1.2783(15) |
| $\boldsymbol{N}{ }^{\text {c }}$ | 60 | 37 | 24 |
| $\boldsymbol{\sigma}_{\boldsymbol{R} M \boldsymbol{S}}(\mathrm{kHz})^{\mathrm{c}}$ | 13.7 | 13.6 | 5.8 |

${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\mathrm{b}}$ Ray's asymmetry parameter is calculated as $\kappa=\frac{2 B_{0}-A_{0}-C_{0}}{A_{0}-C_{0}}$
${ }^{\mathrm{c}} N$ and $\sigma_{\mathrm{RMS}}$ are respectively the number of measured transitions and the standard deviation of the fit.

Pickett's SPFIT/SPCAT suite of programs ${ }^{44}$ was used in an attempt to produce a simultaneous, global fit of transitions of both $0^{-}$and $0^{+}$sub-states. The Hamiltonian was selected to include one or more Coriolis coupling constants to account for the large amplitude motion causing the splitting. Several procedures were employed, one of which
was to fix the quadrupole coupling to the values shown in table 5.2 , fit the rotational constants and some selected Coriolis terms, followed by adjustment of these terms prior to repeating the fit. It was not possible to produce a unique solution and constrain the fit due to large amplitude motions associated with the $\mathrm{H}_{2} \mathrm{O}$ subunit. As it will be discussed later, a wagging and a torsional motion were identified, and both appear to contribute a significant amount to the large amplitude motions within this complex. The Hamiltonians implemented in SPFIT/SPCAT are unable to account for these motions and subsequently did not allow determination of Coriolis coupling terms. Significant differences are also observed for $D_{J}$ and $D_{J K}$ between the $0^{-}$and $0^{+}$sub-states consistent with the proposal of complex internal dynamics and large amplitude motions.

Isotopic experiments were performed with isotopic water HDO and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ to confirm the geometry and subsequently the assignment of molecular carriers to the identified spectra. A total of four isotopologues of the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ (imid $\cdots \mathrm{H}_{2} \mathrm{O}$, imid $\cdots \mathrm{DOH}$, imid $\cdots \mathrm{H}^{18} \mathrm{OH}$ and imid $\cdots \mathrm{HOD})$ and three isotopologues of the $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}\left(\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}, \mathrm{H}_{2}{ }^{18} \mathrm{O} \cdots \mathrm{imid}\right.$ and HDO $\cdots$ imid) were assigned and their determined spectroscopic parameters are summarized table 5.3 and 5.4. The changes in the rotational constants of the D and ${ }^{18} \mathrm{O}$ isotopologues are consistent with expected isotopic shifts. The $5_{05} \rightarrow 4_{04}$ transitions of the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid and $\mathrm{HDO} \cdots$ imid isotopologues is shown in figure 5.4. It is immediately apparent that the splitting between the $0^{-}$and $0^{+}$sub-states decreases upon deuteration supporting the proposal of large amplitude motions associated with the protons of the $\mathrm{H}_{2} \mathrm{O}$ subunit. Observation of the spectrum of only one HDO $\cdots$ imid isotopologue suggests that the two protons are equivalent within the complex and isotopic substitution of either one of them creates an equal change in the moment of inertia of that complex. Only one substate of the $\mathrm{H}_{2}{ }^{18} \mathrm{O} \cdots$ imid isotopologue was observed with significantly low intensity and that was assigned to the $0^{-}$sub-state. The experimentally determined rotational constants for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid alongside their percentage deviations from their corresponding calculated values are shown in table 5.5.
$\mathrm{H}_{2} \mathrm{O}$-Imid


HDO Imid


## Frequency (MHz)

Figure 5.4. (a, left panel) Expanded section of the $5_{05} \rightarrow 4_{04}$ transition of $\mathrm{H}_{2} \mathrm{O} \cdots$ imid and (b, right panel) the same transition of the HDO $\cdots$ imid isotopologue. Rotational transitions are split into $0^{-}$and $0^{+}$states. The splitting between the $0^{-}$and $0^{+}$states decreases upon deuteration implying an internal motion of the water molecule.

Table 5.3. Spectroscopic parameters determined for isotopologues of imid $\cdots \mathrm{H}_{2} \mathrm{O}$.

|  | imid $\cdots \mathrm{D}_{\mathrm{b}} \mathrm{OH}_{\mathrm{nb}}$ | imid $\cdots \mathrm{H}_{2}{ }^{18} \mathrm{O}$ | imid $\cdots \mathrm{H}_{\mathrm{b}} \mathrm{OD}_{\mathrm{nb}}$ |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{A}_{\mathbf{0}}(\mathrm{MHz})$ | 9481.55(46) ${ }^{\text {a }}$ | 9499.20(45) | 9422.95(34) |
| $\boldsymbol{B}_{0}(\mathrm{MHz})$ | 1793.3641(15) | 1707.6406(23) | 1742.7498(29) |
| $\boldsymbol{C}_{\mathbf{0}}(\mathrm{MHz})$ | 1508.1838(10) | 1447.3811(20) | 1472.3732(15) |
| $\boldsymbol{D}_{\boldsymbol{J}}(\mathrm{kHz})$ | 1.320(26) | 1.427(22) | 1.088(21) |
| $\boldsymbol{D}_{\boldsymbol{J} \boldsymbol{K}}(\mathrm{kHz})$ | 60.97(25) | 57.83(12) | 57.29(19) |
| $\boldsymbol{d}_{\mathbf{1}}(\mathrm{kHz})$ | - | -0.276(23) | -0.139(24) |
| $\chi_{a j}(\mathrm{~N} 1)(\mathrm{MHz})$ | [1.143(19)] | [1.143(19)] | [1.143(19)] |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 1)-\chi_{c \boldsymbol{c}}(\mathrm{~N} 1)\right]$ (MHz) | [3.712(56)] | [3.712(56)] | [3.712(56)] |
| $\chi_{a \boldsymbol{a}}(\mathrm{~N} 3)(\mathrm{MHz})$ | [-2.889(21)] | [-2.889(21)] | [-2.889(21)] |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 3)-\chi_{c \boldsymbol{c}}(\mathrm{~N} 3)\right](\mathrm{MHz})$ | [-1.07(11)] | -1.07(11)] | [-1.07(11)] |
| $\kappa$ | -0.92847(6) | -0.93535(6) | -0.93199(5) |
| $\boldsymbol{P}_{\boldsymbol{a b}}\left(\mathrm{u} \AA^{2}\right)$ | 281.797(21) | 295.959(22) | 289.799(16) |
| $\boldsymbol{P}_{\boldsymbol{b} \boldsymbol{b}}\left(\mathrm{u} \AA^{2}\right)$ | $53.294(21)$ | 53.209(22) | 53.442(16) |
| $\boldsymbol{P}_{\boldsymbol{c c}}\left(\mathrm{u} \AA^{2}\right)$ | 0.008(21) | -0.007(22) | 0.191(16) |
| $\Delta_{0}\left(\mathrm{u} \AA^{2}\right)$ | -0.015(42) | 0.014(44) | -0.381(32) |
| $\boldsymbol{N}^{\text {b }}$ | 19 | 41 | 25 |
| $\boldsymbol{\sigma}_{\text {RMS }}(\mathrm{kHz})^{\text {b }}$ | 9.2 | 13.3 | 10.3 |

[^1]Table 5.4. Spectroscopic parameters determined for isotopologues of $\mathrm{H}_{2} \mathrm{O}$ imid.

|  | HDO...imid |  | $\mathrm{H}_{2}{ }^{18} \mathrm{O} \cdots$ imid |
| :---: | :---: | :---: | :---: |
|  | 0 | $0^{+}$ |  |
| $\boldsymbol{A}_{\mathbf{0}}(\mathrm{MHz})$ | 9384.56(67) ${ }^{\text {a }}$ | 9430.41(50) | 9437.55(38) |
| $\boldsymbol{B}_{0}(\mathrm{MHz})$ | 1586.6402(18) | 1586.7041(26) | 1557.5747(16) |
| $\boldsymbol{C}_{\mathbf{0}}(\mathrm{MHz})$ | 1366.8028(15) | 1366.6089(20) | 1343.3755(18) |
| $\boldsymbol{D}_{\boldsymbol{J}}(\mathrm{kHz})$ | 0.633(23) | 1.138(17) | 0.711(23) |
| $\boldsymbol{D}_{\boldsymbol{J}}(\mathrm{kHz})$ | 37.59(35) | 34.62(29) | [49.77] |
| $\boldsymbol{d}_{\mathbf{1}}(\mathrm{kHz})$ | - | -0.613(18) | - |
| $\chi_{a \boldsymbol{a}}(\mathrm{~N} 1)$ (MHz) | [0.923] | [0.916] | [0.923] |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 1)-\chi_{c \boldsymbol{c}}(\mathrm{~N} 1)\right](\mathrm{MHz})$ | [3.80] | [4.07] | [3.80] |
| $\chi_{\boldsymbol{a} \boldsymbol{a}}(\mathrm{N} 3)(\mathrm{MHz})$ | [-1.932] | [-1.859] | [-1.932] |
| $\left[\chi_{\boldsymbol{b} \boldsymbol{b}}(\mathrm{N} 3)-\chi_{c \boldsymbol{c}}(\mathrm{~N} 3)\right](\mathrm{MHz})$ | [-2.66] | [-2.47] | [-2.66] |
| $\boldsymbol{\kappa}$ | -0.945163(4) | -0.9454129(35) | -0.9470732(26) |
| $P_{\text {ab }}\left(\mathrm{u} \AA^{2}\right)$ | 317.2037(18) | 317.3548(15) | $323.5506(11)$ |
| $\boldsymbol{P}_{\boldsymbol{b} \boldsymbol{b}}\left(\mathrm{u} \AA^{2}\right)$ | 52.5403(18) | 52.4416(15) | 52.6414(11) |
| $P_{c c}\left(\mathrm{u} \AA^{2}\right)$ | $1.3104(18)$ | $1.1465(15)$ | 0.9071(11) |
| $\Delta_{0}\left(\mathrm{u} \AA^{2}\right)$ | -2.621(4) | -2.2930(29) | -1.8143(22) |
| $N^{\text {b }}$ | 15 | 15 | 11 |
| $\boldsymbol{\sigma}_{\boldsymbol{R} \boldsymbol{M} \boldsymbol{S}}(\mathrm{kHz})^{\mathrm{b}}$ | 12.7 | 8.4 | 10.6 |

${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figure. ${ }^{\mathrm{b}} N$ and $\sigma_{\text {RMS }}$ are respectively the number of hyperfine transitions and the standard deviation of the fit.

Table 5.5. Calculated rotational constants of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid and their percentage deviations from the experimentally determined ground state rotational constants.

|  | B3LYP(D3BJ)/aug-cc-pVTZ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ |  | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |  |  |
|  |  |  |  | 0 | $0^{+}$ |
| $\boldsymbol{A}_{\boldsymbol{e}}(\mathrm{MHz})$ | 9522.83 | 0.21\% ${ }^{\text {a }}$ | 9516.67 | 0.84\% | -0.05\% |
| $\boldsymbol{B}_{\boldsymbol{e}}(\mathrm{MHz})$ | 1788.40 | -2.12\% | 1677.86 | 0.89\% | 0.89\% |
| $\boldsymbol{C}_{\boldsymbol{e}}(\mathrm{MHz})$ | 1512.19 | -1.31\% | 1436.02 | 1.04\% | 1.6\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | \|5.3|, |1.0|, |1.2| |  | $\|6.4\|,\|1.2\|,\|0\|$ |  |  |
| $\Delta E\left(\mathrm{~cm}^{-1}, \mathrm{~kJ} \mathrm{~mol}^{-1}\right)^{\mathrm{b}}$ | 0 |  | 263, 3.15 |  |  |
|  | $\omega$-B97XD/aug-cc-pVQZ |  |  |  |  |
|  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ |  | $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ |  |  |
|  |  |  |  | 0 | $0^{+}$ |
| $\boldsymbol{A}_{\boldsymbol{e}}(\mathrm{MHz})$ | 9608 | 1.10\% | 9570.98 | 1.4\% | 0.52\% |
| $\boldsymbol{B}_{\boldsymbol{e}}(\mathrm{MHz})$ | 1778.24 | -2.71\% | 1695.37 | 1.91\% | 1.92\% |
| $\boldsymbol{C}_{\boldsymbol{e}}(\mathrm{MHz})$ | 1507.59 | -1.62\% | 1449.96 | 1.99\% | 2.01\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | $\|5.3\|,\|1.1\|,\|1.2\|$ |  | $\|6.2\|,\|0.6\|,\|0\|$ |  |  |
| $\Delta E\left(\mathrm{~cm}^{-1}, \mathrm{~kJ} \mathrm{~mol}^{-1}\right)^{\mathrm{b}}$ | 0 |  | 606, 7.3 |  |  |

${ }^{\text {a }}$ Percentage deviation calculated as $\frac{A_{\text {calc }}-A_{\text {exp }}}{A_{\text {exp }}} \times 100$ where the comparison is between results for the parent isotopologues of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$.
${ }^{\mathrm{b}}$ Imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is calculated to be the global minimum by both methods. The energy of the $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ isomer is given relative to the energy of imid $\cdots \mathrm{H}_{2} \mathrm{O}$.

### 5.5 Geometry Interpretation

In chapter 4, it was explained how an initial insight into the geometry of a complex may be obtained by evaluating the experimentally determined rotational constants to derive the values of the planar moments $P_{a a}, P_{b b}$ and $P_{c c}$ and the inertial defect $\Delta_{0}$. It has been explained that a $\Delta_{0}$ value of zero is obtained for a planar molecule at equilibrium. However, at the zero-point, $\Delta_{0}$ is expected to be contaminated by low lying vibrations. Typically, in-plane vibrations have a positive contribution to $\Delta_{0}$ whereas out-of-plane vibrations (and mass) result in negative contributions. The value of $\Delta_{0}=0.0059(24) \mathrm{u} \AA^{2}$ for the parent isotopologue of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is very close to zero suggesting that this isomer is effectively planar at the zero-point. Looking at the values of $\Delta_{0}$ and $P_{c c}$, these vary significantly between the two sub-states of the parent isotopologue of the $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ isomer. The value of $\Delta_{0}=-1.8282 \mathrm{u} \AA^{2}$ for the $0^{-}$sub-state is close to that expected for a molecule with two rigid hydroxylic protons. However, for the $0^{+}$sub-state, a value of $-1.2783 \mathrm{u} \AA^{2}$ is calculated suggesting that the protons of the $\mathrm{H}_{2} \mathrm{O}$ subunit are brought closer to the $a b$-plane of $\mathrm{H}_{2} \mathrm{O} \cdots$ imid. This observation is consistent with large amplitude motions occurring at the $\mathrm{H}_{2} \mathrm{O}$ subunit, particularly involving the two protons, at the timescale of molecular rotation.

Atomic coordinates of the O and H atoms in the $\mathrm{H}_{2} \mathrm{O}$ subunit in both imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O}$. .-imid are determined by evaluating the shifts in rotational constants caused by isotopic substitution. The Kraitchman method was used to generate the substitution $r_{s}$ coordinates and these are collectively shown in table 5.6 and compared to the calculated $r_{e}$ coordinates. The method can only produce the magnitudes of the relative coordinates and for that reason the signs were those determined for the equilibrium geometry at the $\omega \mathrm{B} 97 \mathrm{X}$ -D/aug-cc-pVQZ level. Costain's errors are displayed in parentheses alongside the relative coordinates. In imid $\cdots \mathrm{H}_{2} \mathrm{O}$, the $c$-axis coordinate of the O atom is returned as an imaginary number, so it was set to zero. This is consistent with the proposed planarity of that complex indicated by the small value of the calculated $\Delta_{0}$. The $c$-axis coordinate of the bonding H participating in the intermolecular bond is only $|c|=0.104(17) \AA$. Even though the position of H atoms is generally not well determined with the $r_{s}$ method due to elongation effects ${ }^{45}$, the results are in good agreement with the calculated coordinates. The nonbonding hydrogen, not participating in the intermolecular bond, is calculated to lie $0.4521(38) \AA$ above the $a b$-plane. The DFT calculated $c$-axis coordinate is $0.6829 \AA$. These
numbers may be connected to the planar geometry implied by the small value of $\Delta_{0}$ of the parent imid $\cdots \mathrm{H}_{2} \mathrm{O}$ by invoking a rapid motion of the non-bonding hydrogen of water rapidly switching between equivalent positions above and below the ab-plane of the complex. A similar interpretation was given to the discrepancies between the calculated and experimental geometry of the 2-flyoropyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ complex ${ }^{43}$. For the imid.• $\cdot \mathrm{H}_{\mathrm{b}} \mathrm{OD}_{\mathrm{nb}}$ isotopologue, $\Delta_{0}$ is calculated to be $-0.381(32) \mathrm{u} \AA^{2}$, significantly larger than that of the parent isotopologue and subsequently implying that the non-bonding deuterium atom is lying out of the $a b$-plane, both at equilibrium and at the zero-point. This may be rationalized by considering that the $r_{s}$ method does not account for the elongation of the O-D bond when compared to O-H and therefore neglects differences in vibrational energy of the isotopologues caused by that bond elongation.

It was discussed earlier that two distinct sub-states are observed in the spectrum of the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid isomer indicating that the $\mathrm{H}_{2} \mathrm{O}$ moiety undergoes one or more large amplitude motions. Rigid rotor assumptions about the structure are not effective. However, it is possible to calculate the $r_{s}$ coordinate of the O atom. Considering the geometry of $\mathrm{H}_{2} \mathrm{O} \cdot$. -imid depicted in figure 5.1, the O atom of the water subunit is involved in the intermolecular hydrogen bond acting as a proton donor. This will, to a certain extent, constrain the position of the O atom. Only one state of the $\mathrm{H}_{2}{ }^{18} \mathrm{O} \cdots \mathrm{imid}$ was observed and that was assigned to the $0^{-}$state which gives the most consistent results between the $r_{e}, r_{s}$ and $r_{0}$ coordinates. It is also in agreement with the intensities of the $0^{-}$and $0^{+}$states of $\mathrm{H}_{2} \mathrm{O} \cdots$ imid and $\mathrm{HDO} \cdots$ imid where the $0^{-}$state was statistically more intense than the $0^{+}$ state in both isotopologues. It is expected that $0^{-}$of $\mathrm{H}^{18} \mathrm{O} \cdots \mathrm{imid}$ is three times more intense than $0^{+}$. The $c$-axis coordinate was calculated to be an imaginary number suggesting the intermolecular hydrogen bond is in the $a b$-plane of the imidazole ring. The magnitude of the calculated $b$-coordinate is small indicating that O lies very close to the $a$-axis of the complex. These observations confirm the calculated geometry of the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid isomer and stand along the earlier assumption that the O atom is relatively constrained.

Table 5.6. Experimentally-determined $\left(r_{0}, r_{s}\right)$ and DFT-calculated $\left(r_{e}\right)$ atomic coordinates for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid.

|  |  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $a / \AA$ | $b / \AA$ | c / A |
| $\mathrm{H}_{\mathrm{b}}$ | $r_{e}$ (calc.) | 2.253901 | 0.141020 | -0.054538 |
|  | $r_{s}$ (exp.) | $2.25889(77)^{\text {a }}$ | $0.3339(53)$ | -0.104(17) |
|  | $r_{0}$ (exp.) | 2.230(5) | 0.187(25) | $0^{\text {b }}$ |
| O | $r_{e}$ (calc.) | 3.203723 | -0.048453 | -0.124829 |
|  | $r_{s}$ (exp.) | $3.13460(50)$ | -0.115(14) | $0^{\text {c }}$ |
|  | $r_{0}$ (exp.) | 3.151(2) | -0.0770(6) | $0^{\text {b }}$ |
| $\mathrm{H}_{\mathrm{nb}}$ | $r_{e}$ (calc.) | 3.584692 | 0.289172 | 0.682930 |
|  | $r_{s}(\text { exp.) }$ | $3.62122(47)$ | 0.5218 (33) | 0.4521 (38) |
|  | $r_{0}(\exp .)^{\text {a }}$ | 3.636(21) | 0.749(14) | $0^{\text {b }}$ |
|  |  | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |  |  |
|  | A | $a$ | $b$ | c |
| O | $r_{e}$ (calc.) | -3.15362 | 0.077918 | 0.00007 |
|  | $r_{s}$ (exp.) | -3.24141(48) | 0.042(38) | $0^{\text {c }}$ |
|  | $r_{0}$ (exp.) | -3.2518(37) | 0.0258(58) | 0 |

${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\mathrm{b}}$ The $r_{0}$ coordinates are those determined under one of two alternative model geometries which fit the rotational constants with high accuracy (see text for details). The coordinates shown are those obtained when the $r_{0}$ parameters are as shown in Table 4.
${ }^{\mathrm{c}}$ Imaginary result is obtained so $r_{\mathrm{s}}$ coordinate is assumed equal to zero.

Given that some structural information has been obtained through the $r_{s}$ coordinates of the two isomers, it is possible to determine some $r_{0}$ parameters, provided some reasonable assumptions are made. Numbering of heavy atoms in imidazole follows that of figure 5.1 and 5.2 whilst the hydrogens are labelled based on the heavy atom their attached. The atom connectivity for the initial $z$-matrix is established through the $r_{s}$ geometry determined above. Planarity of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is established based on the value of $\Delta_{0}$. The $r_{0}$ parameters were determined using STRFIT. The $r_{0}$ parameters that were determined for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ are $r\left(H_{b} \cdots N 3\right)$ that described the length of the intermolecular hydrogen bond and the angles $\angle\left(H_{b} \cdots N 3-C 2\right)$ and $\angle\left(O-H_{b} \cdots N 3\right)$ which describe the position and orientation of the water molecule with respect to the ab-plane of imidazole. It is also assumed that the geometry of imidazole and water is unaffected by complexation and for
that reason the individual $r_{0}$ geometries of the two subunits were used. As in the case of pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$, there are four possible orientations for the water subunit whilst still fulfilling the condition that the complex is planar. The orientation can be defined by the dihedral angles $\angle\left(H_{n b}-O-H_{b} \cdots N 3\right)$ and $\angle\left(O-H_{b} \cdots N 3-C 2\right)$ both of which can obtain a value of 0 or $180^{\circ}$. The four possible orientations are depicted in figure 5.5.

| i $\begin{aligned} & \angle\left(H_{n b}-O-H_{b} \cdots N 3\right)=180^{\circ} \\ & \angle\left(O-H_{b} \cdots N 3-C 2\right)=0^{\circ} \end{aligned}$ | ii |  $0^{\circ}-0^{\circ}$ |
| :---: | :---: | :---: |
| iii $0^{\circ}-180^{\circ}$ |  |  $180^{\circ}-180^{\circ}$ |

Figure 5.5. The four possible orientations of the $\mathrm{H}_{2} \mathrm{O}$ subunit with respect to the imidazole ring in imid $\cdots \mathrm{H}_{2} \mathrm{O}$. The two relative dihedral angles are justified in red and green, respectively.

Fits were performed for all four possible structures. When assuming that $\angle\left(H_{n b}-O-H_{b}\right.$. $\cdot N 3)=0^{\circ}$, the fit does not converge, eliminating structures ii and iii. Fits performed assuming $\angle\left(H_{n b}-O-H_{b} \cdots N 3\right)=180^{\circ}$ generated two structures, i and iv, for both of which structural parameters were determined with high precision. The structural parameters in table 5.7 were determined while assuming $\angle\left(O-H_{b} \cdots N 3-C 2\right)=0^{\circ}$. An alternative set of structural parameters is obtained when $\angle\left(O-H_{b} \cdots N 3-C 2\right)=180^{\circ}$ which is not included here. Two sets of structural parameters were determined for the isoxazole $\cdots \mathrm{H}_{2} \mathrm{O}$ and pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$, both of which fitted the experimentally determined rotational constants and moment of inertia. In the case of isoxazole $\cdots \mathrm{H}_{2} \mathrm{O}$, the correct
structure was determined based on the experimentally determined nuclear quadrupole coupling constants $\chi_{a a}(N)$. For imid $\cdots \mathrm{H}_{2} \mathrm{O}$, the atomic coordinates of N1 and N3 are effectively the same in structures i and iv, within $1 \%$ of the magnitude of the coordinates, with the standard deviations of the measured values of $\chi_{a a}(N 1)$ and $\chi_{a a}(N 3)$ being of comparable magnitude, therefore making this test inconclusive. However, looking at the DFT calculated geometry, it is clear that $\angle\left(O-H_{b} \cdots N 3-C 2\right)=0^{\circ}$. Setting that dihedral angle to the DFT value, the best agreement between fitted and calculated structural parameters is obtained. The results in table 5.6 and 5.7 are calculated on the assumption that $\angle\left(O-H_{b} \cdots \mathrm{~N} 3-C 2\right)=0^{\circ}$. When assuming $\angle\left(O-H_{b} \cdots N 3-C 2\right)=180^{\circ}$, the values of the fitted structural parameters are $r\left(H_{b} \cdots N 3\right)=2.006(41) \AA, \angle\left(H_{b} \cdots N 3-C 2\right)$ $=89.7(42)^{\circ}$ and $\angle\left(O-H_{b} \cdots N 3\right)=146.9(29)^{\circ}$. This structure brings $\mathrm{H}_{\mathrm{b}}$ in close proximity to H 2 at only $2.24 \AA$ apart which is too short an interaction given that the sum of the van der Waals radii for two hydrogen atoms is $2.4 \AA$. A list of atomic $r_{0}$ coordinates of both structures i and iv can be found in table A5 appendix A.

Table 5.7. Experimentally-determined ( $\mathrm{r}_{0}$ ) and DFT-calculated $\left(\mathrm{r}_{\mathrm{e}}\right)$ structural parameters of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid.

| Parameter ${ }^{\text {a }}$ |  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | Parameter ${ }^{\text {a }}$ |  | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $r\left(H_{b} \cdots N 3\right)(\AA)$ | $r_{e}$ | 1.931 | $r(H 1 \cdots O)(\AA)$ | $r_{e}$ | 1.953 |
|  | $r_{0}$ | $2.024(29)^{\text {b,c }}$ |  | $r_{0}$ | $2.007(4)^{\text {b }}$ |
| $\angle\left(H_{b} \cdots N 3-C 2\right)\left({ }^{\circ}\right)$ | $r_{e}$ | 116 | $\angle(H 1 \cdots O \cdots \mathrm{X})\left({ }^{\circ}\right)$ | $r_{e}$ | 153 |
|  | $r_{0}$ | 89.5(32) |  | $r_{0}$ | 152(6) |
| $\angle\left(O-H_{b} \cdots N 3\right)\left({ }^{\circ}\right)$ | $r_{e}$ | 171 |  |  |  |
|  | $r_{0}$ | 172.2(26) |  |  |  |

${ }^{\text {a }}$ See text and Figure 5.5 for parameter definitions.
${ }^{b}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\text {c }}$ The $r_{0}$ parameters are those determined under one of two alternative model geometries which fit the rotational constants with high accuracy (see text for details).

A hydrogen bond deviating from linearity is observed in imid $\cdots \mathrm{H}_{2} \mathrm{O}$, consistent with results for pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$, pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$ and pyridazine $\cdots \mathrm{H}_{2} \mathrm{O}$. This is the result of secondary interactions between the O atom of the $\mathrm{H}_{2} \mathrm{O}$ subunit and hydrogen atoms on carbon atoms adjacent to the pyridinic nitrogen in each of imidazole, pyridine, pyrimidine
and pyridazine. In the case of imidazole, the secondary interaction is observed between O and the H 2 hydrogen on the C 2 carbon. The angle $\angle\left(O-H_{b} \cdots N 3\right)$ is calculated to be $171^{\circ}$ at the $\omega$ B97X-D/aug-cc-pVQZ level being in excellent agreement with the experimental value of $172.1(26)^{\circ}$. From the $r_{0}$ fit, the $r(O \cdots H 2)$ distance is derived to be $3.13(8) \AA$ which is significantly lower than the DFT calculated $3.54 \AA$ value. This may be rationalized by the fact that DFT calculates the equilibrium geometry while the fitted rotational constants used for the $r_{0}$ fit are determined for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ the zero-point. The primary hydrogen bonding interaction is characterized within reasonable precision at the $\omega$ B97X-D/aug-cc-pVQZ level whilst the weak, secondary interaction is significantly underestimated.

It was discussed earlier that large amplitude motions occur in $\mathrm{H}_{2} \mathrm{O} \cdots$ imid which mainly involves the two hydrogen atoms of the water subunit. The angle $\angle(O \cdots H 1-N 1)$ which defines the position of the O atoms with respect to the imidazole ring was fixed to the DFT value of $174.7^{\circ}$. The values of the inertial defects $\Delta_{0}$ and planar moments $P_{c c}$ calculated earlier for the two spectral states that were assigned to that isomer and its isotopologues, suggest that only the hydroxylic protons lie outside the plane. Based on that, the dihedral $\angle(O \cdots H 1-N 1-C 2)$ was fixed to $180^{\circ}$, placing the O atom in the plane of the imidazole ring. A dummy atom X was placed between the two hydrogen atoms and on the $\mathrm{C}_{2}$ axis dissecting the plane of the water subunit. The dummy atom also lies in the plane of the imidazole ring such that $\angle(X \cdots O \cdots H 1-N 1)=0^{\circ}$. This assumption is based on the DFT calculated geometry suggesting that the hydrogen atoms are symmetrically located on either side of the imidazole plane.

The fitted $r_{0}$ structural parameters obtained under the constraints described above yield the values summarized in table 5.6 and 5.7. These are $r_{0}(\mathrm{O} \cdots \mathrm{H} 1)=2.000(4) \AA$ and $\angle(X \cdot \cdot$ - $O \cdots H 1$ ) $=159(7)^{\circ}$ and in good agreement with the DFT calculated structures; however, it is not possible to determine more structural parameters unless more assumptions are made. If it is assumed that $\angle(X \cdots O \cdots H 1-N 1)=180^{\circ}$, then $r(O \cdots H 1)=2.001(4) \AA$ and $\angle(X \cdots O \cdots H 1)=151(7)^{\circ}$. Both assumptions yield results within the range of the large amplitude motions of wagging and torsion within the water molecule, as it will be shown in section 5.6. Within the PES scans, transitions states are identified at $\angle(X \cdots O \cdots H 1-$ $N 1)=90^{\circ}$ or $270^{\circ}$. Pursuing the fit while assuming the above angles yields similar values for both $r(O \cdots H 1)$ and $\angle(X \cdots O \cdots H 1)$ but at the expense of greater uncertainties. The
residuals that describe the differences between measured values of rotational constants and those implied by the fitted structures are higher for $A_{0}$ than for $B_{0}$ and $C_{0}$. This suggests that large amplitude motions are mainly associated with a torsional motion around the $\angle(X-O \cdots H 1-N 1)$ coordinate and a wagging motion defined by the angle $\angle(X \cdots O \cdots$ H1). Similar interpretations for the large amplitude motions identified for similar complexes such as $\mathrm{H}_{2} \mathrm{O} \cdots$ indole and $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole.

### 5.6 Potential Energy Scans of Intermolecular Coordinates of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$

The large amplitude motions in $\mathrm{H}_{2} \mathrm{O} \cdots$ imid were modelled with DFT calculations characterizing the PES's of those motions. The PES's were produced at the $\omega$ B97X-D/aug-cc-pVQZ level while all internal coordinates, except for the scanned ones described below, were fixed. The dummy atom X that was used in the structure fits was also implemented here for the definition of the scanned coordinates. The PES calculated when varying the angle $\angle(X \cdots O \cdots H 1)$ between $130^{\circ}$ and $210^{\circ}$ is depicted in figure 5.6. This coordinate corresponds to the wagging motion of the water molecule, mainly involving the hydrogen atoms. The PES is relatively flat and exhibits two shallow minima at $154^{\circ}$ and $200^{\circ}$ separated by a barrier of approximately $10 \mathrm{~cm}^{-1}$.


Figure 5.6. Calculated potential energy surface tracing the wagging motion of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ at the $\omega$ B97X-D/aug-cc-pVQZ level. The transparent white spheres are drawn to illustrate the molecular geometries when $\angle(X \cdots O \cdots H 1)$ is $90^{\circ}$ or $200^{\circ}$. The trend rises steeply towards higher energy beyond the limits of this plot.

The PES describing a torsional motion of the $\mathrm{H}_{2} \mathrm{O}$ subunit is shown in figure 5.7. The coordinate that was scanned describes the angle formed between the $\mathrm{X} \cdots \mathrm{O}$ vector and the imidazole plane between 0 and $180^{\circ}$. Two minima are observed at both 0 and $180^{\circ}$ and the barrier to interconversion is approximately $143 \mathrm{~cm}^{-1}$. It is very likely that both motions may contribute to the large amplitude motions causing the spectral splitting in $\mathrm{H}_{2} \mathrm{O} \cdots$ imid.


Figure 5.7. 1D potential energy surface of a torsional motion in $\mathrm{H}_{2} \mathrm{O} \cdots$ imid defined by the angle formed by the $\mathrm{X} \cdots \mathrm{O}$ vector and the imidazole plane between 0 and $180^{\circ}$ at the $\omega$ B97X-D/aug-cc-pVQZ level. The opaque white spheres indicate the molecular geometries where this angle is equal to $30^{\circ}$ or $120^{\circ}$ respectively.

### 5.7 Force Constant and Dissociation Energy of the $\mathrm{N} \cdots \mathrm{H}-\mathrm{O}$ and $\mathrm{O} \cdots \mathrm{H}-\mathrm{N}$ non-Covalent

 BondsThe intermolecular stretching force constants $k_{s}$ for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ may be evaluated by a model introduced by Millen, described in detail elsewhere. ${ }^{46}$ The model approaches complexes by means of a pseudodiatomic model which considers the geometry of the complex subunits. In order to apply the model, it is required that $a$-axis of the complex is aligned or almost aligned with the axis of the intermolecular hydrogen bond, which applies for both imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$. The model assumes that contributions to the fitted value of the centrifugal distortion $D_{J}$ by stretching modes other than that of the intermolecular interaction are negligible. It also assumes that upon complexation, the geometry of the subunits remains unaffected. The model is strictly designed for equilibrium values of rotational and centrifugal distortion constants but given that these are rarely available, zero-point quantities may be used. The stretching force constant $k_{s}$ is expressed as;

$$
\begin{equation*}
k_{s}=16 \pi^{4}\left(\mu R_{C M}\right)^{2}\left[4 B_{0}^{4}+C_{0}^{4}-\left(B_{0}^{4}-C_{0}^{4}\right)^{2}\left(B_{0}^{4}+C_{0}^{4}\right)^{2}\right] /\left(h D_{J}\right) \tag{Eq.5.1}
\end{equation*}
$$

where $\mu$ is the reduced mass of the pseudodiatomic, expressed as $\mu=\frac{M_{I} M_{W}}{M_{I}+M_{W}}$ where $M_{I}$ and $M_{W}$ are the mass of the imidazole and water subunits, respectively. The distance between the centers of mass between the two subunits is defined by $R_{C M}$. The stretching frequency ${ }^{47}$ of the intermolecular interaction $v$ is given by the expression;

$$
\begin{equation*}
v=\frac{1}{2 \pi c} \sqrt{\frac{k_{s}}{\mu}} \tag{Eq.5.2}
\end{equation*}
$$

where $c$ is the speed of light.
Results for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ alongside those for other complexes of six- and five-membered $N$-heteroaromatics with water are summarized in table 5.8. These are calculated from the rotational and centrifugal distortion constants determined here and from previous studies. For pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$, two values are calculated for $k_{s}$ and $v$, each one corresponding to the rotational and centrifugal distortion constants determined for the individual substates. Looking at table 5.8, it is apparent that values for $k_{s}$ and $v$ are generally larger for complexes between $N$-heteroaromatics and water where
the latter is acting as the proton acceptor. The force constant describing the hydrogen bond in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is twice the magnitude of those in each state of pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$. Comparing imid $\cdots \mathrm{H}_{2} \mathrm{O}$ to pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$, pyridazine $\cdots \mathrm{H}_{2} \mathrm{O}$ and $1,3,5$-triazine $\cdots \mathrm{H}_{2} \mathrm{O}, k_{s}$ and $v$ are of similar magnitude. This highlights the similarities in the intermolecular hydrogen bond in these complexes. The values of $k_{s}$ and $v$ for the $0^{-}$state of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ are similar to those determined for the respective state in $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole. The values of $k_{s}$ and $v$ determined for the two states of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ are significantly different from one another. It is likely that the effects of the internal motions described earlier are affecting the values of the centrifugal distortion constants and this reflects on the force constants and stretching frequencies of these bonds. The assumption that stretching modes other than that for the intermolecular hydrogen bond have a negligible contribution to the measured centrifugal distortion constants is therefore unreliable. Secondary interactions like those described for the complexes in table 5.7 will have a significant contribution to the values of the centrifugal distortion constants and subsequently to $k_{s}$ and $v$. For these reasons, it is not possible to draw further conclusions about the strength of these interactions by looking at the force constants alone.

Table 5.8. Stretching force constants $k_{s}$, and stretching wavenumbers $v / c$, determined for the hydrogen bonded complexes discussed in this work and in references 15,17,19, 21-23.

|  | $k_{\mathrm{s}}\left(\mathrm{kg} \mathrm{m} \mathrm{s}^{-2}\right)$ | $v / c\left(\mathrm{~cm}^{-1}\right)$ |
| :---: | :---: | :---: |
| imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | $10.69(17)^{\mathrm{a}}$ | $112.9(9)$ |
| isoxazole $\cdots \mathrm{H}_{2} \mathrm{O}$ | $26.9(10)$ | $178.6(33)$ |
| pyridine $\cdots \mathrm{H}_{2} \mathrm{O}^{\mathrm{b}}$ | $4.36(11) / 5.95(16)$ | $71.0(9) / 82.9(11)$ |
| pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$ | 13.8 | 126 |
| pyridazine $\cdots \mathrm{H}_{2} \mathrm{O}$ | 13.1 | 122.8 |
| $1,3,5$-triazine $\cdots \mathrm{H}_{2} \mathrm{O}$ | 9.05 | 108.1 |
| $\mathrm{H}_{2} \mathrm{O} \cdots$ imid $^{\mathrm{b}}$ | $22.0(8) / 45.6(1.9)$ | $162(3) / 233(5)$ |
| $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole | 28 | 180 |

[^2]
### 5.8 Nuclear Quadrupole Coupling Constants

Measured nuclear quadrupole coupling constants $\chi_{a a}$ and $\chi_{b b}-\chi_{c c}$ of N1 and N3 in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ are sensitive to subtle changes in the electronic environment around the N nuclei. To perform direct comparisons on the coupling between imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid and the imidazole monomer, the diagonalized coupling terms $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ are calculated with QDIAG following the procedure described for PCA in chapter 4 and the underpinning theory in chapter 2 . The off-diagonal term $\chi_{a b}$ was calculated at the B3LYP(D3BJ)/aug-cc-pVTZ level for each complex (table 5.1) and $25 \%$ uncertainty of its value was given. The orientation of the $x$-, $y$ - and $z$-nuclear axes placed on N 1 and N3 are based on the convention established by Cristen et al. ${ }^{12}$ for the imidazole monomer. For N 1 , it holds that $\chi_{z z} \approx \chi_{c c}$, and for $\mathrm{N} 3, \chi_{y y} \approx \chi_{c c}$ because the complexes are essentially approaching planarity. The angle between the $x$-axis (for N1) or $y$-axis (for N3) and the $a$-axis is defined as $\varphi$. The derived values of $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ for N1 and N3 are in good agreement with those determined for the imidazole monomer and they are summarized in table 5.9.

No significant changes in the electronic environment around the N1 and N3 nuclei in imidazole are observed upon attachment of $\mathrm{H}_{2} \mathrm{O}$. The magnitude and sign of the $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ coupling component is consistent across imid $\cdots \mathrm{H}_{2} \mathrm{O}, \mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ and the imidazole monomer. As it was discussed in chapter 4 , the values of $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ will be somewhat dependent on the calculated values of $\chi_{a b}$. The measured values of the nuclear quadrupole coupling components are expected to be impacted by internal motions occurring at the water subunit causing changes at the efg on N1 and N3.

Table 5.9. Diagonal nuclear quadrupole coupling terms $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ for imid $\cdots \mathrm{H}_{2} \mathrm{O}$, $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ and imidazole monomer.

|  | Imid $\cdots \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{H}_{2} \mathrm{O} \cdots$ Imid | Imidazole $^{\mathrm{a}}$ |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{\chi}_{x x}(\mathrm{~N} 1)(\mathrm{MHz})$ | $1.096(27)$ | $0.912(74)$ | $0.890(52)$ |
| $\boldsymbol{\chi}_{y y}(\mathrm{~N} 1)(\mathrm{MHz})$ | $1.332(54)$ | $1.45(51)$ | $1.633(58)$ |
| $\boldsymbol{\chi}_{z z}(\mathrm{~N} 1)(\mathrm{MHz})$ | $-2.428(30)$ | $-2.36(23)$ | $-2.524(12)$ |
| $\boldsymbol{\eta}^{\mathrm{b}}$ | $0.097(25)$ | $0.23(22)$ | $0.1361(59)$ |
| $\boldsymbol{\chi}_{x x}(\mathrm{~N} 3)(\mathrm{MHz})$ | $1.23(19)$ | $1.92(78)$ | $1.835(23)$ |
| $\boldsymbol{\chi}_{\boldsymbol{y} \boldsymbol{y}}(\mathrm{N} 3)(\mathrm{MHz})$ | $1.980(56)$ | $2.30(22)$ | $2.278(24)$ |
| $\boldsymbol{\chi}_{z z}(\mathrm{~N} 3)(\mathrm{MHz})$ | $-3.21(15)$ | $-4.21(74)$ | $-4.113(34)$ |
| $\boldsymbol{\eta}^{\mathrm{b}}$ | $0.234(63)$ | $0.09(19)$ | $0.060(20)$ |

${ }^{a}$ Results from Christen et al. ${ }^{12}$
${ }^{\mathrm{b}}$ Asymmetry parameter $\eta=\left(\chi_{x x}-\chi_{y y}\right) / \chi_{z z}$

### 5.9 Discussion

A notable outcome of this work is that both imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid were formed and isolated in a free jet expansion of argon buffer gas. A previous FT-IR study by Zischang et al. featuring co-expansion of imidazole, from a heated reservoir, and water in a helium buffer only identified the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ isomer. ${ }^{25}$ The authors reported that their sample preparation conditions did not yield the $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ isomer and suggested that it effectively relaxes into imid $\cdots \mathrm{H}_{2} \mathrm{O}$. The competition between kinetic and thermodynamic control within an expanding gas sample was previously explored by Ruoff et al. ${ }^{48}$ According to their work, conformational relaxation to lower energy configurations occurs more effectively in a gas sample that contains a high concentration of krypton or argon. Higher energy conformations are more readily accessible within an expanding gas sample containing neon or helium. The supersonic expansion dynamics were briefly discussed in chapter 2. Considering that in this work the two isomers were formed in an argon buffer expansion and the observation of Ruoff et al., ${ }^{48}$ it is anticipated that both isomers might be observable in a neon or helium supersonic expansion. A similar conclusion was drawn by FT-IR experiments on benzimidazole ${ }^{26}$ and N -methylbenzimidazole. ${ }^{49}$

The question "where does the first water molecule go in imidazole?" was posed by Zischang et al. in their aforementioned work ${ }^{25}$ and it was concluded that imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is the lowest energy isomer. In this work, imid $\cdots \mathrm{H}_{2} \mathrm{O}$ was observed with a higher intensity than $\mathrm{H}_{2} \mathrm{O}$ imid despite the fact that the latter is calculated to have a larger dipole moment than the former $\left(\left|\mu_{a}\right|=5.3 \mathrm{D}\right.$ and $\left.\left|\mu_{a}\right|=6.2 \mathrm{D}\right)$. The spectrum of $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ was split into two components, $0^{-}$and $0^{+}$, due to internal motions associated with the water subunit which may result in an overall decrease of signal intensity. In our experiment, it is not possible to directly correlate signal intensity with the relative energy of the two isomers. DFT calculations suggest that imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is lower in energy than $\mathrm{H}_{2} \mathrm{O} \cdots$ imid, however, this cannot be determined by the experimental results.

Geometrical parameters for a number of $N$-heteroaromatic monohydrates are shown in table 5.10. A primary hydrogen bond is observed between the pyridinic nitrogen of pyrazine, pyridine, pyridazine, 1,3,5-triazine, 2-fluoropyridine, oxazole and imidazole (this work) and water as well as a secondary interaction with $\mathrm{C}-\mathrm{H}$ bonds adjacent to each pyridinic nitrogen. The interplay between primary and secondary interactions determines the orientation of the water subunit in each monohydrate, particularly the $\angle(\mathrm{O}-\mathrm{Hb} \cdots$ $N 3$ ) angle. In table 5.10, it is observed that the primary hydrogen bond deviates from
linearity with the $\angle(O-H b \cdots N 3)$ angle varying between $141.12^{\circ}$ in oxazole and $172.2^{\circ}$ in imidazole. The length of the primary hydrogen in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is similar to that in pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$, as it is expected considering the similarities in the immediate chemical environment. ${ }^{19}$ The calculated $r\left(H_{b} \cdots N\right)$ in pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ is $1.95 \AA$ whilst the experimentally determined value of $r\left(H_{b} \cdots N 3\right)$ in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is $1.927(27) \AA$. The length of the secondary interaction in imidazole $r(O \cdots H 2)$ was determined to be $3.05 \AA$ which longer than the respective secondary interaction in pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ by approximately 0.36 $\AA$. Fewer complexes with a primary hydrogen bond at the pyrrolic nitrogen of an $N$ heteroaromatic are available. The $\angle(O \cdots H 1-N 1)$ angle of $\mathrm{H} 2 \mathrm{O} \cdots \mathrm{imid}$ is calculated to be $174.7^{\circ}$ implying that linearity of the hydrogen bond is compromised by some secondary interaction between the imidazole ring and the water subunit. The $\angle(X \cdots O \cdots H 1)$ angle ranges from $143^{\circ}$ for $\mathrm{H} 2 \mathrm{O} \cdots$ pyrrole to $165^{\circ}$ for $\mathrm{H} 2 \mathrm{O} \cdots$ indole. Structural parameters in all these molecules are expected to be somewhat contaminated by the large amplitude molecules concerning the water subunit in each one of them.

Table 5.10. Lengths and geometries of hydrogen bonds reported for complexes described in references $17,18,19,21-23,15$.

| Proton donor $=\mathrm{H}_{2} \mathrm{O}$ | $\boldsymbol{r}\left(\boldsymbol{H}_{\boldsymbol{b}} \cdots \boldsymbol{N} 3\right)(\AA)$ | $\angle\left(\boldsymbol{O}-\boldsymbol{H}_{\boldsymbol{b}} \cdots \boldsymbol{N} 3\right)\left({ }^{\circ}\right)$ |
| :---: | :---: | :---: |
| 6-membered rings |  |  |
| pyrazine $\cdots \mathrm{H}_{2} \mathrm{O}$ | $1.94(2)$ | $152(4)$ |
| pyridine $\cdots \mathrm{H}_{2} \mathrm{O}^{\mathrm{a}}$ | 1.95 | 156 |
| pyrimidine $\cdots \mathrm{H}_{2} \mathrm{O}$ | 1.98 | 164.7 |
| pyridazine $\cdots \mathrm{H}_{2} \mathrm{O}$ | 2.04 | 165.5 |
| 5-membered rings |  |  |
| imid $\cdots \mathrm{H}_{2} \mathrm{O}^{\mathrm{b}}$ | $2.024(23)$ | $172.2(26)$ |
| isoxazole $\cdots \mathrm{H}_{2} \mathrm{O}$ | 2.1467 | 141.12 |
| Proton donor $=\mathrm{N}-$ | $r(H 1 \cdots O)(\AA)$ | $\angle(H 1 \cdots O \cdots X)\left({ }^{\circ}\right)$ |
| heteroaromatic | - | $143(5)$ |
| $\mathrm{H}_{2} \mathrm{O} \cdots$ pyrrole | $2.007(4)$ | $152(6)$ |
| $\mathrm{H}_{2} \mathrm{O} \cdots$ imid ${ }^{\mathrm{b}}$ | $2.007(5)$ | $165(5)$ |
| $\mathrm{H}_{2} \mathrm{O} \cdots$ indole |  |  |

[^3]
### 5.10 Outlook

The broadband rotational spectra of two isomers of a monohydrate complex formed between imidazole and water, imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid, were recorded in the 7.0-18.5 GHz region. Rotational constants, centrifugal distortion constants and nuclear quadrupole coupling constants were determined experimentally for both species. A non-linear hydrogen bond is observed in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ as a result of a secondary interactions. Secondary interactions also appear to affect the linearity of the hydrogen bond in the $\mathrm{H}_{2} \mathrm{O} \cdots$ imid isomer too. Two substates, $0^{-}$and $0^{+}$, were observed in the spectra of $\mathrm{H}_{2} \mathrm{O} \cdots$ imid as a result of large amplitude motions within the water moiety. Observation of both isomers in an argon free jet expansion suggests that both isomers are similar in energy.

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# Chapter 6. Barriers to Internal Rotation in Methylimidazole Isomers 

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### 6.1 Introduction

The imidazole monomer ${ }^{1,2}$ was discussed in chapter 5 in the context of stepwise microsolvation. Imidazole, alongside pyridine, pyrimidine, and pyrrole, among others, is an $N$-heterocyclic compound with a significant role in chemistry, ${ }^{3}$ medicine, ${ }^{4}$ biochemistry, ${ }^{5}$ and photochemistry. ${ }^{6}$ Structural isomers of methylimidazole exhibit very different physical properties as well as different toxicity levels. ${ }^{7}$ Some imidazoles can be key compounds around tumor growth and development of certain cancers. ${ }^{6,8}$ To a certain extent, their properties can be controlled by addition of functional groups resulting in functionalized imidazoles with anti-cancer, ${ }^{6}$ anti-fungal ${ }^{9}$ and anti-HIV ${ }^{4}$ activity, among others. Substitution across an aromatic ring with $\mathrm{CH}_{3}$ groups is common and will modify its physical and chemical properties. ${ }^{7,10}$ Microwave spectroscopy is a powerful method in probing the energetic hindering potential of internal rotation of $\mathrm{CH}_{3}$ groups. ${ }^{11}$

A large number of methylated aromatic molecules have been characterized by microwave spectroscopy and barriers to internal rotation of the methyl group have been determined. ${ }^{12-}$ ${ }^{17}$ It is crucial to determine and rationalize energetic barriers and obtain information on bonding preferences in order to establish fundamental conformational preferences. Gas phase measurements at temperatures as low as 2 K allow for precise determination of such properties by analysis of the rotational signatures of individual molecules. ${ }^{18}$ The barrier to internal rotation of the methyl group in toluene is effectively unhindered. Fluorination of toluene ${ }^{19,20}$ at the ortho- and meta-positions hinders the essentially free internal rotation of the methyl group and creates a threefold periodic barrier which will be denoted as $V_{3}$. The presence of fluorine substituents at one of the ortho- positions in toluene leads to a barrier in the order of $200 \mathrm{~cm}^{-1}$. Lower barriers are observed when a single fluorine atom is at a meta- or para- position, of the order of $5-16 \mathrm{~cm}^{-1}$. The $V_{3}$ barriers to internal rotation of the $\mathrm{CH}_{3}$ group in isomers of methylthiazole ${ }^{18,21,22}$ and methyloxazole ${ }^{23}$ depend on the position where the $\mathrm{CH}_{3}$ is attached. The $V_{3}$ barrier in 2-methyloxazole is $252 \mathrm{~cm}^{-1}$ while in 4methyloxazole and 5-methyloxazole that value becomes 428 and $478 \mathrm{~cm}^{-1}$, respectively.

In this chapter, the microwave spectra of $N$-methylimidazole ( $N$-MI), 2-methylimidazole (2-MI), 4-methylimidazole (4-MI) and 5-methylimidazole (5-MI) in the $7.0-18.5 \mathrm{GHz}$ frequency range are reported and analyzed. The geometry of the isomers and the internal rotation parameters are also approached by DFT calculations. Supersonic expansion and laser ablation methods described in chapter 3 were used to probe the molecules of interest. Data for 2-MI were collected and provided by Chris Medcraft and Juliane Heitkämper. 4MI and 5-MI co-exist as a tautomeric mixture and were thus probed within the same experiment. The $V_{3}$ for these two isomers was determined by B. Harris as part of their PhD thesis ${ }^{24}$ and these values are $311.9362(78)$ and $378.416(68) \mathrm{cm}^{-1}$, respectively. $N$-MI, which is a liquid under ambient conditions, was placed in the reservoir described in section 3.3 and seeded directly into the flow of the expanding argon carrier gas.

### 6.2 Experimental

The microwave spectra of N -MI, 2-MI, 4-MI and $5-\mathrm{MI}$ were recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range. $N$-MI (Sigma-Aldrich, 99\%) was vaporized from the reservoir described in chapter 3, section 3.3, and seeded directly into the flow of argon in the supersonic expansion. The 4(5)-MI (Sigma-Aldrich, 98\%) tautomeric pair was mixed with Cu powder (Sigma-Aldrich, $<75 \mu \mathrm{~m}, 99 \%$ ) and $\mathrm{MgSO}_{4}$ (Sigma-Aldrich, $\geq 99.5 \%$ ) and pressed into a 13 mm diameter rod in 1:1:1 by mass ratio. Rods containing 2-MI (Sigma-Aldrich, 98\%) and $\mathrm{Cu} 1: 1$ by mass ratio were prepared by Chris Medcraft and Juliane Heitkämper. Vaporized material from the rods were entrained into the supersonic jet of expanding Ar which was kept at 7 bar constant backing pressure for laser ablation experiments and 2 bar for $N$-MI.

### 6.3 Density Functional Theory

Density Functional Theory (DFT) calculations on $N$-MI, 4-MI and 5-MI (figure 6.1) were performed prior to experiments using Gaussian 09 . Geometry optimizations were carried out using the B3LYP functional, with D3BJ correction. The functional was used in conjunction with three basis sets: cc-pVTZ, aug-cc-pVTZ and Def2-TZVP. Calculated rotational constants are benchmarked against experimentally determined constants and their percentage deviations are summarized in table 6.1. Given the level of consistency with the experiment at the B3LYP(D3BJ)/aug-cc-pVTZ level, atomic $r_{e}$ coordinates of optimized geometries, the off-diagonal nuclear quadrupole coupling terms $x_{a b}(N 1)$ and $x_{a b}(N 3)$, centrifugal distortion constants $D_{J}, D_{J K}, D_{K}, d_{1}, d_{2}$ and potential energy curves of estimated $V_{3}$ barriers to internal rotation are calculated at that level too. The relative coordinate that was scanned to estimate the $V_{3}$ barriers to internal rotation was the dihedral $\angle(H-C 6-N 1-C 2), \angle(H-C 6-C 2-N 3), \angle(H-C 6-C 4-C 5)$ and $\angle(H-C 6-$ $C 5-N 1$ ) for each of $N$-, 2-, 4- and $5-\mathrm{MI}$, respectively. Calculations on $2-\mathrm{MI}$ at the B3LYP(D3BJ)/aug-cc-pVTZ level were performed by C. Medcraft and J. Heitkämper and are used here for comparisons.


Figure 6.1. Calculated equilibrium geometries of $N-, 2-, 4-$, and $5-\mathrm{MI}$. Dipole moments are drawn to extend from positive to negative charges.

### 6.4 Initial Assumptions and Observations

The calculated geometries of $N$-, 2-, 4- and 5-MI are displayed in figure 6.1. Considering the calculated geometries and calculated rotational constants, all four isomers are asymmetric tops close to the prolate limit with the $a$-inertial axis being almost co-linear with the $\mathrm{H}_{3} \mathrm{C}-\mathrm{N}$ bond of N -MI and the $\mathrm{H}_{3} \mathrm{C}-\mathrm{C}$ bond of $2-, 4-$ and $5-\mathrm{MI}$. The molecular skeleton of the aromatic ring lies within the plane defined by the $a$ - and $b$-inertial axes which are mutually perpendicular to the $c$-axis. The electric dipole moment is dependent on the arrangement of the pyrrolic and pyridinic nitrogen within the ring with respect to the $a$ - and $b$-inertial axes. In all cases, the dipole moment lies within the plane of the aromatic ring. The microwave spectra of $N-, 2-, 4-$ and $5-\mathrm{MI}$ in the $7.0-18.5 \mathrm{GHz}$ frequency range are displayed in figure 2.2, 2.4 and 2.5 and were collected over the course of 1.14, 0.9 and 2.6 M FID's, respectively, with 4- and 5-MI co-existing in the same spectrum. Expanded portions of the spectra with selected transitions are displayed in figure 2.3 and 2.6. At first glance, the spectra carry hyperfine structure induced by the presence of pyrrolic and pyridinic nitrogen (nuclear spin $I=1$ ) in the aromatic rings. A total of 150 to 300 hyperfine transitions were assigned to the spectrum of each isomer. The ratio of identified transitions of $a$ - and $b$-type is consistent with the ratio of the $\left|\mu_{a}\right|$ and $\left|\mu_{b}\right|$ dipole moment components in each isomer.

It was discussed before that laser ablation of organic molecules, particularly those containing nitrogen, generates a series of gas phase reaction products. It is believed that these products are generated by fragmentation of the precursor organic molecules and, potentially, subsequent recombination of these fragments in the gas phase. In the spectra of 2-, 4- and 5-MI, identified fragmentation products ${ }^{2,25-31}$ include $\mathrm{HC}_{3} \mathrm{~N}, \mathrm{HC}_{5} \mathrm{~N}, \mathrm{HC}_{7} \mathrm{~N}$, $\mathrm{CH}_{3} \mathrm{CN}, \mathrm{CH}_{2}=\mathrm{CHCN}$ (vinyl cyanide), $\mathrm{CH}_{3} \mathrm{CCCN}$ (methylcyanoacetylene) and $\mathrm{C}_{5} \mathrm{~N}_{2} \mathrm{H}_{3}$ (imidazole). In previous studies of imidazole (chapter 5) and trans-urocanic acid, ${ }^{32}$ to name a few, essentially the same range of side-products was observed when they we laser ablated under similar experimental conditions. After assignment of the spectra of MI isomers, there is a large number of remaining unassigned lines with only a fraction the intensity of the parent MI. As it will be discussed in the chapter 7, some of these lines were assigned to weakly bound complexes formed between methylimidazole isomers and $\mathrm{H}_{2} \mathrm{O}$ and Ar.

Presence of a $\mathrm{CH}_{3}$ within each MI isomer suggests that internal rotation of that group coupling to the overall molecular rotation is possible. Considering previous studies of
similar methylated aromatic and heteroaromatic molecules, e.g. toluene, ${ }^{33}$ isomers of methylpyridine, ${ }^{34-36}$ methylpyrimidine, ${ }^{37}$ methylpyrrole, ${ }^{38,39}$ methylthiazole, ${ }^{18,21,22}$ and methyloxazole, ${ }^{18}$ where internal rotation of the $\mathrm{CH}_{3}$ group was examined, it is likely that the $\mathrm{CH}_{3}$ in MI isomers is also rotating internally. Evidence supporting this assumption is provided by the calculated $V_{3}$ barriers to internal rotation as well as the presence of "doublets" in the spectra. Rotational levels are split into $A$ - and $E$-states ( $m=0$ and $m=$ $\pm 1$, respectively) when a group of 3-fold symmetry is present within the molecule and undergoes internal rotation. Details on the underpinning theory of internal rotational is provided in Chapter 2 section 2.9. Fitting of $A$-states ${ }^{\mathrm{B}}$ was possible using a semi-rigid asymmetric Hamiltonian (section 2.7). A global fit of both $A$ - and $E$-states requires the inclusion of terms accounting for the internal rotation (section 2.9). The fitting procedures as well as the information derived from the fits will be discussed in detail in the following sections.

[^4]
### 6.5 Fitting of A-States

Fitting of $A$-States molecular transitions was performed with Pgopher ${ }^{40}$ using Watson's Sreduced Hamiltonian ${ }^{41}$ (chapter 2, section 2.7). The Hamiltonian contains information about $A_{0}, B_{0}$ and $C_{0}$ rotational constants and $D_{J}, D_{J K}, D_{K}, d_{1}$ and $d_{2}$ distortion constants. The nuclear quadrupole coupling terms for the pyrrolic and pyridinic nitrogen, N1 and N 3 , respectively, are denoted as $\chi_{a a}$ and $\chi_{b b}-\chi_{c c}$. Upon rotation, the nuclear spin of N , $I=1$, couples to the rotational angular momentum $J$ resulting in formation of the quantum number $F$ expressing the total angular momentum (chapter 2, figure 2.5 and 2.6). On this basis, the quadrupole matrix is built in blocks of $F$. For MI isomers where two N nuclei are present, N 1 and N 3 , we have $J+I_{N 1}=F_{1}$ and $J+I_{N 3}=F$.

Experimentally determined spectroscopic parameters derived from fitting of $A$-states are summarized in table 6.2. Calculated rotational constants $A_{e}, B_{e}$ and $C_{e}$ are benchmarked against the experimentally determined ones (table 6.1) for the $A$-states which from now on will be denoted as $A_{0}^{\prime}, B_{0}^{\prime}$ and $C_{0}^{\prime}$ and called effective rotational constants. It was not possible to obtain an experimental value for $d_{1}$ and $d_{2}$ for $N-\mathrm{MI}$ and for $d_{2}$ for 2-MI. In these cases, the DFT calculated values for these parameters were included and kept fixed in the fits. The fits for 2-MI, 4-MI and 5-MI benefit significantly by inclusion of $d_{1}$ and $d_{2}$, resulting in reduced standard deviation of the fits ( $11.3,10.8$ and 12.8 kHz respectively) and reduced uncertainty in the rest of the fitted spectroscopic parameters (rotational constants, centrifugal distortion constants and nuclear quadrupole coupling constants). In the case of $N$-MI, inclusion of $d_{1}$ and $d_{2}$ does not affect the standard deviation or the uncertainties. However, for the sake of completeness and in order to adopt a consistent approach for all isomers, $d_{1}$ and $d_{2}$ were kept fixed at the DFT values. The fitted values of $D_{J}$ and $D_{J K}$ are consistently small for all MI isomers, as expected for semi-rigid aromatic molecules. Centrifugal distortion constants determined for similar aromatic molecules containing a methyl top are similar in magnitude. ${ }^{18,22,23,42}$


Figure 6.2. The microwave spectrum of $N-\mathrm{MI}$ in the $7.0-18.5 \mathrm{GHz}$ region collected over the course of 1.15 M FID's.


Figure 6.3. Expanded portion of the spectrum displayed in figure 2. The $3_{03} \rightarrow 2_{02}$ transition of $N$-MI averaged over 1.15 million FID's illustrating transitions of both $A(m=0)$ and $E$ ( $m= \pm 1$ ) symmetry states. Hyperfine splittings are introduced by the two nitrogen nuclei which are very similar for both $A$ - and $E$-states. The experimental spectrum is shown at the top (black) and the simulation at the bottom (green and red). The simulation for the $E$ states is generated by shifting the simulation for the $A$-states the appropriate amount of MHz.


Figure 6.4. The microwave spectrum of 2-MI in the $7.0-18.5 \mathrm{GHz}$ region collected over the course of 0.9 M FID's.


Figure 6.5. The microwave spectrum of 4 - and $5-\mathrm{MI}$ in the $7.0-18.5 \mathrm{GHz}$ region collected over the course of 2.6 M FID's.


Figure 6.6. Expanded portions of the spectrum of 4 - and 5-MI. The $2_{12} \rightarrow 1_{01}$ transitions of 4- and 5-MI averaged over 2.6 M FID's. The transitions are split into two components, $A$ and $E$-states, which is an outcome of internal rotation of the $\mathrm{CH}_{3}$ group in both molecules. The energy separation between the two states is proportional to the barrier to internal rotation, i.e. the calculated barrier for $5-\mathrm{MI}$ is higher than that of $4-\mathrm{MI}$, being consistent with a larger energy separation in 4-MI.

Table 6.1. Calculated rotational constants for $N$-, 2-, 4- and 5-MI. Percentage deviations of calculated rotational constants are calculated for performance benchmarking.

|  | $N$-Methylimidazole |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | B3LYP(D3BJ) |  |  |  |  |  |
|  | Def2-TZVP |  | cc-pVTZ |  | aug-cc-pVTZ |  |
| $A_{e}(\mathrm{MHz})^{\text {a }}$ | 9207.27 | $0.55 \%{ }^{\text {b }}$ | 9207.62 | $0.55 \%{ }^{\text {b }}$ | 9206.40 | $0.54 \%{ }^{\text {b }}$ |
| $B_{e}(\mathrm{MHz})$ | 3626.73 | 0.46\% | 3625.86 | 0.44\% | 3625.11 | 0.42\% |
| $C_{e}(\mathrm{MHz})$ | 2645.17 | 0.48\% | 2644.64 | 0.46\% | 2644.17 | 0.44\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|(D)^{\text {c }}$ | 3.9, 1.1, 0 |  | 3.9, 1, 0 |  | 4, 1, 0 |  |
|  | 2-Methylimidazole |  |  |  |  |  |
|  | B3LYP(D3BJ) |  |  |  |  |  |
|  | Def2-TZVP |  | cc-pVTZ |  | aug-cc-pVTZ |  |
| $A_{e}(\mathrm{MHz})$ | 8978.77 | 0.96\% | 8976.79 | 0.94\% | 8981.74 | 1.00\% |
| $B_{e}(\mathrm{MHz})$ | 3606.09 | 0.14\% | 3606.79 | 0.16\% | 3604.12 | 0.08\% |
| $C_{e}(\mathrm{MHz})$ | 2614.67 | 0.38\% | 2614.78 | 0.38\% | 2613.80 | 0.34\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | 0.6, 3.6, 0 |  | 0.6, 3.5, 0 |  | 0.6, 3.5, 0 |  |
|  | 4-Methylimidazole |  |  |  |  |  |
|  | B3LYP(D3BJ) |  |  |  |  |  |
|  | Def2-TZVP |  | cc-pVTZ |  | aug-cc-pVTZ |  |
| $A_{e}$ (MHz) | 9044.46 | 0.87\% | 9041.35 | 0.83\% | 9044.12 | 0.86\% |
| $B_{e}(\mathrm{MHz})$ | 3518.21 | 0.28\% | 3519.09 | 0.30\% | 3517.24 | 0.25\% |
| $C_{e}(\mathrm{MHz})$ | 2614.67 | 0.45\% | 2573.26 | 0.46\% | 2572.51 | 0.43\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | 2.1, 2.7, 0 |  | 2, 2.6, 0 |  | 2, 2.7. 0 |  |
|  | 5-Methylimidazole |  |  |  |  |  |
|  | B3LYP(D3BJ) |  |  |  |  |  |
|  | Def2-TZVP |  | cc-pVTZ |  | aug-cc-pVTZ |  |
| $A_{e}$ (MHz) | 9116.30 | 0.68\% | 9117.85 | 0.69\% | 9116.59 | 0.68\% |
| $B_{e}(\mathrm{MHz})$ | 3486.59 | 0.43\% | 3486.06 | 0.41\% | 3485.96 | 0.41\% |
| $C_{e}(\mathrm{MHz})$ | 2562.23 | 0.51\% | 2561.96 | 0.50\% | 2561.83 | 0.49\% |
| $\left\|\mu_{a}\right\|,\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|$ (D) | 2.7, 2.9, 0 |  | 2.7, 2.9, 0 |  | 2.8, 2.9, 0 |  |

${ }^{\text {a }}$ DFT-calculated rotational constants.
${ }^{b}$ Percentage deviations from experimental constants are calculated by means of equation $\left[\left(A_{e}-A_{0}\right) / A_{0}\right] \times 100$
${ }^{\mathrm{c}}$ Calculated electric dipole moment components along the principal inertial axes.

Table 6.2. Effective rotational constants $A_{0}^{\prime}, B_{0}^{\prime}$ and $C_{0}^{\prime}$ alongside other spectroscopic parameters determined by fitting A-state transitions of $N$-, 2-, 4- and 5-MI.

|  | $N-\mathrm{MI}$ | $2-\mathrm{MI}$ | $4-\mathrm{MI}$ | $5-\mathrm{MI}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{0}^{\prime}(\mathrm{MHz})$ | $9194.5817(17)^{\mathrm{a}}$ | $8992.75911(97)$ | $8971.89077(89)$ | $9057.12512(100)$ |
| $B_{0}^{\prime}(\mathrm{MHz})$ | $3609.78192(71)$ | $3600.99984(38)$ | $3508.27356(31)$ | $3471.61329(36)$ |
| $C_{0}^{\prime}(\mathrm{MHz})$ | $2632.63930(68)$ | $2604.96676(32)$ | $2561.66742(25)$ | $2549.43964(33)$ |
| $D_{J}(\mathrm{kHz})$ | $0.244(47)$ | $0.1947(56)$ | $0.2560(37)$ | $0.2206(40)$ |
| $D_{K}(\mathrm{kHz})$ | $44.51(91)$ | $97.06(11)$ | $7.882(18)$ | $3.080(33)$ |
| $D_{J K}(\mathrm{kHz})$ | $1.135(91)$ | $1.942(53)$ | $1.358(37)$ | $1.759(34)$ |
| $d_{1}(\mathrm{kHz})$ | $[-0.065776]^{\mathrm{b}}$ | $-0.0684(18)$ | $-0.0746(16)$ | $-0.0622(25)$ |
| $d_{2}(\mathrm{kHz})$ | $[-0.00108]$ | $[0.00512]$ | $-0.01540(93)$ | $-0.0146(11)$ |
| $\chi_{a a}(N 1)(\mathrm{MHz})$ | $1.7347(51)$ | $1.3010(59)$ | $1.4065(49)$ | $1.1630(66)$ |
| $\left[\chi_{b b}(\mathrm{~N} 1)-\chi_{c c}(\mathrm{~N} 1)\right](\mathrm{MHz})$ | $3.6373(83)$ | $4.178(10)$ | $3.8163(88)$ | $4.167(10)$ |
| $\chi_{a b}(\mathrm{~N} 1)(\mathrm{MHz})^{c}$ | $[-0.0793]$ | $[0.1263]$ | $[-0.1051]$ | $[-0.0643]$ |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | $-2.0837(52)$ | $1.3742(64)$ | $0.9529(55)$ | $-2.0975(57)$ |
| $\left[\chi_{b b}(\mathrm{~N} 3)-\chi_{c c}(\mathrm{~N} 3)\right](\mathrm{MHz})$ | $-2.200(10)$ | $-5.399(10)$ | $-5.1394(82)$ | $-2.415(12)$ |
| $\chi_{a b}(\mathrm{~N} 3)(\mathrm{MHz})^{\mathrm{c}}$ | $[-2.9276]$ | $[1.7777]$ | $[2.2221]$ | $[2.9711]$ |
| $\left\|\mu_{a \mid,}\right\| \mu_{b}\left\|,\left\|\mu_{c}\right\|(\mathrm{D})^{\mathrm{d}}\right.$ | $4,1,0$ | $0.6,3.5,0$ | $2,2.7,0$ | $2.8,2.9,0$ |
| $\Delta_{0}^{\prime}\left(\mathrm{u} \AA^{2}\right)$ | $-3.02267(6)$ | $-2.536524(29)$ | $-3.097382(24)$ | $-3.142257(30)$ |
| $P_{c c}^{\prime}\left(\mathrm{u} \AA^{2}\right)$ | $1.511333(29)$ | $1.268262(14)$ | $1.548691(12)$ | $1.571128(15)$ |
| $N^{e}$ | 150 | 195 | 236 | 251 |
| $\sigma_{\mathrm{RMS}}(\mathrm{kHz})^{\mathrm{f}}$ | 9.9 | 11.3 | 10.8 | 12.8 |

${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figures; ${ }^{b}$ Numbers in square brackets are fixed to results calculated using DFT at the B3LYP(D3BJ)/aug-cc-pVTZ level; ${ }^{c}$ Off-diagonal nuclear quadrupole coupling term, $\chi_{a b}$ fixed to DFTcalculated value; ${ }^{\text {d }}$ DFT-calculated results; ${ }^{\mathrm{e}}$ Number of hyperfine components included in the fit; ${ }^{\mathrm{f}}$ Root mean square deviation of the fit.

It was not possible to determine the off-diagonal nuclear quadrupole coupling terms, $\chi_{a b}(N 1)$ and $\chi_{a b}(N 3)$, through fitting of the available spectroscopic data. $\chi_{a b}(N 1)$ and $\chi_{a b}(N 3)$ were kept fixed at their DFT values and will be used for diagonalization of the $\chi_{a a}(N 1), \chi_{b b}(\mathrm{~N} 1)-\chi_{c c}(N 1), \chi_{a a}(N 3)$ and $\left.\chi_{b b}(\mathrm{~N} 3)-\chi_{c c}(N 3)\right)$ nuclear quadrupole coupling terms in section 6.8. Diagonalization results in determination of $\chi_{z z}, \chi_{y y}$ and $\chi_{x x}$ coupling terms which are expressed in terms of mutually perpendicular principal nuclear axes $z, y$ and $x$ placed on the individual quadrupolar nuclei N 1 and N 3 in each MI isomer. The signal to noise ( $\mathrm{S}: \mathrm{N}$ ) ratio of the spectra of the parent $N$-, $2-, 4$ - and $5-\mathrm{MI}$ was approximately $250: 1$, which allowed for observation of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues in their natural isotopic abundance. In section 6.6 molecular geometries, it will be shown how experimentally determined rotational constants for the available ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues resulted in determination of atomic coordinates of heavy atoms in the molecular skeleton of each MI isomer. The experimentally determined spectroscopic parameters of the available ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues are detailed in table 6.3 and 6.4. The nuclear quadrupole coupling constants $\chi_{a a}$ and $\chi \chi_{b b}-\chi_{c c}$ for N1 and N3 were kept fixed to the values determined for the respective parent isotopologue.

Table 6.3. Experimentally determined effective rotational constants for the torsional ground state of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of N - and 2MI.

|  | $N$-Methylimidazole |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }^{15} \mathrm{~N}(1)$ | ${ }^{13} \mathrm{C}(2)$ | ${ }^{15} \mathrm{~N}(3)$ | ${ }^{13} \mathrm{C}(4)$ | ${ }^{13} \mathrm{C}(5)$ | ${ }^{13} \mathrm{C}(6)$ |
| $A_{0}^{\prime}$ (MHz) | 9194.9288(38) ${ }^{\text {a,b }}$ | 9010.820(95) | 9114.31(22) | 9123.37(11) | 8986.80(11) | 9194.72(15) |
| $B_{0}^{\prime}$ (MHz) | 3598.4477(22) | 3609.2353(16) | 3558.0319(39) | 3558.9266(15) | 3609.5046(21) | 3498.3721(19) |
| $C_{0}^{\prime}$ (MHz) | 2626.6414(18) | 2617.0542(11) | 2598.50601(28) | 2599.7298(13) | 2615.1501(12) | 2572.8642(16) |
| $N^{\text {c }}$ | 13 | 31 | 7 | 25 | 28 | 25 |
| $\sigma_{\text {r.m. }}{ }^{\text {d }}$ (kHz) | 9.9 | 10.9 | 11.3 | 10.9 | 12.1 | 13.4 |
|  | 2-Methylimidazole |  |  |  |  |  |
|  | ${ }^{15} \mathrm{~N}(1)$ | ${ }^{13} \mathrm{C}(2)$ | ${ }^{15} \mathrm{~N}(3)$ | ${ }^{13} \mathrm{C}(4)$ | ${ }^{13} \mathrm{C}(5)$ | ${ }^{13} \mathrm{C}(6)$ |
| $A_{0}^{\prime}$ (MHz) | 8814.6319(18) | 8992.8302(11) | 8792.1062(42) | 8915.8214(17) | 8926.2872(14) | 8992.7498(14) |
| $B_{0}^{\prime}$ (MHz) | 3600.6798(11) | $3590.29885(71)$ | 3600.9490(24) | $3552.2344(10)$ | 3548.18883(98) | 3487.68163(79) |
| $C_{0}^{\prime}$ (MHz) | 2589.6296(10) | 2599.38473(67) | 2587.8671(18) | 2572.97540(96) | 2571.75208(87) | 2545.13613(77) |
| $N^{\text {c }}$ | 18 | 48 | 7 | 46 | 43 | 47 |
| $\sigma_{\text {r.m. }}{ }^{\text {d }}$ (kHz) | 11.8 | 11.5 | 15.1 | 17.4 | 13.5 | 13.4 |

${ }^{a}$ Numbers in parentheses are standard deviations in units of the last significant figure.
${ }^{\mathrm{b}}$ Each column presents the data for a different isotopologue. The column header indicates the identity of the atom substituted into the parent isotopologue where the atom numbering is that shown in Figure 1. For example, the results shown in the first column are those for isotopologues where ${ }^{15} \mathrm{~N}$ is present in the $\mathrm{N}(1)$ position. The values of all other parameters are fixed to those determined for the corresponding isomer as shown in Table S3.
${ }^{\text {c }}$ Number of hyperfine components included in the fit.
${ }^{\mathrm{d}}$ Root mean square deviation of the fit.

Table 6.4. Experimentally determined effective rotational constants for the torsional ground state of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of 4- and 5MI.

|  | 4-Methylimidazole |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }^{15} \mathrm{~N}(1)$ | ${ }^{13} \mathrm{C}(2)$ | ${ }^{15} \mathrm{~N}(3)$ | ${ }^{13} \mathrm{C}(4)$ | ${ }^{13} \mathrm{C}(5)$ | ${ }^{13} \mathrm{C}(6)$ |
| $A_{0}^{\prime}$ (MHz) | 8916.089(14) ${ }^{\text {a,b }}$ | 8885.3930(18) | 8777.7047(39) | 8971.9848(21) | 8775.4655(16) | 8971.8365(14) |
| $B_{0}^{\prime}$ (MHz) | 3459.545(11) | 3467.6755(11) | 3508.2093(21) | 3496.8472(14) | 3507.8617(10) | $3396.53395(80)$ |
| $C_{0}^{\prime}(\mathrm{MHz})$ | 2531.7195(67) | 2532.96827(81) | 2545.6403(17) | 2555.58829(99) | 2545.16947(73) | 2501.55747(70) |
| $N^{\text {c }}$ | 7 | 30 | 9 | 24 | 24 | 23 |
| $\sigma_{\text {r.m. }}{ }^{\text {d }}$ (kHz) | 18.7 | 13.1 | 14.8 | 12.9 | 9.7 | 8 |
| 5-Methylimidazole |  |  |  |  |  |  |
|  | ${ }^{15} \mathrm{~N}(1)$ | ${ }^{13} \mathrm{C}(2)$ | ${ }^{15} \mathrm{~N}(3)$ | ${ }^{13} \mathrm{C}(4)$ | ${ }^{13} \mathrm{C}(5)$ | ${ }^{13} \mathrm{C}(6)$ |
| $A_{0}^{\prime}$ (MHz) | - | 8989.8304(58) | - | 8859.5298(18) | 9061.7295(39) | 9057.0010(34) |
| $B_{0}^{\prime}$ (MHz) | - | 3426.5369(17) | - | 3471.4965(11) | 3461.1415(30) | 3360.8398(10) |
| $C_{0}^{\prime}(\mathrm{MHz})$ | - | 2519.94907(90) | - | 2532.97377(84) | 2542.8130(24) | 2489.41542(95) |
| $N^{\text {c }}$ | - | 9 | - | 8 | 6 | 9 |
|  | - | 8.2 | - | 6.8 | 9.2 | 10.5 |

${ }^{\mathrm{a}}$ Numbers in parentheses are standard deviations in units of the last significant figure.
${ }^{\mathrm{b}}$ Each column presents the data for a different isotopologue. The column header indicates the identity of the atom substituted into the parent isotopologue where the atom numbering is that shown in Figure 1. For example, the results shown in the first column are those for isotopologues where ${ }^{15} \mathrm{~N}$ is present in the $\mathrm{N}(1)$ position. The values of all other parameters are fixed to those determined for the corresponding isomer as shown in Table S3.
${ }^{\text {c }}$ Number of hyperfine components included in the fit.
${ }^{d}$ Root mean square deviation of the fit.

### 6.6 Molecular Geometry

A first insight into the geometry of each MI isomer is obtained in terms of planar (second) moments. The relative equations have been discussed in previous chapters. The planar moment assigned to the $c$-inertial axis, $P_{c c}$, was evaluated for a range of molecules by R. K. Bohn et al. ${ }^{43}$ It was shown that for a relatively small and rigid, singly-methylated molecule, where the only contributions to the out-of-plane mass are due to the protons on the $\mathrm{CH}_{3}$ group, results in a value of $P_{c c}$ of approximately $1.6 \mathrm{u} \AA^{2}$. For $N-, 2-, 4$ - and 5-MI, $P_{\mathrm{cc}}$ was calculated using the experimentally determined rotational constants summarized in table 6.2 for each isomer by means of equation 2.72 .

The $P_{c c}^{\prime}$ values determined for $N$-, 2-, 4- and 5-MI are 1.50055(3), 1.26843(3), 1.54873(1) and $1.57117(2) \mathrm{u} \AA^{2}$, respectively. In the case of 4 - and $5-\mathrm{MI}$ those values are sufficiently close to the expected $1.6 \mathrm{u} \AA^{2}$ value for a planar and rigid molecule where the only out-ofplane contributions are coming from the $\mathrm{CH}_{3}$ protons. Evidently, this is not the case for N - and 2-MI where these values significantly deviate from the expected value. This observation is consistent with the proposal that internal rotation of a $\mathrm{CH}_{3}$ group may affect the effective rotational constants of a rotating molecule (obtained by fitting of $A$-state transitions as described in section 6.5). In section 6.7, it will be shown how the $V_{3}$ barrier to internal rotation for $\mathrm{CH}_{3}$ may be evaluated by means of the inertial defect $\Delta_{0}^{\prime}$.

Determination of atomic coordinates of all carbon and nitrogen atoms in $N$-, 2- and 4-MI and all carbon atoms in 5-MI was performed using Kraitchman's method ${ }^{44,45}\left(r_{s}\right)$. As described in chapter 2, section 2.10.2, the method determines the position of an atom based on shifts in rotational constants caused by isotopic substitution of that atom. Atomic coordinates of C and N atoms in N -, 2-, 4 - and $5-\mathrm{MI}$ are displayed in table 6.5 alongside their Costain errors ${ }^{46}$ in parentheses. The method only generates the magnitude of the relative coordinates so for that reason signs were implied by the DFT calculated coordinates of the optimized structures. Given that only an $A$-states fit could be performed on the ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues, the effective rotational constants were used to calculate the atomic coordinates without affecting the precision and quality of these coordinates. It is obvious in table 6.5 that the resulting $r_{s}$ coordinates are in good agreement with the DFT $r_{e}$ coordinates calculated for each isomer. Considering that an equilibrium structure is calculated by DFT whilst the $r_{s}$ method determines the zero-point structure, some discrepancies are observed between theory and experiment, e.g. C(4) in 5-MI. Imaginary
coordinates are obtained for some atoms, i.e. $\mathrm{C}(5)$ of $5-\mathrm{MI}$, which lie close to an inertial axis or the center of mass suggesting that the magnitude of these coordinates is very small and they were therefore set to zero.

Atomic coordinates were evaluated with the program EVAL, also available from the PROSPE website, ${ }^{47}$ and bond lengths between the heavy atoms in $N-, 2$-, 4 - and 5-MI were determined. These are summarized in table 6.6 and compared against values obtained for unmethylated imidazole. Data from X-ray ${ }^{48,49}$ and neutron ${ }^{50}$ diffraction experiments are available for imidazole and they are displayed alongside its $r_{0}$ and $r_{s}$ bond lengths. A crystal structure ${ }^{51}$ is only available for $2-\mathrm{MI}$ and the results are consistent with the $r_{s}$ structure determined here through microwave spectroscopy. The differences between the structure obtained through X-ray crystallography and the gas phase structure mainly arise due to lattice and crystal packing effects in the former. The $\mathrm{C}(2)-\mathrm{N}(3), \mathrm{N}(3)-\mathrm{C}(4), \mathrm{C}(4)-$ $\mathrm{C}(5)$ and $\mathrm{C}(2)-\mathrm{C}(6)$ bonds in the gas phase structure are elongated by an average value of approximately $0.018 \AA$ whilst the $\mathrm{N}(1)-\mathrm{C}(2)$ bond is approximately $0.03 \AA$ shorter.

Table 6.5. Experimentally determined $\left(r_{s}\right)$ and calculated $\left(r_{e}\right)$ atomic coordinates of C and N atoms in $N$-, 2-, $4-$, and $5-\mathrm{MI}$ on the $a$ - and $b$ axes assuming a planar geometry around the heavy atoms $(|c|=0)$.

|  |  | N(1) |  | C(2) |  | N(3) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $a$ | $b$ | $a$ | $b$ | $a$ | $b$ |
| $N-\mathrm{MI}$ | $r_{\text {s }} / \AA$ | $-0.6689(22)^{\text {a }}$ | $0.0{ }^{\text {b }}$ | 0.145(10) | -1.0635(14) | 1.4337(11) | 0.7094(23) |
|  | $r_{\mathrm{e}} / \AA$ | -0.6716 | -0.0105 | 0.1295 | -1.1303 | 1.4278 | 0.7083 |
| 2-MI | $r_{\text {s }} / \AA$ | 0.112(13) | -1.0738(14) | -0.6496(23) | $0.0{ }^{\text {b }}$ | 0.045(34) | 1.1411(13) |
|  | $r_{\mathrm{e}} / \AA$ | 0.1314 | -1.0695 | -0.6595 | 0.0457 | 0.0791 | 1.1324 |
| 4-MI | $r_{\text {s }} / \AA$ | 1.4323(11) | -0.6051(25) | 1.3003(12) | 0.7509(20) | 0.051(29) | 1.1248(13) |
|  | $r_{\mathrm{e}} / \AA$ | 1.4227 | -0.6046 | 1.3036 | 0.7510 | 0.0459 | 1.1192 |
| 5-MI | $r_{\mathrm{s}} / \AA$ | - | - | -1.3867(11) | -0.6560(23) | - | - |
|  | $r_{\mathrm{e}} / \AA$ | -0.0855 | $-1.0559$ | -1.3898 | -0.6484 | -1.4789 | 0.6568 |
|  |  | C(4) |  | $\mathrm{C}(5)$ |  | $\mathrm{C}(6)$ |  |
| $N-\mathrm{MI}$ |  | $a$ | $b$ | $a$ | $b$ | $a$ | $b$ |
|  | $r_{\mathrm{s}} / \AA$ | 1.4171(11) | -0.6656(23) | 0.103(15) | -1.1324(13) | -2.1209(7) | $0.0{ }^{\text {b }}$ |
|  | $r_{\mathrm{e}} / \AA$ | 1.4173 | -0.6651 | 0.1295 | $-1.1303$ | -2.1199 | 0.0154 |
| 2-MI | $r_{\mathrm{s}} / \AA$ | $1.3902(11)$ | 0.7071(21) | 1.4481(10) | -0.6578(23) | -2.1448(7) | -0.008(191) |
|  | $r_{\mathrm{e}} / \AA$ | 1.3898 | 0.7084 | 1.4477 | -0.6550 | $-2.1463$ | -0.0053 |
| 4-MI | $r_{s} / \AA$ | -0.6891(22) | $0.0{ }^{\text {b }}$ | 0.130(12) | -1.1279(13) | -2.1865(7) | -0.019(79) |
|  | $r_{\mathrm{e}} / \AA$ | -0.6965 | -0.0448 | 0.1446 | $-1.1253$ | -2.1858 | -0.0197 |
| 5-MI | $r_{\text {s }} / \AA$ | -0.070(22) | 1.1205(13) | 0.6667(23) | $0.0{ }^{\text {b }}$ | 2.20012(68) | 0.029(53) |
|  | $r_{\mathrm{e}} / \AA$ | -0.1792 | 1.1152 | 0.7089 | 0.0731 | 2.1950 | 0.0209 |

${ }^{\text {a }}$ Numbers in parentheses are Costain errors (in units of the last significant figure) calculated as $\delta z=0.0015 /|z| \AA$ where $z$ is the value of the coordinate.
${ }^{\mathrm{b}}$ An imaginary result was obtained so this coordinate is assumed equal to zero.

Table 6.6. Calculated ( $r_{e}$ ) and experimentally determined ( $r_{s}$, X-ray and neutron diffraction) bond lengths between the heavy atoms in imidazole and methylimidazole isomers.

| Structural <br> parameters |  | $\mathrm{N}(1)-\mathrm{C}(2)$ | $\mathrm{C}(2)-\mathrm{N}(3)$ | $\mathrm{N}(3)-\mathrm{C}(4)$ | $\mathrm{C}(4)-\mathrm{C} 5)$ | $\mathrm{C}(5)-\mathrm{N}(1)$ | $\mathrm{X}-\mathrm{C}(6)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N -MI | $r_{s}$ | $1.340(27)$ | $1.336(10)$ | $1.3750(33)$ | $1.394(14)$ | $1.371(28)$ | $1.4518(24)$ |
|  | $r_{e}$ | 1.372 | 1.338 | 1.381 | 1.395 | 1.380 | 1.458 |
| $2-\mathrm{MI}$ | $r_{s}$ | $1.316(58)$ | $1.336(63)$ | $1.414(32)$ | $1.3662(31)$ | $1.400(13)$ | $1.4952(26)$ |
|  | $r_{e}$ | 1.377 | 1.337 | 1.385 | 1.390 | 1.3803 | 1.497 |
| $100 \mathrm{~K}^{a}$ | $X-$ | $1.347(2)$ | $1.327(2)$ | $1.384(2)$ | $1.356(3)$ | $1.370(2)$ | $1.487(2)$ |
|  | ray |  |  |  |  |  |  |
| 4 -MI | $r_{s}$ | $1.3624(32)$ | $1.304(28)$ | $1.367(54)$ | $1.346(54)$ | $1.404(11)$ | $1.4976(26)$ |
|  | $r_{e}$ | 1.372 | 1.334 | 1.387 | 1.394 | 1.383 | 1.500 |
| $5-\mathrm{MI}$ | $r_{s}$ | - | - | - | $1.341(14)$ | - | $1.5337(26)$ |
|  | $r_{e}$ | 1.376 | 1.334 | 1.385 | 1.394 | 1.385 | 1.498 |
| Imidazole ${ }^{\mathrm{b}}$ | $r_{0}$ | 1.3704 | 1.3164 | 1.3875 | 1.3676 | 1.3788 | - |
|  | $r_{s}$ | 1.3643 | 1.3135 | 1.3822 | 1.3638 | 1.3774 | - |
| $123 K^{c}$ | $X-$ | 1.349 | 1.326 | 1.378 | 1.358 | 1.369 | - |
| $293 K^{d}$ | ray | 1.337 | 1.311 | 1.381 | 1.311 | 1.373 | - |
| $103 K^{e}$ | n-diff | $1.347(1)$ | $1.323(1)$ | $1.375(1)$ | $1.368(1)$ | $1.369(1)$ | - |
| $293 K^{e}$ |  | $1.358(1)$ | $1.333(1)$ | $1.389(1)$ | $1.378(1)$ | $1.381(1)$ | - |

${ }^{\mathrm{a}}$ Reference $51 ;{ }^{\mathrm{b}}$ Reference 2; ${ }^{\mathrm{c}}$ Reference 49; ${ }^{\mathrm{d}}$ Reference 48; ${ }^{\mathrm{e}}$ Reference 50

### 6.7 Internal Rotation of $\mathrm{CH}_{3}$ - Global Fit of $A$ - and $E$-States

Internal rotation has been explored in numerous aromatic molecules containing one or more $\mathrm{CH}_{3}$ groups. ${ }^{12,17,18,21-23,33,39,42,52}$ Internal rotation of a group with 3-fold symmetry is represented by a periodic potential function describing how the potential energy varies with rotating angle. As we saw in chapter 2 , section 2.9 , this can be generally described by the relationship Eq.2.61.

It was shown that the $V_{3}$ barrier to internal rotation in isomers of methylthiazole ${ }^{18,21,22}$ (MT) and methyloxazole ${ }^{23}(\mathrm{MO})$ varies significantly depending on the position where the $\mathrm{CH}_{3}$ group substitutes. $V_{3}$ barriers of $34.9,358$ and $332 \mathrm{~cm}^{-1}$ were reported for each of 2-, 4- and 5-MT. Likewise, the $V_{3}$ barriers in 2-, 4- and 5-MO were determined to be 251, 428 and $478 \mathrm{~cm}^{-1}$, respectively. Another outstanding example of varying $V_{3}$ barrier with substitution position is observed for the seven isomers of methylindole ${ }^{53}$ (MIN), 1-, 2-, 3-, 4-, 5-, 6- and 7-MIN (the numbering was decided by the authors), with values varying from 121 to 426 $\mathrm{cm}^{-1}$.

The $V_{3}$ barriers to internal rotation in $N$-, 2-, 4- and $5-\mathrm{MI}$ were calculated with DFT methods as described in section 6.3. The calculated barriers are 190, 115, 295 and $377 \mathrm{~cm}^{-}$ ${ }^{1}$ for each isomer, respectively, suggesting a correlation between barrier height and position of $\mathrm{CH}_{3}$ substitution. Potential energy curves with the relative $V_{3}$ barriers are shown in figure 6.7. In this section, the PAM (theory section 2.9.1) was initially employed to


Figure 6.7. Potential energy surfaces of the relative dihedral angles describing internal rotation of the $\mathrm{CH}_{3}$ in $N-, 2-, 4$ - and $5-\mathrm{MI}$.
estimate the $V_{3}$ barrier to internal rotation for each MI isomer. Given the limitations of the PAM, a complete analysis and a global fit considering both $A$ - and $E$-states is performed using the IAM (theory section 2.9.2) as implemented in the program XIAM. ${ }^{54}$

N -, 2-, 4-, and 5-MI fulfill the requirements explained in chapter 2, section 2.9.1 and it is possible to approach the $V_{3}$ barriers in each one of them using PAM. To summarize, those requirements are that the local $\mathrm{C}_{3}$ axis of the threes-fold $\mathrm{CH}_{3}$ group is co-linear or almost co-linear with the $a$-inertial axis of the molecule. Also, out-of-plane contributions to the inertial defect $\Delta_{0}$ are negligible at the zero-point and the value of $\Delta_{0}$ primarily arises from the $\mathrm{CH}_{3}$ protons.

Examining figure 6.1 where the optimized equilibrium geometries of $N$-, 2-, 4- and $5-\mathrm{MI}$ are shown, it is apparent that the $a$-axis is almost co-linear with the $\mathrm{N}-\mathrm{CH}_{3}$ or $\mathrm{C}-\mathrm{CH}_{3}$ bond. This is also supported by the $r_{s}$ coordinates determined in section 6.6. As expected for small, rigid, aromatic molecules, contributions of out-of-plane vibrations to the inertial defect $\Delta_{0}$ are negligible at the zero-point and the value of $\Delta_{0}$ mainly arises from the $\mathrm{CH}_{3}$ protons. Within the PAM, there are two limiting cases; i. where the $\mathrm{CH}_{3}$ group undergoes unhindered internal rotation about its $\mathrm{C}_{3}$ axis or ii. the $\mathrm{CH}_{3}$ group is essentially rigid with two out-of-plane protons, resulting in the molecule behaving as a rigid-rotor. It has been shown ${ }^{18}$ that in the first case of unhindered internal rotation, the $A_{0}^{\prime}$ rotational constant can exceed that expected for a molecule with a rigid $\mathrm{CH}_{3}$ group by approximately 187 MHz . The inertial defect of the molecule relies exclusively on the rest of the molecular skeleton and the $\mathrm{CH}_{3}$ does not contribute to it. In the latter case of essentially rigid behavior, differences between effective rotational constants and rigid rotor constants are expected to be much smaller (approaching zero) and the inertial defect $\Delta_{0}$ to have a value of approximately $-3.2 \mathrm{u} \AA^{2}$. On this basis, the effective rotational constants $A_{0}^{\prime}, B_{0}^{\prime}$ and $C_{0}^{\prime}$ determined in section 6.5 can be compared against the rotational constants expected for a rigid rotor, denoted as $A_{R R}, B_{R R}$ and $C_{R R}$, to estimate the $V_{3}$ barrier to internal rotation in MI isomers.

STRFIT ${ }^{55}$ was used to calculate $A_{R R}, B_{R R}$ and $C_{R R}$. For the initial $z$-matrix, the $r_{s}$ geometry of the C and N atoms in each of N -, 2-, and 4-MI were used. The positions of the H -atoms were implied by the DFT calculated geometries at the B3LYP(D3BJ)/aug-cc-pVTZ level. In the case of $5-\mathrm{MI}$ where no isotopic data are available for the N atoms, the $r_{s}$ geometry of unsubstituted imidazole ${ }^{2}$ was used, assuming that the imidazole subunit remains
unchanged upon methylation. For all isomers, it was further assumed that in the $\mathrm{CH}_{3}$ group the $r(C-H)$ distance is $1.09 \AA$ and the $\angle(C-C-H)$ angle $110^{\circ}$. Based on the expression;

$$
\begin{equation*}
F_{\alpha}=\frac{h}{8 \pi^{2} I_{\alpha}} \tag{Eq.6.1}
\end{equation*}
$$

where $F_{\alpha}$ is the standard rotational constant for an $\mathrm{sp}^{3}$ hybridized methyl top, $h$ is the Planck constant, it follows that the moment of inertia of the $\mathrm{CH}_{3}$ top is $I_{\alpha} \cong 3.2 \mathrm{u} \AA^{2}$.

The rotational constants resulting when assuming rigid rotor behavior are summarized in table 6.7 alongside the effective rotational constants of $N$-, 2-, 4- and 5-MI. The inertial defect $\Delta_{0}^{\prime}$ is calculated by means of equation 2.73 using the effective rotational constants. For 2-MI, the $A_{0}^{\prime}$ rotational constant exceeds $A_{R R}$ by approximately 100 MHz whilst the difference between $B_{0}^{\prime}$ and $C_{0}^{\prime}$ and $B_{R R}$ and $C_{R R}$, respectively, is significantly lower. This behavior is also observed for $N$-MI and, to a lesser extent, for 4 - and $5-\mathrm{MI}$. At a first approximation and whilst considering these observations, it is expected that the lowest $V_{3}$ barrier will be found for 2-MI, followed by $N-\mathrm{MI}, 4-\mathrm{MI}$ and $5-\mathrm{MI}$, consistent with the DFT calculated barriers.

Table 6.7. Effective rotational constants compared to rigid rotor rotational constants.

|  | $\mathrm{N}^{2} \mathrm{MI}^{\mathrm{a}}$ | $2-\mathrm{MI}^{\mathrm{a}}$ | $4-\mathrm{MI}^{\mathrm{a}}$ | $5-\mathrm{MI}^{\mathrm{a}, \mathrm{b}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{0}^{\prime}(\mathrm{MHz})$ | $9194.5817(17)^{\mathrm{c}}$ | $8992.75911(97)$ | $8971.89077(89)$ | $9057.12512(100)$ |
| $A_{R R}(\mathrm{MHz})$ | 9153.91 | 8907.60 | 9002.00 | 9023.03 |
| $B_{0}^{\prime}(\mathrm{MHz})$ | $3609.78192(71)$ | $3600.99984(38)$ | $3508.27356(31)$ | $3471.61329(36)$ |
| $B_{R R}(\mathrm{MHz})$ | 3626.68 | 3616.00 | 3515.11 | 3468.67 |
| $C_{0}^{\prime}(\mathrm{MHz})$ | $2632.63930(68)$ | $2604.96676(32)$ | $2561.66742(25)$ | $2549.43964(33)$ |
| $C_{R R}(\mathrm{MHz})$ | 2640.99 | 2614.51 | 2569.10 | 2545.88 |
| $\Delta_{0}^{\prime} / \mathrm{u} \AA^{2}$ | $-3.02267(6)^{\mathrm{d}}$ | $-2.536524(29)$ | $-3.097382(24)$ | $-3.142257(30)$ |

[^5]${ }^{\mathrm{b}}$ Rigid rotor rotational constants defined as in footnote (a) while making the additional assumptions that $r(\mathrm{~N}(1)-\mathrm{C}(2)), r(\mathrm{~N}(3)-\mathrm{C}(2)), r(\mathrm{~N}(3)-\mathrm{C}(4))$ and angles internal to the imidazole ring are equal to $r_{s}$ results for imidazole.
${ }^{\text {c }}$ Effective rotational constants $\left(A_{0}^{\prime}, B_{0}^{\prime}\right.$ and $\left.C_{0}^{\prime}\right)$ determined by fitting to $A$-species transitions (full details of fits including the values of centrifugal distortion and hyperfine constants are provided in Table 6.2).
${ }^{\mathrm{d}}$ The assumption of rigid rotor behavior leads to $\Delta_{0}^{\prime} \cong 3.2 \mathrm{u} \AA^{2}$ for each isomer.

The procedure followed to estimate $V_{3}$ barriers with PAM will only be described in detail for N - and 2-MI. Within the "high-barrier approximation" described in detail elsewhere ${ }^{18,45}$, higher potential terms are neglected, i.e. $V_{6}=V_{9}=\ldots=0$. Contributions to the $B_{0}^{\prime}$ and $C_{0}^{\prime}$ rotational constants due to the non-zero direction cosine between the $\mathrm{C}_{3}$ axis of the $\mathrm{CH}_{3}$ group and the $b$ - and $c$-axis are also neglected. The effective Hamiltonian appropriate for the ground torsional state $(A$-states, $\mathrm{m}=0)$ can be expressed in terms of Herschbach's barrier dependent perturbation coefficient ${ }^{45}, W_{v \sigma}^{(n)}$, and is described by the following relationship;

$$
\begin{equation*}
\widehat{H}_{v=0, \sigma=0}=\left(A+F \rho_{a}^{2} W_{00}^{(2)}\right) \hat{P}_{a}^{2}+B \hat{P}_{b}^{2}+C \hat{P}_{c}^{2} \tag{Eq.6.2}
\end{equation*}
$$

where $\hat{P}_{a}, \hat{P}_{b}$ and $\hat{P}_{c}$ are the rotational angular momentum operators along the $a$-, $b$ - and $c$ axes, respectively. $A, B$ and $C$ are the rotational constants for a generic, rigid molecule, the standard rotational constant for an $\mathrm{sp}^{3}$ hybridized methyl top $F=h /\left[8 \pi^{2} I_{\alpha}\left(1-\rho_{\alpha}\right)\right]$, $\rho_{\alpha}=I_{\alpha} / I_{a}$, and $W_{00}^{(2)}$ is Herschbach's barrier dependent perturbation coefficient. $W_{00}^{(2)}$ depends on the reduced barrier $s=4 V_{3} / 9 F$, according to Microwave Molecular Spectra ${ }^{45}$ and the tables by Hayashi and Pierce ${ }^{56}$. The perturbation coefficient can be expressed in terms of moments of inertia and inertial defect;

$$
\begin{equation*}
W_{00}^{(2)}=\left(1+\frac{\Delta^{\prime}}{I_{\alpha}}\right)\left(1+\frac{\Delta^{\prime}}{I_{a}^{\prime}}\right) \tag{Eq.6.3}
\end{equation*}
$$

where $\Delta^{\prime}$ is the effective inertial defect, $I_{\alpha}$ is the moment of inertia of the $\mathrm{sp}^{3}$ hybridized $\mathrm{CH}_{3}$ group and $I_{a}^{\prime}$ is the effective moment of inertia along the $a$-inertial axis of the molecule.

In-plane vibrational contributions to the inertial defect of the imidazole subunit at the zeropoint are small resulting in a value of $\Delta_{0}=+0.029 \mathrm{u} \AA^{2}$. These were subtracted from $\Delta_{0}^{\prime}$
shown in table 6.7. On this basis, it is calculated that $W_{00}^{(2)}$ for $N$-MI and 2-MI is approximately 0.042 and 0.182 (unitless quantities), respectively. With reference to reduced barrier tables in Microwave Molecular Spectra ${ }^{45}$ and the work of Hayashi and Pierce ${ }^{56}$, these values correlate to values of reduced barriers $s$ of 17.1 and 10.2. It is estimated that $V_{3} \cong 215$ and $128 \mathrm{~cm}^{-1}$ for $N$ - and 2-MI, respectively. These values are sensitive to assumptions made for the molecules, for example, if $I_{\alpha}=3.10 \mathrm{u} \AA^{2}$ is assumed, then $V_{3} \cong 141 \mathrm{~cm}^{-1}$ for 2-MI. Relatively good agreement is also observed between these values and the DFT calculated ones ( 190 and $115 \mathrm{~cm}^{-1}$ ).

It should be noted that this procedure is appropriate for molecules with low barriers where $\left|\frac{\Delta^{\prime}}{I_{\alpha}}\right| \ll 1$ and systems where vibrational contributions (and/or contributions arising by mass distribution directly) to $\Delta^{\prime}$ are small. For these reasons, PAM does not provide a reliable measure of the $V_{3}$ barrier height particularly for 4 - and 5-MI where the barriers are intermediate to high, as it will be discussed later. For the same reasons, PAM was not used in the process of determining the $V_{3}$ barriers in the weakly-bound complexes of MI isomers with $\mathrm{H}_{2} \mathrm{O}$ in chapter 7 .

The IAM was used to produce global fits with inclusion of both ground and first excited torsional $A$ - and $E$-states $(m=0, m= \pm 1)$. The $A$ - and $E$-states for a given transition in the spectrum of an asymmetric molecule share the same set of quantum numbers $J, K_{-1}$ and $K_{+1}$. Considering the DFT calculated barrier heights, it is expected that the splitting between the two states will be in the range of 500 kHz to 10 MHz , with the lowest barrier accounting for the largest splitting. The global fits produce experimental values of rotational constants $A_{0}, B_{0}$ and $C_{0}$, and centrifugal distortion constants $D_{J}, D_{J K}, D_{K}, d_{1}$ and $d_{2}$, as appropriate. Parameters describing the internal rotation in each MI isomer include $F_{0}$, which was defined earlier as the rotational constants for and $\mathrm{sp}^{3}$ hybridized $\mathrm{CH}_{3}$ internal rotor, $V_{3}$ barriers to internal rotation and fitted angles between the local $\mathrm{C}_{3}$ axis of the $\mathrm{CH}_{3}$ group and the $a$-, $b$ - and $c$-inertial axes of the molecules denoted as $\angle(i, a), \angle(i, b)$ and $\angle(i, c)$.

In order to perform a fit with XIAM, an input file is required. The effective rotational constants and centrifugal distortion constants were used as the starting points for the global fits of transitions yielded by each isomer. The initial values of the polar coordinates of the internal rotation axis in the principal axes system, $\delta$ and $\varepsilon$, are deduced from the DFT
geometries. A definition of these coordinates was provided in chapter 2, section 2.9.2. The DFT calculated $V_{3}$ barriers are also used as initial values. The line-list of transitions consists of the $A$-state transitions, initially fitted with Pgopher, along with an identified $E$ state transition frequency. Identifying the correct $E$-state transition frequencies through spectral inspection can be challenging, however, the two states will typically exhibit very similar hyperfine structure and signal intensity due to statistical weights. Given that XIAM is not coded to treat internal rotation in a molecule with two quadrupolar nuclei, it was necessary to neglect the hyperfine structure and exclude the quantum numbers $F_{1}$ and $F$ from the line-list. For this reason, the transition frequency centers were estimated, and iterative corrections of those center-frequencies were made after a few fit cycles and after inclusion of more $E$-state transitions. The precision of the fits is greatly underestimated by this procedure, however, the fitted $V_{3}$ barriers are in excellent agreement with their calculated values. The spectra were examined for further torsional excited states with $|m|>1$, however, no transitions were identified that might reasonably be related to such states. Considering the low rotational temperature of the supersonic expansion, it is expected that states with $|m|>1$ will not be populated.

Watson's S-reduced Hamiltonian ${ }^{41}$ with the appropriate internal rotation terms as implemented in XIAM was used and the results of the global fits are summarized in table 6.8. For each of $N$-, 2-, 4- and $5-\mathrm{MI}$, the fitted values of $\angle(i, a)$ imply that the $a$-axis is essentially aligned with the $\mathrm{C}_{3}$ axis ( 0 or $180^{\circ}$ ) of the $\mathrm{C}-\mathrm{CH}_{3}$ (or $\mathrm{N}-\mathrm{CH}_{3}$ ) bond. The planarity of the imidazole subunit is further supported by the fitted values of the $\angle(i, c)$ angles which are very close to $90^{\circ}$. The fitted $V_{3}$ barriers are 185.104(11), 122.7529(38), 317.20 (14) and 386.001 (19) $\mathrm{cm}^{-1}$ for $N-, 2-, 4$ - and $5-\mathrm{MI}$, respectively. These values are consistent with those determined with PAM and in good agreement with the values reported by B. Harris ${ }^{24}$ for $4-$ and $5-\mathrm{MI}$. A fitted value for $F_{0}$ is obtained for $N$-, 2-, and 4MI, 157.9291 (88), 157.6901 (44) and $157.784(60) \mathrm{GHz}$, respectively, which correspond to an approximate value of $I_{\alpha} \cong 3.20 \AA$. It was not possible to determine $F_{0}$ for 5 -MI so during the fits it was kept fixed to 157.68 GHz .

Table 6.8. Results of "global" fits of spectroscopic parameters to $A$ and $E$-species transition frequencies to determine rotational constants and internal rotation parameters for $N$-, 2-, 4 - and $5-\mathrm{MI}$.

|  | $N-\mathrm{MI}$ | $2-\mathrm{MI}$ | $4-\mathrm{MI}$ | $5-\mathrm{MI}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{A}_{\mathbf{0}}^{\prime}(\mathrm{MHz})$ | $9156.7503(50)^{\mathrm{a}}$ | $8892.9063(26)$ | $8966.7590(10)$ | $9054.9327(15)$ |
| $\boldsymbol{B}_{\mathbf{0}}^{\prime}(\mathrm{MHz})$ | $3609.9582(16)$ | $3601.19596(95)$ | $3508.41729(51)$ | $3471.74371(51)$ |
| $\boldsymbol{C}_{\mathbf{0}}^{\prime}(\mathrm{MHz})$ | $2632.4462(16)$ | $2604.8287(98)$ | $2561.52449(47)$ | $2549.30663(32)$ |
| $D_{J}(\mathrm{kHz})$ | $0.16(11)$ | $[0.1947(56)]^{\mathrm{b}}$ | $0.288(20)$ | $0.271(11)$ |
| $D_{K}(\mathrm{kHz})$ | $32.07(1.10)$ | $-21.51(45)$ | $7.98(33)$ | $1.76(36)$ |
| $D_{J K}(\mathrm{kHz})$ | $-2.99(14)$ | $7.44(10)$ | $1.566(74)(34)$ | $1.592(58)$ |
| $d_{1}(\mathrm{kHz})$ | $[-0.065776]^{\mathrm{c}}$ | $-0.0764(90)$ | $-0.0719(47)$ | $-0.0586(46)$ |
| $d_{2}(\mathrm{kHz})$ | $[-0.00108]^{\mathrm{c}}$ | $[0.00512]^{\mathrm{c}}$ | $-0.0146(23)$ | $-0.0183(20)$ |
| $\boldsymbol{V}_{\mathbf{3}}\left(\mathrm{cm}^{-1}\right)$ | $185.104(11)$ | $122.7529(38)$ | $317.20(14)$ | $386.001(19)$ |
| $\boldsymbol{F}_{\mathbf{0}}(\mathrm{GHz})$ | $157.9291(88)$ | $157.6901(44)$ | $157.784(60)$ | $[157.68]$ |
| $\angle(\boldsymbol{i}, \boldsymbol{a})\left({ }^{\circ}\right)^{\mathrm{d}}$ | $0.33(20)$ | $176.0705(94)$ | $187.79(12)$ | $187.539(66)$ |
| $\angle(\boldsymbol{i}, \boldsymbol{b})\left(^{\circ}\right)^{\mathrm{d}}$ | $90.00(32)$ | $86.25(11)$ | $96.37(16)$ | $84.93(15)$ |
| $\angle(\boldsymbol{i}, \boldsymbol{c})\left(^{\circ}\right)^{\mathrm{d}}$ | $90.33(61)$ | $88.8240(84)$ | $85.53(15)$ | $84.44(14)$ |
| $\boldsymbol{\kappa}^{\mathrm{e}}$ | -0.70 | -0.68 | -0.70 | -0.72 |
| $\Delta_{\mathbf{0}}\left(\mathrm{u} \AA^{2}\right)$ | $-3.20701(14)$ | $-3.1497(7)$ | $-3.1278(4)$ | $-3.140029(34)$ |
| $\boldsymbol{P}_{\boldsymbol{c c}}\left(\mathrm{u} \AA^{2}\right)$ | $1.60351(7)$ | $1.5748(4)$ | $1.556392(21)$ | $1.570015(17)$ |
| $\sigma_{\text {RMS }}(\mathrm{kHz})^{\mathrm{f}}$ | 8.9 | 13.8 | 4.5 | 3.4 |
| $N^{\mathrm{f}}$ | 32 | 46 | 47 | 44 |

${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figure.; ${ }^{b}$ Fixed to $D_{J}$ determined by fitting to transitions of the $A$ species of 2-MI (see Table 6.2).; ${ }^{\text {c }}$ Fixed to DFT-calculated results.; ${ }^{\text {d }}$ Angle between the three-fold axis of the methyl group ( $i$ ) and the respective inertial axes $(a, b, c)$.; ${ }^{e}$ Ray's asymmetry parameter, $\kappa$.; ${ }^{\mathrm{f}}$ Number of transitions included in the fit and root mean square deviation of the fit.

### 6.8 Nuclear Quadrupole Coupling Constants (NQCC)

The diagonal nuclear quadrupole coupling terms $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ were calculated with QDIAG for $N$-, 2-, 4-, and 5-MI. The results are summarized in table 6.9 alongside the values for unsubstituted imidazole ${ }^{2}$, and 2- and 4 -iodoimidazole ${ }^{57}$. The axes orientation on N1 and N3 is common across all molecules and a detailed description was given in chapter 5 for the case of the imidazole-water complex. For N1, the $z$-axis is almost parallel to the $c$-axis resulting in $\chi_{c c}(N 1) \approx \chi_{z z}(N 1)$ whilst for N 3 this is permuted to the $y$-axis so it holds $\chi_{c c}(\mathrm{~N} 3) \approx \chi_{y y}(\mathrm{~N} 3)$. The off-diagonal component $\chi_{a b}$ was calculated at the B3LYP(D3BJ)/aug-cc-pVTZ level for each isomer and was given a $25 \%$ uncertainty.

Within the limitations of our analysis, no significant changes are observed in the electronic environment of N 1 and N 3 of imidazole upon substitution with a $\mathrm{CH}_{3}$ group or an I atom. The sign and the magnitude of the diagonalized nuclear quadrupole coupling constants are consistent across each molecule. The uncertainty in $\chi_{x x}$ and $\chi_{y y}$ in N1 is relatively large, in the second or third significant figure, so it is not possible to perform meaningful comparisons for these components. Likewise, $\chi_{x x}$ and $\chi_{z z}$ in N3 carry relatively large uncertainties.

Table 6.9. Diagonalization of nuclear quadrupole coupling terms to determine $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$.

|  | $N-\mathrm{MI}$ | 2-MI | 4-MI | 5-MI | Imidazole | 2-iodoim | 4-iodoim |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\chi_{x x}(\mathrm{~N} 1)(\mathrm{MHz})$ | $0.943(10)$ | $1.225(28)$ | $1.160(21)$ | $1.1512(86)$ | $0.890(52)$ | $0.98(26)$ | $1.386(23)$ |
| $\chi_{y y}(\mathrm{~N} 1)(\mathrm{MHz})$ | $1.7427(64)$ | $1.514(29)$ | $1.451(20)$ | $1.514(13)$ | $1.633(58)$ | $1.77(26)$ | $1.136(21)$ |
| $\chi_{z z}(\mathrm{~N} 1)(\mathrm{MHz})$ | $-2.6860(49)$ | $-2.7395(58)$ | $-2.6114(50)$ | $-2.6650(60)$ | $-2.524(12)$ | $-2.7561(47)$ | $-2.5223(86)$ |
| $\eta^{a}$ | $0.294(31)$ | $0.2977(44)$ | $0.106(21)$ | $0.111(81)$ | $0.1361(59)$ | $0.29(13)$ | $0.099(12)$ |
| $\chi_{x x}(\mathrm{~N} 3)(\mathrm{MHz})$ | $2.04(69)$ | $1.97(26)$ | $1.94(41)$ | $2.000(71)$ | $1.835(23)$ | $2.0097(47)$ | $1.75(23)$ |
| $\chi_{y y}(\mathrm{~N} 3)(\mathrm{MHz})$ | $2.1419(27)$ | $2.0124(59)$ | $2.0933(49)$ | $2.2563(66)$ | $2.278(24)$ | $2.17(14)$ | $2.0051(86)$ |
| $\chi_{z z}(\mathrm{~N} 3)(\mathrm{MHz})$ | $-4.18(69)$ | $-3.98(27)$ | $-4.0360(31)$ | $-4.25(71)$ | $-4.113(34)$ | $-4.18(14)$ | $-3.76(23)$ |
| $\eta$ | $0.0244(80)$ | $0.011(17)$ | $0.011(65)$ | $0.04(10)$ | $0.060(20)$ | $0.038(34)$ | $0.068(61)$ |

${ }^{\text {a }}$ The asymmetry parameter $\boldsymbol{\eta}=\frac{\chi_{x x}-\chi_{y y}}{\chi_{z z}}$

### 6.9 Discussion

The $V_{3}$ barriers to internal rotation are compared across the series of isomers of methylimidazole (MI) (this work), methylpyrrole ${ }^{38,39}$ (MP), methylthiazole ${ }^{18,21,22}$ (MT), methyloxazole ${ }^{23}$ (MO) and methylindole ${ }^{53}$ (MIN) and summarized in table 6.10. A graphical outlook on the $V_{3}$ barriers across a wide range of methylated $N$-heteroaromatic molecules is given in Figure 6.8. It is immediately apparent that the barrier height greatly depends on the substitution position of the $\mathrm{CH}_{3}$ group across each ring. For the isomers of MI, MT and MO, the broad trend in barrier height is that the lowest $V_{3}$ value is observed for each of 2-MI, 2-MT and 2-MO. Likewise, the highest $V_{3}$ barrier in each of the series is observed for $5-\mathrm{MI}, 5-\mathrm{MT}$ and $5-\mathrm{MO}$ with $4-\mathrm{MI}, 4-\mathrm{MT}$ and $4-\mathrm{MO}$ being the intermediate case. The heteroatoms appear to have a great influence on the barrier height. For example, $V_{3}$ barrier for 2-MT is $35 \mathrm{~cm}^{-1}$ whilst for 2-MI and 2-MO that value becomes 123 and 252 $\mathrm{cm}^{-1}$, respectively. Significant differences are also observed between MI and MP isomers. The $V_{3}$ barrier in $N$-MI is $186 \mathrm{~cm}^{-1}$ whilst in $N$-MP this value decreases by a factor of three. Comparing 2-MI and 2-MP, the $V_{3}$ barrier of the latter is approximately twice that of the former.

In molecules where a highly symmetric environment is observed around the $\mathrm{CH}_{3}$ group, like in toluene and $N$-MP, only a low $V_{6}$ barrier is determined. Lowering the symmetry to a $C_{s}$ point-group like in 2-MP, results in a hindered $V_{3}$ potential arising from steric and electronic effects. Comparing $N$-MI and $N$-MP, the $V_{3}$ barrier of the latter exceeds that of the former by a factor of three, despite the fact that the local, immediate, chemical environment of two C-H bonds adjacent to the $\mathrm{N}-\mathrm{CH}_{3}$ is the same in both molecules. This suggests that electronic effects induced by the presence of the second heteroatom in N -MI can propagate across the aromatic system and hinder the internal rotation. In each of 2MI, 2-MT and 2-MO which exhibit the lowest $V_{3}$ in each series, two heteroatoms are adjacent to the $\mathrm{C}-\mathrm{CH}_{3}$ bond suggesting that the local environment is more symmetric in comparison to $4-\mathrm{MI}, 4-\mathrm{MT}$ and $4-\mathrm{MO}$ and $5-\mathrm{MI}, 5 \mathrm{MT}$ and $5-\mathrm{MO}$, respectively. Particularly 5-MI, 5-MT and 5-MO exhibit the highest $V_{3}$ barriers and the most asymmetric environment with a heteroatom and a $\mathrm{C}-\mathrm{H}$ bond adjacent to each $\mathrm{C}-\mathrm{CH}_{3}$ in each series. Similar arguments were put in place in the cases of 2-MT and 2-MP. These interpretations, however, arise from empirical and intuitive observations so it is not possible to draw generalized conclusions that apply to all aromatic systems.

The effects of steric and electronic interactions were considered by Spangler ${ }^{11}$ who emphasized on how significant effects are observed on the $V_{3}$ barriers when $\pi$-orbitals from aromatic rings interact with $\pi$-like orbitals on the adjacent $\mathrm{CH}_{3}$ group. In cases where high symmetry is present ${ }^{33,38}$ like in toluene and $N$-MP, contributions to the hindering potential that result from overlap between the $\pi$-orbitals and $\pi$-like orbitals are of equal magnitude but opposite sign. A low $V_{6}$ barrier is observed in toluene and $N$-MP. Spangler's model accounts for the differences between $N$-MP and $N$-MI and explains the arrangement of the H atoms of the $\mathrm{CH}_{3}$ with respect to the plane of the two molecules. In $N$-MP, the hindering potential is a six-fold $V_{6}$ barrier meaning the H atoms of the $\mathrm{CH}_{3}$ are staggered with the pyrrole ring. The three-fold $V_{3}$ barrier in N -MI (and the other of the isomers) results in an eclipsed projection of the $\mathrm{CH}_{3}$ protons, with one of them being in the plane of the imidazole ring.

In methylimidazole where the symmetry is reduced, the overlap between $\pi$-orbitals and $\pi$ like orbitals accounts for the differences in the $V_{3}$ barriers to internal rotation between the four isomers. The magnitudes of these barriers are strongly related to the relative populations and energies of these orbitals. Mulliken charges orbital population analyses were performed for each isomer, however, the calculation results are dependent on the level of theory used and are as such inconclusive and unreliable. The $V_{3}$ barrier to internal rotation of the $\mathrm{CH}_{3}$ group in 2-MO and 2-MT were determined to be 252 and $35 \mathrm{~cm}^{-1}$, respectively. It was suggested that a higher degree of aromatic character is associated with the latter which explains the low $V_{3}$ while 2-MO is less aromatic since the barrier is higher. That would imply an intermediate degree of aromatic character associated with 2-MI.

The values of $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ derived from the measured values of $\chi_{a a}$ and $\chi_{b b}-\chi_{c c}$ for N1 and N3 in methylimidazole isomers suggests that methylation of imidazole results in minimal changes in the electronic environment around N1 and N3. However, these values alone, do not provide an insight into the aromaticity of the imidazole ring. It is possible to perform orbital population analyses using the extended Townes-Dailey model ${ }^{58,59}$ as in chapter 4 for PCA; however, this analysis will only give sufficient information regarding the p-orbitals on the N atoms. The accuracy of the analysis may also be compromised by the lack of experimentally determined values for the off-diagonal component $\chi_{a b}$ so it was not performed.

Table 6.10. Barrier to internal rotation in methylated 5 -membered heteroaromatic rings. (from references 16, 39, 21-23, 39)

|  | $V_{3}\left(\mathrm{~cm}^{-1}\right)$ | $F_{0}(\mathrm{GHz})$ |
| :---: | :---: | :---: |
| $N$-MI | $185.104(11)$ | $157.9291(88)$ |
| 2-MI | $122.7529(38)$ | $157.6901(44)$ |
| 4-MI | $317.20(14)$ | $157.784(60)$ |
| 5-MI | $386.001(19)$ | 157.68 |
|  |  |  |
| $N$-methylpyrrole | $67.8021(38)$ | - |
| 2-methylpyrrole | $279.7183(26)$ | 167.0422 |
|  |  |  |
| 2-methylthiazole | $34.938(20)$ | 165.1886 |
| 4-methylthiazole | $357.59(11)$ | $166.79(6)$ |
| 5-methylthiazole | $332.03(8)$ | $164.20(36)$ |
|  |  |  |
| 2-methyloxazole | $251.83(12)$ | $167.52(68)$ |
| 4-methyloxazole | $427.99(8)$ | $167.67(27)$ |
| 5-methyloxazole | $477.88(13)$ | $168.52(37)$ |




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Figure 6.8. From left to right; pyrrole, thiazole, oxazole, imidazole, isothiazole, isoxazole, indole. The numbers next to each carbon indicate the measured barrier to internal rotation (in $\mathrm{cm}^{-1}$ ) for the respective methylated analogue. (references $15,16,39,21-23,39,53,60$ )

### 6.10 Conclusions

The ground state rotational spectra of $N$-, 2-, 4- and $5-\mathrm{MI}$ were recorded in the $7.0-18.5$ GHz frequency range. Rotational constants, centrifugal distortion constants, barriers to internal rotation of the $\mathrm{CH}_{3}$ groups and nuclear quadrupole coupling constants of the N atoms were determined experimentally and computationally. $r_{s}$ structure determination was performed by evaluation of changes in the moment of inertia of each isomer by analyzing the observed spectra of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues. The gas phase structure of 2 MI was compared to the structure determined by X-ray diffraction ${ }^{51}$. Differences between the two mainly arise from lattice and crystal packing effects in the latter. Planarity is observed within the heavy atoms' skeleton of the aromatic ring in each isomer with the only contributions to the out-of-plane mass arising from two protons of the $\mathrm{CH}_{3}$ group. Spectroscopic parameters related to the internal rotation of the $\mathrm{CH}_{3}$ groups were evaluated including the values of the $V_{3}$ barrier heights. A strong correlation between the value of $V_{3}$ and the position where the $\mathrm{CH}_{3}$ group is substituting in the ring was observed, consistent with observations for isomers of MT and MO. Driving force for that variation in $V_{3}$ is likely dominated by electronic effects and, to a lesser extent, by steric hindrance around the $\mathrm{CH}_{3}$ group obstructing its internal motion. The nuclear quadrupole coupling constants $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ in terms of principal nuclear axes $(x, y, z)$ located on each individual N atoms are reported and compared to those determined for other imidazole derivatives. Subtle differences are observed between the different molecules suggesting that nuclear charges in the N atoms are not significantly affected by methylation or halogenation.

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## Chapter 7. Hydrogen Bonding of Methylimidazole Isomers with Water: The Effect on the Barrier Height

### 7.1 Introduction

It was discussed in chapters 5 and 6 that imidazole is a biologically significant molecule. It is the building block of adenine, guanine, histamine, histidine, to name a few, meaning imidazole is abundant in the human body. Functionalizing imidazole results in molecules with biochemical activity, i.e. the anti-fungal drug chlotrimazol, ${ }^{1}$ the antibiotic and antiprotozoal drug metronidazole ${ }^{2}$ and various antivirals inhibiting replication of hepatitis viruses $^{3}$ (HAV, HBV, HCV etc). These molecules, once present in the human body, are expected to interact with others, including water, as part of their mode of action. Understanding conformational and bonding preferences by targeting prototype "building blocks" like imidazole is an imperative part of the process of synthesizing novel drugs that will make it through the phases of clinical trials.

Hydrogen bonds are the primary type of intermolecular interactions that are manifested in the structures of the weakly bound complexes formed between the imidazole building block and other molecules. Rotational spectroscopy is a powerful tool that allows for characterization of these interactions on a macroscopic scale. Conformational and bonding trends may be rationalized and an insight into the dynamics of imidazole-bearing complexes is given at internal temperatures as low as 2 K . Several microwave spectroscopy studies have explored the effect that complex formation imposes on the barrier to internal rotational of a group of three-fold symmetry in a molecule. ${ }^{4-10}$ In toluene, ${ }^{11}$ a six-fold barrier of approximately $4.9 \mathrm{~cm}^{-1}$ is observed suggesting essentially free rotation of the $\mathrm{CH}_{3}$ group. The symmetry is reduced to three-fold upon attachment of $\mathrm{SO}_{2}$ to toluene ${ }^{6}$ resulting in a $V_{3}$ of $83.2 \mathrm{~cm}^{-1}$.

The binding of water to imidazole was explored in chapter 5 where two monohydrate complexes of imidazole were simultaneously isolated within an argon free-jet expansion. In chapter 6, the barriers to internal rotation in methylimidazole isomers were determined with rotational spectroscopy. ${ }^{12}$ The stepwise solvation of various aromatic and heteroaromatic molecules has been explored with microwave spectroscopy, ${ }^{13-18}$ however, there is very limited information on the stepwise microsolvation of their methylated analogues and the effect of microsolvation on the barrier height. To the author's best
knowledge, this is the first comparative study of the effect of the first step of microsolvation on the barrier height of $N-, 2-, 4-$, and $5-\mathrm{MI}$.

### 7.2 Experimental Details

The experimental details are given in chapter 6 section 6.2. The spectra of $N$-, 2-, 4- and 5$\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ were recorded alongside the spectra of their monomers $N-, 2-, 4-$ and $5-\mathrm{MI}$, respectively. No deliberate actions were taken to introduce water in the experiments; it is likely a contaminant present in the gas line or the walls of the vacuum chamber, as also seen in chapter 5 , section 5.2 , or within the respective methylimidazole sample. Isotopic experiments with $\mathrm{D}_{2} \mathrm{O}$ (Sigma-Aldrich, $99.9 \% \mathrm{D}$ atom) were performed to confirm the assignment of molecular carriers and partially elucidate the geometry of the complexes. Approximately 0.1 mL of $\mathrm{D}_{2} \mathrm{O}$ was placed in the reservoir described in chapter 3 and that amount was sufficient to collect data for all complexes in three individual experiments.

For $\mathrm{N}-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, an additional experiment was performed where the reservoir attached on the valve faceplate was heated to $90^{\circ} \mathrm{C}$. The heater was placed around the reservoir and the temperature was monitored by a K-type thermocouple attached to a temperature controller. $N$-MI vapour co-expanded with argon at a constant pressure of 5 bar into the vacuum chamber. The resulting spectrum was collected over the course of 2.34 M FID averages. For isotopic substitution of the H atoms in the water subunit, $\mathrm{D}_{2} \mathrm{O}$ (SigmaAldrich, $99.9 \% \mathrm{D}$ atom) was placed in a reservoir attached to the gas line, approximately 20 cm before the pulse valve. This experiment was part of a series where the performance, reliability and safety of the heater was evaluated as an alternative method to laser vaporization.

### 7.3 Computational Methods

Geometry optimizations of the $N-, 2-, 4-$ and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ complexes (figure 7.1 ) were performed. The starting points were directed by the work in chapters 5 and 6 . The optimized geometries of $N-, 2-, 4-$ and $5-\mathrm{MI}$ were used and a water molecule was placed in close proximity to the pyridinic nitrogen of each methylimidazole monomer. Geometry optimizations were also performed for alternative monohydrates where water coordinates at the pyrrolic nitrogen of 2-, 4- and $5-\mathrm{MI}$, in a manner seen in chapter 5 for $\mathrm{H}_{2} \mathrm{O}$ imid. The coordinates for the $\mathrm{H}_{2} \mathrm{O} \cdots 2-\mathrm{MI}, \mathrm{H}_{2} \mathrm{O} \cdots 4-\mathrm{MI}$ and $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ at the B3LYP(D3BJ)/aug-cc-pVTZ level are displayed in appendix A tables A31-A33. In chapter 6, where the geometry and barriers to internal rotation of the $N-, 2-, 4-$ and $5-\mathrm{MI}$ are discussed, given the level of consistency between theory and experiment, the B3LYP(D3BJ)/aug-cc-pvtz method ${ }^{19-24}$ was used for structural comparisons and prediction of the $V_{3}$ barriers to internal rotation. Geometry optimizations of $N-, 2-, 4-$ and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ were therefore performed at the same level. Optimizations were also performed with the $\omega$ B97X-D/aug-cc-pVQZ method in order to evaluate its performance with these complexes, like in chapter 5 for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O}$ imid. Finally, the geometries were also calculated at the MP2/aug-cc-pVDZ level. The $V_{3}$ barriers to internal rotation for each complex are predicted with all methods by scanning the dihedral angles $\angle(H-C 6-N 1-C 2), \angle(H-C 6-C 2-N 3)$, $\angle(H-C 6-C 4-C 5)$ and $\angle(H-C 6-C 5-N 1)$ for each of $N-, 2-, 4-$ and $5-\mathrm{MI}^{\cdots} \mathrm{H}_{2} \mathrm{O}$, respectively. The calculated rotational constants ( $A_{e}, B_{e}$ and $C_{e}$ ), nuclear quadrupole coupling constants and dipole moment components ( $\left|\mu_{a}\right|,\left|\mu_{b}\right|$ and $\left|\mu_{c}\right|$ ) are summarized in tables 7.1-7.3. The $V_{3}$ barriers to internal rotation and energies $\Delta E$ for each complex at each level are summarized in tables 7.9 and 7.10 alongside their percentage deviations of calculated rotational constants from experimentally determined ones. The calculated optimized geometries for each of $N$-, 2-, 4- and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ at B3LYP(D3BJ)/aug-cc-pvtz are shown in figure 7.1.


Figure 7.1. Optimized equilibrium geometries of $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ at the B3LYP(D3BJ)/aug-cc-pVTZ.

Table 7.1. Calculated spectroscopic parameters at the B3LYP(D3BJ)/aug-pVTZ level.

|  |  | B3LYP(D3BJ)/aug-cc-pVTZ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Spectroscopic | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ |
| parameters |  |  |  |  |
| $A_{e}(\mathrm{MHz})$ | 5754.89 | 4182.14 | 3812.17 | 7574.94 |
| $B_{e}(\mathrm{MHz})$ | 1313.14 | 1769.10 | 1752.87 | 1183.73 |
| $C_{e}(\mathrm{MHz})$ | 1079.70 | 1255.94 | 1216.30 | 1033.88 |
| $\chi_{a a}(N 1)(\mathrm{MHz})$ | 1.3800 | 1.3054 | 1.2926 | 1.2282 |
| $\chi_{b b}-\chi_{c c}(N 1)(\mathrm{MHz})$ | 3.8624 | 4.2411 | 3.8734 | 4.1386 |
| $\chi_{a b}(N 1)(\mathrm{MHz})$ | -0.3646 | -0.1060 | -0.1275 | -0.1279 |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | -3.9395 | -3.2677 | -3.7995 | -3.4384 |
| $\chi_{b b}-\chi_{c c}(N 3)(\mathrm{MHz})$ | -0.1405 | -0.4252 | -0.1113 | -0.8268 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | -0.1242 | 1.6956 | -0.4669 | 1.7300 |
| $\left\|\mu_{a \mid},\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|(\mathrm{D})\right.$ | $5.5,0.4,1.4$ | $4.4,1.7,1$ | $5.4,0.5,1.3$ | $5.8,1.5,1.2$ |

Table 7.2. Calculated spectroscopic parameters at the $\omega$ B97X-D/aug-cc-pVQZ level.

|  |  | $\omega$ B97X-D/aug-cc-pVQZ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Spectroscopic | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ |
| parameters |  |  |  |  |
| $A_{e}(\mathrm{MHz})$ | 6111.37 | 4197.93 | 3993.46 | 7828.80 |
| $B_{e}(\mathrm{MHz})$ | 1277.08 | 1758.92 | 1740.95 | 1176.29 |
| $C_{e}(\mathrm{MHz})$ | 1067.06 | 1252.42 | 1230.17 | 1032.29 |
| $\chi_{a a}(N 1)(\mathrm{MHz})$ | 1.3700 | 1.2408 | 1.2838 | 1.1703 |
| $\chi_{b b}-\chi_{c c}(N 1)(\mathrm{MHz})$ | 3.6886 | 4.1757 | 3.7182 | 4.0763 |
| $\chi_{a b}(N 1)(\mathrm{MHz})$ | 0.3987 | -0.1415 | -0.1741 | -0.1667 |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | -3.9955 | -3.3702 | -3.7285 | -3.4338 |
| $\chi_{b b}-\chi_{c c}(N 3)(\mathrm{MHz})$ | -0.3999 | -0.6404 | -0.4053 | -1.1633 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | 0.4037 | 1.6781 | -0.9716 | 1.8540 |
| $\left\|\mu_{\mathrm{a} \mid,}\right\| \mu_{\mathrm{b}}\left\|,\left\|\mu_{c}\right\|(\mathrm{D})\right.$ | $6.1,0.1,1.2$ | $4.5,1.8,1.1$ | $5.4,0.3,1.2$ | $5.7,1.6,1.2$ |

Table 7.3. Calculated spectroscopic parameters at the MP2/aug-cc-pVDZ level.

|  | MP2/aug-cc-pVDZ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Spectroscopic | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ |
| parameters | 5034.14 | 4149.27 | 3987.81 | 8291.84 |
| $A_{e}(\mathrm{MHz})$ | 1424.65 | 1739.08 | 1714.32 | 1164.63 |
| $B_{e}(\mathrm{MHz})$ | 1121.24 | 1243.81 | 1215.47 | 1030.84 |
| $C_{e}(\mathrm{MHz})$ | 0.9915 | 1.0375 | 1.1681 | 0.9680 |
| $\chi_{a a}(N 1)(\mathrm{MHz})$ | 3.1973 | 3.6275 | 3.2083 | 3.5815 |
| $\chi_{b b}-\chi_{c c}(N 1)(\mathrm{MHz})$ | -0.3833 | 0.1489 | -0.1779 | -0.1465 |
| $\chi_{a b}(N 1)(\mathrm{MHz})$ | -3.5256 | -2.6000 | -2.8887 | -2.4216 |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | -0.1978 | -0.3701 | -0.0461 | -0.7368 |
| $\chi_{b b}-\chi_{c c}(N 3)(\mathrm{MHz})$ | 0.5722 | -1.5757 | -1.0735 | 1.8503 |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | $5.3,0.3,1.1$ | $4.2,1.2,0$ | $5.5,0.4,1.2$ | $5.2,1.5,1.2$ |
| $\left\|\mu_{\mathrm{a} \mid},\left\|\mu_{b}\right\|,\left\|\mu_{c}\right\|(\mathrm{D})\right.$ |  |  |  |  |

### 7.4 Spectral Analysis

Numerous lines remain unassigned alongside the microwave spectra of $N-, 2-, 4-$, and $5-$ MI in the $7.0-18.5 \mathrm{GHz}$ range (chapter 6 , figure $6.2,6.4$, and 6.5 ), excluding the identified species discussed in chapter 6 . Considering the presence of transitions ${ }^{25}$ assigned to $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$, formation of water complexes may be favored. ${ }^{25}$ The monohydrate complexes of $N-, 2-, 4$ and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ (figure 7.1) are calculated to be near prolate asymmetric tops with their electronic charges distributed such that the total dipole moment components are almost aligned with $a$-inertial axis. Considering the predicted values and magnitudes of the $V_{3}$ barriers, $A / E$ splitting of transition frequencies is expected to be resolvable by our experiment. The spectra that were recorded in each of the three individual experiments were examined and the $N-, 2-\mathrm{c}, 4$-, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ complexes were searched for. The spectra were recorded over the course of $2.34,1.2$ and 2.6 M FID averages, respectively. Consistent with the broad expectations described above, $a$-type patterns are immediately identifiable in each spectrum. The partially resolved hyperfine structure is consistent with the presence of two nitrogen nuclei, N 1 and N 3 , in the imidazole ring. $A$-state transition frequencies were fit with Watson's S-reduced Hamiltonian ${ }^{26,27}$ as implemented in Pgopher ${ }^{28}$ to produce the measured values of the spectroscopic parameters summarized table 7.4. ${ }^{26,27}$ The detailed form of the Hamiltonian has been described in chapter 2. The calculated value of the $\chi_{a b}$ nuclear quadrupole terms for N1 and N3 in each complex was included in the fits. This was so the measured values of $\chi_{a a}$ and $\chi_{b b}-\chi_{c c}$ would be used for the generation of the diagonal coupling terms $\chi_{z z}, \chi_{x x}$ and $\chi_{y y}$, a procedure described in chapters 2-6. Discussion of the diagonalized nuclear quadrupole coupling constants is beyond the scope of the chapter so these values are summarized in appendix A, table A43. Measured values of effective rotational constants $A_{0}^{\prime}, B_{0}^{\prime}$, and $C_{0}^{\prime}$, centrifugal distortion constants, nuclear quadrupole coupling constants are summarized in table 7.4 alongside derived values for the planar moment $P_{c c}^{\prime}$ and inertial defect $\Delta_{0}^{\prime}$. A definition of effective rotational constants was given in chapter 6 .

[^6]Table 7.4. Effective rotational constants $A_{0}^{\prime}, B_{0}^{\prime}$, and $C_{0}^{\prime}$ and other spectroscopic parameters determined with Pgopher for $A$-state transitions of $N$-, 2-, 4 -, and $5-\mathrm{MI}{ }^{\prime \cdots} \mathrm{H}_{2} \mathrm{O}$.

| Spectroscopic <br> parameters | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{0}^{\prime}(\mathrm{MHz})$ | $5015.939(64)^{\mathrm{a}}$ | $4238.129(36)$ | $4084.506(22)$ | $8440.90(44)$ |
| $B_{0}^{\prime}(\mathrm{MHz})$ | $1409.9347(14)$ | $1733.7787(15)$ | $1707.3390(15)$ | $1167.56380(82)$ |
| $C_{0}^{\prime}(\mathrm{MHz})$ | $1107.2937(14)$ | $1240.3116(12)$ | $1214.3010(11)$ | $1032.85910(75)$ |
| $D_{J}(\mathrm{kHz})$ | $2.3593(68)$ | $0.451(16)$ | $0.119(11)$ | $0.2633(48)$ |
| $D_{K}(\mathrm{kHz})$ | - | $-69.1(55)$ | - | - |
| $D_{J K}(\mathrm{kHz})$ | $-16.723(57)$ | $6.49(11)$ | $28.876(76)$ | $27.320(39)$ |
| $d_{k}(\mathrm{kHz})$ | $-0.0708(64)$ | - | $-0.3145(70)$ | $-0.0369(37)$ |
| $d_{j}(\mathrm{kHz})$ | $-0.882(10)$ | $-0.148(12)$ | $-0.133(11)$ | - |
| $\chi_{a a}(N 1)(\mathrm{MHz})$ | $1.245(16)$ | $1.218(21)$ | $1.199(16)$ | $1.650(62)$ |
| $\chi_{b b}-\chi_{c c}(N 1)(\mathrm{MHz})$ | $3.909(56)$ | $4.127(46)$ | $3.819(52)$ | $4.78(15)$ |
| $\chi_{a b}(N 1)(\mathrm{MHz})$ | $[-0.3646]$ | $[-0.1060]$ | $[-0.1275]$ | $[-0.1279]$ |
| $\chi_{a a}(N 3)(\mathrm{MHz})$ | $-3.609(13)$ | $-2.979(16)$ | $-3.356(12)$ | $-2.739(54)$ |
| $\chi_{b b}-\chi_{c c}(N 3)(\mathrm{MHz})$ | $-0.065(43)$ | $-0.313(47)$ | $-0.416(62)$ | $-1.31(38)$ |
| $\chi_{a b}(N 3)(\mathrm{MHz})$ | $[-0.1242]^{\mathrm{b}}$ | $[1.6956]$ | $[-0.4669]$ | $[1.7300]$ |
| $\left\|\mu_{\mathrm{a} \mid},\left\|\mu_{\mathrm{b}}\right\|,\left\|\mu_{\mathrm{c}}\right\|(\mathrm{D})\right.$ | $5.5,0.4,1.4$ | $4.4,1.7,1$ | $5.4,0.5,1.3$ | $5.8,1.5,1.2$ |
| $\Delta_{0}^{\prime}\left(\mathrm{u} \AA^{2}\right)$ | $-2.7868(15)$ | $-3.2743(11)$ | $-3.5453(8)$ | $-3.4207(32)$ |
| $P_{c c}^{\prime}\left(\mathrm{u} \AA^{2}\right)$ | $1.3934(7)$ | $1.6371(6)$ | 1.7727 | $1.7104(16)$ |
| $\mathrm{N}^{\mathrm{c}}$ | 111 | 80 | 84 | 68 |
| $\sigma_{\mathrm{RMS}}(\mathrm{kHz})^{\mathrm{d}}$ | 16.5 | 14.4 | 11.6 | 14.3 |

[^7]

Figure 7.2. Expanded portion of the spectrum of $N$-MI collected over the course 2.34 M FID's. The $4_{04} \rightarrow 3_{03}$ transition of $N-M I \cdots \mathrm{H}_{2} \mathrm{O}$ split into $A$ - and $E$-states and their energy separation is related to the $V_{3}$ barrier height.


Figure 7.3. Expanded portion of the spectrum of 2-MI collected over the course 1.2 M FID's. The $3_{03} \rightarrow 2_{02}$ transition of $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ split into $A$ - and $E$-states and their energy separation is related to the $V_{3}$ barrier height.


Figure 7.4. Expanded portion of the spectrum of 4-MI collected over the course 2.6 M FID's. The $4_{23} \rightarrow 3_{22}$ transition of $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ split into $A$ - and $E$-states and their energy separation is related to the $V_{3}$ barrier height.


Figure 7.5. Expanded portion of the spectrum of 5-MI collected over the course 2.6 M FID's. The $8_{27} \rightarrow 7_{26}$ transition of $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ split into $A$ - and $E$-states and their energy separation is related to the $V_{3}$ barrier height.

The assignment of molecular carriers to the fitted spectra was further confirmed with isotopic experiments with $\mathrm{D}_{2} \mathrm{O}$. Two singly deuterated isotopologues were observed for each complex, with deuterium either substituting at the position of the bonding hydrogen participating in the intermolecular interaction, $\mathrm{H}_{\mathrm{b}}$, or at the position of the non-bonding hydrogen, $\mathrm{H}_{\mathrm{nb}}$. The fitted spectroscopic parameters obtained through fitting of $A$-state transitions with Watson's S-reduction are summarized in table 7.5. The spectra of the deuterated isotopologues were recorded over the course of $1.44,0.9$, and 2.9 M FID's, respectively.

In chapter 5, no splitting due to large amplitude motions (LAM) in the water subunit was observed in the spectrum of the imid $\cdots \mathrm{H}_{2} \mathrm{O}$, where water is the proton donor ${ }^{29}$. The $A$-state transitions of $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ were explored for evidence of LAM other than that of the $\mathrm{CH}_{3}$ undergoing internal rotation. No evidence was found that the water subunit undergoes LAM that couple the overall rotation and internal rotation in each of $N$-, 2-, 4-, and 5-MI $\cdots \mathrm{H}_{2} \mathrm{O}$, consistent with observations ${ }^{29,30}$ for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and 2-fluoropyridine $\cdots \mathrm{H}_{2} \mathrm{O}$. Absence of $c$-type transitions in the spectra of the four complexes discussed here, indicate that wagging and flipping motions at the water subunit are unhindered or that the complexes are rigidly planar. In chapter 5, we also reported the formation of the $\mathrm{H}_{2} \mathrm{O}$ imid complex where water is the proton acceptor and interacting via the pyrrolic $\mathrm{N}-\mathrm{H}$ site of imidazole. The spectrum was split into two components, labelled as $0^{-}$and $0^{+}$, as a result of a torsional motion associated with the water subunit. The overall intensity of that spectrum was lower than that of imid $\cdots \mathrm{H}_{2} \mathrm{O}$, despite $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}$ having a larger dipole moment, possibly as a result of the splitting described above and the relative energies favouring formation of the former. The spectra of $\mathrm{H}_{2} \mathrm{O} \cdots 2-\mathrm{MI}, \mathrm{H}_{2} \mathrm{O} \cdots 4-\mathrm{MI}$ and $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}^{\mathrm{D}}$ were searched for but not detected under these experimental conditions. Assuming that their geometry would be similar to that of $\mathrm{H}_{2} \mathrm{O}$ imid and that LAM associated with the $\mathrm{H}_{2} \mathrm{O}$ subunit and the $\mathrm{CH}_{3}$ group couple each other, the spectrum would be expected to be split into four components, $\mathrm{A}^{-}, \mathrm{A}^{+}, \mathrm{EO}^{-}$, and $\mathrm{E} 0^{+}$. No evidence for spectra following these expectations are observed under these experimental conditions. The calculated energies of $\mathrm{H}_{2} \mathrm{O} \cdots 2-\mathrm{MI}, \mathrm{H}_{2} \mathrm{O} \cdots 4-\mathrm{MI}$ and $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ at the B3LYP(D3BJ)/aug-cc-pVTZ level sugest that these monohydrate isomers are higher in energy by approximately $1000 \mathrm{~cm}^{-1}$.

[^8]Table 7.5. Effective rotational constants and other spectroscopic parameters determined with Pgopher for A-state transitions of N -, 2-, 4-, and $5-\mathrm{MI} \cdots \mathrm{HOD}$ and $\cdots \mathrm{DOH}$ isotopologues.

| Spectroscopic <br> parameters | $N-\mathrm{MI} \cdots \mathrm{DOH}$ | $N-\mathrm{MI} \cdots \mathrm{HOD}$ | $2-\mathrm{MI} \cdots \mathrm{DOH}$ | $2-\mathrm{MI} \cdots \mathrm{HOD}$ |
| :---: | :---: | :---: | :---: | :---: |
| $A_{0}(\mathrm{MHz})$ | $5036.633(58)^{\mathrm{a}}$ | $4981.903(86)$ | $4216.458(58)$ | $4187.992(50)$ |
| $B_{0}(\mathrm{MHz})$ | $1380.3352(17)$ | $1351.3770(25)$ | $1708.8034(25)$ | $1662.8773(22)$ |
| $C_{0}(\mathrm{MHz})$ | $1089.9312(13)$ | $1070.2310(23)$ | $1225.7080(21)$ | $1200.1827(18)$ |
| $D_{J}(\mathrm{kHz})$ | $2.2804(77)$ | $2.035(12)$ | $0.442(27)$ | $0.473(22)$ |
| $D_{K}(\mathrm{kHz})$ | - | - | $-71.8(97)$ | $-63(10)$ |
| $D_{J K}(\mathrm{kHz})$ | $-18.13(11)$ | $-15.51(26)$ | $6.31(19)$ | $6.32(13)$ |
| $d_{j}(\mathrm{kHz})$ | $-0.8060(89)$ | $-0.523(15)$ | $-0.126(20)$ | $-0.157(16)$ |
| N | 53 | 30 | 45 | 61 |
| $\sigma_{\mathrm{RMS}}(\mathrm{kHz})^{\mathrm{c}}$ | 13.7 | 18.7 | 18.2 | 17.7 |
| Spectroscopic | $4-\mathrm{MI} \cdots \mathrm{DOH}$ | $4-\mathrm{MI} \cdots \mathrm{HOD}$ | $5-\mathrm{MI} \cdots \mathrm{DOH}$ | $5-\mathrm{MI} \cdots \mathrm{HOD}$ |
| parameters |  |  |  |  |
| $A_{0}(\mathrm{MHz})$ | $4064.330(26)$ | $4034.596(34)$ | $8391.57(52)$ | $8351.24(60)$ |
| $B_{0}(\mathrm{MHz})$ | $1683.07260(77)$ | $1638.98921(94)$ | $1148.45060(76)$ | $1123.68324(69)$ |
| $C_{0}(\mathrm{MHz})$ | $1200.18317(88)$ | $1176.7805(11)$ | $1017.18919(75)$ | $998.12784(79)$ |
| $D_{J}(\mathrm{kHz})$ | $0.103(10)$ | $0.109(13)$ | $0.2545(58)$ | $0.2376(52)$ |
| $D_{J K}(\mathrm{kHz})$ | $29.03(13)$ | $29.06(22)$ | $26.930(100)$ | $24.766(95)$ |
| $d_{k}(\mathrm{kHz})$ | $-0.3088(67)$ | $-0.2663(86)$ | $-0.0365(40)$ | $-0.0317(43)$ |
| $d_{j}(\mathrm{kHz})$ | $-0.133(11)$ | $-0.133(11)$ | - | - |
| N | 61 | 44 | 37 | 39 |
| $\sigma_{\mathrm{Rms}}(\mathrm{kHz})$ | 12.7 | 13.4 | 12.5 | 12 |

[^9]
### 7.5 Geometry

It has been discussed in chapters 4,5 , and 6 , that a first insight into the geometry of a complex or molecule may be obtained by evaluating the planar moments and inertial defect from the measured rotational constants with no assumptions about the structure. The reliability of this approach, however, is expected to be affected by the internal rotation of the $\mathrm{CH}_{3}$ group not being aligned with any inertial axis and low lying vibrations in the water subunit in $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$. The evaluated values of $P_{c c}^{\prime}, \Delta_{0}^{\prime}$ and $P_{c c}$ and $\Delta_{0}$ follow broad expectations for planar complexes with an internal three-fold $\mathrm{CH}_{3}$ rotor. It has been shown that inclusion of $E$-states in the fits produces a different set of rotational constants to the $A$-state fit. This accounts for the differences in the values of $P_{c c}^{\prime}, \Delta_{0}^{\prime}$ and $P_{c c}$ and $\Delta_{0}$ in each of $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$.

Substitution coordinates $\left(r_{s}\right)$ of the H atoms in the water subunit were determined using the Kraitchman method ${ }^{27,31}$ described in chapter 2, section 2.10.2. These coordinates are summarized in table 7.6 alongside their Costain errors ${ }^{32,33}$ to account for vibration-rotation coupling effects. DFT Calculated $r_{e}$ coordinates are also shown and the results are in good agreement. As in previous chapters, the coordinate signs were implied by the DFT calculated coordinates and the ones that were calculated as imaginary numbers due to being positioned close to an axis were set to zero. In $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, for $\mathrm{H}_{\mathrm{b}}$ it is calculated that $|c|=0.030(52) \AA$. The uncertainty in the coordinate is large compared to its magnitude which is consistent with the $\mathrm{H}_{\mathrm{b}}$ atom being positioned in the plane defined by $N-\mathrm{MI}$. Often the Kraitchman method performs poorly when it comes to determining the position of a H atom, mainly due to the elongation ${ }^{34}$ and the differences in vibrational energy of the bond caused by D which may explain the high uncertainty in that coordinate. In 2-, 4 -, and 5 MI $\cdots \mathrm{H}_{2} \mathrm{O}$, the value of $|c|$ consistently shows that $\mathrm{H}_{\mathrm{b}}$ involved in the intermolecular interaction lies in the plane of the respective methylimidazole. Similarly, the $\mathrm{H}_{\mathrm{b}}$ atom in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is in the plane of imidazole (chapter 5). It was calculated that the non-bonding $\mathrm{H}_{\mathrm{nb}}$ in the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ complex points above (or below) the plane defined by the imidazole ring with $|c|=0.4521(38) \AA$. It is consistently observed that in each of $N$-, 2-, 4-, and 5$\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ the magnitude and value of the $|c|$ coordinate of $\mathrm{H}_{\mathrm{nb}}$ are similar with one another and with that for imid $\cdots \mathrm{H}_{2} \mathrm{O}$.

In table 7.6 , for $\mathrm{N}-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ and $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, some inconsistencies are observed between the experimental and calculated $b$-coordinate of $\mathrm{H}_{\mathrm{nb}}$. In both complexes, the magnitude of $|b|$ is underestimated by approximately $0.5 \AA$ with both DFT methods. The agreement
improves slightly at the MP2/aug-cc-pVDZ level. Rovibrational calculations were performed for $N$ - and $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ to check whether the optimization calculations had landed on a saddle point or local minimum geometry. No imaginary frequencies were found so each calculation is concerned with a global minimum. These inconsistencies could be rationalized by the fact that DFT methods cannot always account for long range interactions with high precision. Benchmarking has been performed for various systems in a number of studies that support this statement. ${ }^{22,35,36}$ The complex internal dynamics of internal rotation of the $\mathrm{CH}_{3}$ and motions associated with the water subunit may influence the accuracy of these calculations. As it will be seen in the following sections, the calculated $V_{3}$ barriers for $N$ - and $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ are somewhat incosistent when compared to the experimental values. It should be noted that these methods calculate an equilibrium structure whilst the zero-point geometry is probed by the experiment and often the two structures differ from one another.

Table 7.6. Experimental $\left(r_{s}\right)$ and calculated $\left(r_{e}\right)$ coordinates of the H atoms in the water subunit in $N$-, $2-, 4-$, and $5-\mathrm{MI}{ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$.

|  |  |  | $a / \AA$ | b/ $\AA$ | c/ $\AA$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $\mathrm{H}_{\mathrm{nb}}$ | $r_{s}$ | $3.91722(42)^{\text {a }}$ | -0.7145(23) | 0.4670(35) |
|  |  | $r_{e}$ | $3.9972^{\text {b }}$ | -0.2262 | 0.7223 |
|  | $\mathrm{H}_{\mathrm{b}}$ | $r_{s}$ | 2.77970(57) | $0{ }^{\text {c }}$ | -0.030(52) |
|  |  | $r_{e}$ | 2.6691 | -0.1954 | -0.0341 |
| 2-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ | $\mathrm{H}_{\mathrm{nb}}$ | $r_{s}$ | -3.50137(45) | 1.1870(13) | 0.3506(45) |
|  |  | $r_{e}$ | -3.4265 | 1.0444 | 0.6827 |
|  | $\mathrm{H}_{\mathrm{b}}$ | $r_{s}$ | -2.06203(77) | 0.8779(20) | -0.097(16) |
|  |  | $r_{e}$ | -2.1105 | 0.7120 | -0.0300 |
| 4-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ | $\mathrm{H}_{\mathrm{nb}}$ | $r_{s}$ | -3.46242(46) | -1.1470(14) | 0.5651(29) |
|  |  | $r_{e}$ | -3.4750 | -0.6450 | 0.7373 |
|  | $\mathrm{H}_{\mathrm{b}}$ | $r_{s}$ | -2.06768(74) | -0.7993(19) | $0^{\text {c }}$ |
|  |  | $r_{e}$ | -2.1438 | -0.6345 | -0.0151 |
| 5-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ | $\mathrm{H}_{\mathrm{nb}}$ | $r_{s}$ | -4.08392(49) | 0.6321(33) | -0.5224(40) |
|  |  | $r_{e}$ | -3.9921 | 0.6187 | -0.7450 |
|  | $\mathrm{H}_{\mathrm{b}}$ | $r_{s}$ | -2.68608(56) | $0.5923(33)$ | 0.096(20) |
|  |  | $r_{e}$ | -2.7079 | 0.3405 | 0.0369 |

${ }^{\text {a }}$ Costain's errors in units of the last significant figures in parentheses calculated as fractional uncertainties by means of $\delta_{z}=0.0015 /|z|$, where $|z|$ is the absolute value of a coordinate.
${ }^{\mathrm{b}}$ Calculated equilibrium $r_{e}$ coordinates at the $\omega$ B97X-D/aug-cc-pVQZ level.
${ }^{\mathrm{c}}$ Where imaginary results were obtained, the coordinate was set to zero.

### 7.6 Internal Rotation

The $V_{3}$ barriers to internal rotation in $N-, 2-, 4-$, and $5-\mathrm{MI}$ were determined ${ }^{12}$ and discussed in chapter 6. Two methods were used, PAM and IAM, with the resulting value for each isomer being dependent on the position where the $\mathrm{CH}_{3}$ group substitutes on the imidazole ring. The $\mathrm{PAM}^{27,37}$ is appropriate for molecules with low barriers in which the local $\mathrm{C}_{3}$ axis of the $\mathrm{CH}_{3}$ group is close to parallel with the $a$-inertial axis and out-of-plane contributions to $\Delta_{0}^{\prime}$ mainly arise from the $\mathrm{CH}_{3}$ protons. With that in mind, $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ do not fulfill the requirements of the PAM, so the $V_{3}$ barriers will only be approached by the IAM ${ }^{27}$ implemented in the XIAM program. ${ }^{38}$

XIAM allows for simultaneous fitting of both ground and first excited torsional $A$ - and $E$ state transitions ( $m=0$ and $m= \pm 1$ ) with the IAM. For a given $A$ - and $E$-state transition pair for an asymmetric top molecule, the quantum numbers $J, K_{-1}$ and $K_{1}$ are the same for both states. The $V_{3}$ barriers at various levels of theory for $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ are summarized in tables 7.9 and 7.10. Considering their calculated values, the $A$ - and $E$-state splittings are expected to be resolvable in our experiment and varying between 100 kHz to 8 MHz . As it was seen in chapter 6 , the lowest $V_{3}$ barrier typically accounts for the largest splitting whilst the highest $V_{3}$ barrier will generate $A$ - and $E$-state transition pairs that are close in energy and, as such, the smallest splitting. Rotational constants $A_{0}, B_{0}$ and $C_{0}$ and centrifugal distortion constants $D_{J}, D_{J K}, D_{K}, d_{1}$ and $d_{2}$ found in table 7.7 are generated through least squares fitting of $A$ - and $E$-state transitions of $N$-, 2-, 4 -, and $5-\mathrm{MI}^{\cdots} \mathrm{H}_{2} \mathrm{O}$, as appropriate. Internal rotation parameters that were determined for each complex include the $V_{3}$ barrier to internal rotation and the angles $(i, a),(i, b)$ and $(i, c)$. It was not possible to fit the $F_{0}$ standard rotational constant for an $\mathrm{sp}^{3}$ hybridized $\mathrm{CH}_{3}$ top so that parameter was kept fixed to the values determined experimentally for the respective methylimidazole monomer in chapter 6 .

The fitting procedure described in chapter 6 was followed here for $N$-, 2-, 4 -, and 5 $\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$. For the XIAM input file, the rotational constants and centrifugal distortion constants that were experimentally determined through fitting of the $A$-state transitions and are summarized in table 7.4 were used as starting points. The polar coordinates $\varepsilon$ and $\delta$ that define the orientation of the $\mathrm{CH}_{3}$ group with respect to each inertial axis and the $V_{3}$ barrier were based on the DFT calculated geometries at the B3LYP(D3BJ)/aug-cc-pVTZ level. The hyperfine structure induced by the presence of two N nuclei in methylimidazole was not fit as XIAM does not deal with two quadrupolar nuclei. The center frequency of
each $A$-state transition was selected and the $F_{1}$ and $F$ quantum numbers were omitted from the line-lists. The appropriate $E$-state transitions sharing the same $J, K_{-1}$ and $K_{1}$ quantum numbers as the respective $A$-state were identified for a number of transitions. As more $E$ state transtions were identified and progressively added to each line-list, the frequency centers were corrected after a few fit cycles, as described in chapter 6 . Transitions with $|m|>1$ were not detected and this is an outcome of effective adiabatic cooling of molecules in the supersonic expansion.

The spectroscopic parameters displayed in table 7.7 were obtained through global fits of $A$ and $E$-state transitions of $N$-, 2-, 4-, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ with Watson's S-reduction. ${ }^{27,39}$ The fitted values of the $V_{3}$ barriers are 210.611(46), 154,1193(50), 321.05(11) and 380.230(54) $\mathrm{cm}^{-1}$ for $N-, 2-, 4-$, and $5-\mathrm{MI}{ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$, respectively. The values of $(i, a)$ imply that the $\mathrm{CH}_{3}$ top is no longer closely aligned with the $a$-inertial axis like in their respective monomers. The ( $i, c$ ) values suggest that the $\mathrm{CH}_{3}$ is effectively in the plane defined by each imidazole ring. For 5-MI $\cdots \mathrm{H}_{2} \mathrm{O}$, the $(i, a),(i, b)$ and $(i, c)$ angles were kept fixed to their calculated values as it was not possible to simulataneously fit the angles and the $V_{3}$. The projection of the $\mathrm{CH}_{3}$ on each inertial axis is small and the fitted $V_{3}$ value was essentially insensitive to the value given to the polar coordinates $\varepsilon$ and $\delta$.

The fitted $V_{3}$ values were used to benchmark the performance of quantum chemical calculations and the percentage deviations are shown in table 7.9 and 7.10. The percentage deviations are relatively large, however, discrepancies are somewhat expected at these levels of theory especially when long range interactions cannot be accounted for with high precision. The highest level of consistency between theory and experiment is observed at the B3LYP(D3BJ)/aug-cc-pVTZ level with deviations in the range of $14-32 \%$. The agreement between theory and experiment is generally high for $N-, 2$ - and $5-\mathrm{MI}^{\cdots} \mathrm{H}_{2} \mathrm{O}$, particularly for the latter. The $V_{3}$ barrier to internal rotation in $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ is significantly underestimated by all three methods. Considering the complexity of the $N-, 2-, 4-$, and $5-$ $\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ arising from weak interactions and large amplitude motions, convergence of the energy of each molecular system may be hard to achieve. It should also be noted that these methods calculate the $V_{3}$ barrier starting at equilibrium geometry whereas the experimental values correspond to the zero-point. Low lying vibrations like those described for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ are also expected to affect the barrier height, either through spatial interaction or electronic effects propagating across each aromatic system.

Table 7.7. Global fits for $A$ - and $E$-state transitions of $N$-, 2-, $4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ produced in XIAM.

| Spectroscopic <br> parameters | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{A}_{\mathbf{0}}(\mathrm{MHz})$ | $5009.614(42)^{\mathrm{a}}$ | $4234.235(14)$ | $4083.925(11)$ | $8439.68(56)$ |
| $\boldsymbol{B}_{\mathbf{0}}(\mathrm{MHz})$ | $1409.1474(13)$ | $1732.53380(83)$ | $1707.18034(71)$ | $1167.58629(93)$ |
| $\boldsymbol{C}_{\mathbf{0}}(\mathrm{MHz})$ | $1107.5777(12)$ | $1240.29861(72)$ | $1214.30238(51)$ | $1032.84575(85)$ |
| $\boldsymbol{D}_{\boldsymbol{J}}(\mathrm{kHz})$ | $2.2076(56)$ | $0.4472(59)$ | $0.0814(54)$ | $0.3116(68)$ |
| $\boldsymbol{D}_{\boldsymbol{K}}(\mathrm{kHz})$ | - | $[-69.1]$ | - |  |
| $\boldsymbol{D}_{\boldsymbol{J} \boldsymbol{K}}(\mathrm{kHz})$ | $-20.494(74)$ | $6.204(24)$ | $26.686(49)$ | $27.218(72)$ |
| $\boldsymbol{d}_{\boldsymbol{k}}(\mathrm{kHz})$ | $[-0.0708]^{\mathrm{b}}$ | - | $-0.3104(39)$ | $[-0.0188]$ |
| $\boldsymbol{d}_{\boldsymbol{j}}(\mathrm{kHz})$ | $0.8456(76)$ | $-0.1393(55)$ | $-0.1544(52)$ | - |
| $\mathrm{F}_{0}(\mathrm{GHz})$ | $\{157.9291\}^{\mathrm{c}}$ | $\{157.6901\}$ | $\{157.784\}$ | $\{157.68\}$ |
| $\mathrm{V}_{\mathbf{3}}\left(\mathrm{cm} \mathrm{cm}^{-1}\right)$ | $210.611(46)$ | $154.1193(50)$ | $321.05(11)$ | $380.230(54)$ |
| $\angle(\boldsymbol{i}, \boldsymbol{a}) /^{\circ}$ | $91.1034(23)$ | $125.8477(35)$ | $271.9571(75)$ | $171{ }^{\mathrm{f}}$ |
| $\angle(\boldsymbol{i}, \boldsymbol{b}) /^{\circ}$ | $12.740(43)$ | $35.9318(40)$ | $7.936(72)$ | $99^{\mathrm{f}}$ |
| $\angle(\boldsymbol{i}, \boldsymbol{c}) /^{\circ}$ | $77.310(43)$ | $87.8600(69)$ | $82.312(72)$ | $90^{\mathrm{f}}$ |
| $\boldsymbol{\Delta}_{\boldsymbol{0}}^{\prime}\left(\mathrm{u} \AA^{2}\right)$ | $-3.2313(10)$ | $-3.5891(5)$ | $-3.5909(4)$ | $-3.415(4)$ |
| $\boldsymbol{P}_{\boldsymbol{c c}}\left(\mathrm{u} \AA^{2}\right)$ | $1.6156(5)$ | $1.79457(24)$ | $1.79546(20)$ | $1.7073(20)$ |
| $\mathrm{N}^{\mathrm{d}}$ | 54 | 44 | 50 | 48 |
| $\sigma(\mathrm{kHz})^{\mathrm{e}}$ | 10.9 | 5.3 | 4.7 | 16.6 |

${ }^{2}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
${ }^{\mathrm{b}}$ Values in square brackets were kept fixed to the values determined in Pgopher fits in table 7.4.
${ }^{c}$ Values in curly brackets were kept fixed to the values determined in chapter 6 for the $N$-, 2-, 4-, and 5-MI monomers.
${ }^{\mathrm{d}}$ Total number of $A$ - and $E$-state transitions included in the fit.
${ }^{e}$ Root mean square deviation of the fit.
${ }^{\mathrm{f}}$ Angles fixed to the calculated values.

### 7.7 Discussion

To the author's best knowledge, there are no other studies on the effect of complex formation with water on the $V_{3}$ barrier height in five- and six-membered, methylated, heteroaromatic rings. The spectra of corresponding microsolvated, unmethylated analogues ${ }^{13,14,40}$ in water, i.e. oxazole $\cdots \mathrm{H}_{2} \mathrm{O}$, pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$, pyrimidine ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ were mentioned in chapter 5 and used for comparisons with the imid $\cdots \mathrm{H}_{2} \mathrm{O}$ complex. A number of studies have explored the effect of microsolvation in non-aromatic molecules such as in acetic acid, ${ }^{5}$ methyl glycidate,,${ }^{41}$ methyl carbamate, ${ }^{42}$ pyruvic acid, ${ }^{43} o$-toluic acid ${ }^{44}$ and $p$ toluic acid, ${ }^{4}$ to name a few. In the case of acetic acid, the $V_{3}$ barrier decreases upon progressive hydration with water whilst in methyl carbamate, the opposite trend is observed and the $V_{3}$ barrier increases. It is suggested that the barriers are influenced by the strength of the hydrogen bonds in the microsolvated networks. In $p$-toluic acid, the $V_{3}$ barrier remains essentially unchanged upon attachment of $\mathrm{H}_{2} \mathrm{O}$.

It is worth considering how the $V_{3}$ barrier to internal rotation in $N-, 2-, 4-$, and $5-\mathrm{MI}$ is influenced by the first step of their microsolvation with $\mathrm{H}_{2} \mathrm{O}$. The $V_{3}$ barriers are collectively shown in table 7.8 for $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ and their respective methylimidazole monomers. Calculated values at the B3LYP(D3BJ)/aug-cc-pVTZ level are also shown alongside the experimental values. Attachment of one $\mathrm{H}_{2} \mathrm{O}$ molecule to 4 - and 5-MI has very minimal effects on the barrier height, causing the $V_{3}$ to increase by $4 \mathrm{~cm}^{-1}$ and decrease by $6 \mathrm{~cm}^{-1}$, respectively. More profound changes are observed upon hydration of $N$ - and 2MI where an increase of approximately 25 and $32 \mathrm{~cm}^{-1}$ is observed, respectively. As it has been discussed in chapter 6 , steric and electronic effects may cause the barrier to internal rotation of a three-fold group in a molecule to increase or decrease.

Assuming that the $\mathrm{H}_{2} \mathrm{O}$ subunit is positioned in a manner similar to that seen in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ where a secondary interaction $r(\mathrm{O} \cdots \mathrm{H} 2)$ is observed, we can assume that the three-fold potential in 2-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ is hindered by similar secondary interactions between the O atom and the protons in the $\mathrm{CH}_{3}$ group in 2-MI. In imid $\cdots \mathrm{H}_{2} \mathrm{O}$, the $r(\mathrm{O} \cdots \mathrm{H} 2)$ distance was calculated to be approximately $3.5 \AA$ with DFT and was derived to be approximately $3.13(8) \AA$ with the $r_{0}$ fit. It also follows that in 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ the dihedral angles that define the orientation of the $\mathrm{H}_{2} \mathrm{O}$ subunit are are $\angle\left(H_{n b}-O-H_{b} \cdots N 3\right)=180^{\circ}$ and $\angle(O-$ $\left.H_{b} \cdots N 3-C 2\right)=0^{\circ}$. The intermolecular distance between the O of the water and the inplane proton $r\left(\mathrm{O} \cdots \mathrm{H}_{\text {Me }}\right)$ of the $\mathrm{CH}_{3}$ group is calculated to be approximately $2.64 \AA$ and the $r(\mathrm{O} \cdots \mathrm{C} 6)$ distance is $3.51 \AA$ at the $\omega \mathrm{B} 97 \mathrm{X}-\mathrm{D} / \mathrm{aug}-\mathrm{cc}-\mathrm{pVQZ}$ level. These values are
comparable to those determined for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and indicate that secondary interactions between the O and the $\mathrm{CH}_{3}$ protons result in an increase in the $V_{3}$ barrier height as the $\mathrm{CH}_{3}$ internal rotation is sterically hindered. Isotopic data with ${ }^{18} \mathrm{O}$ would likely allow for derivation of the $r(\mathrm{O} \cdots \mathrm{C} 6)$ distance, however, it is highly unlikely to generate a geometry that contradicts the current assumptions and conclusions.

The $V_{3}$ barrier height increase upon hydration of $N$-MI may be due to a combination of steric and electronic effects. As it was discussed in chapter 6, the variation of the $V_{3}$ barrier height across methylimidazole isomers is correlated to the overlap between $\pi$-orbitals on $\mathrm{C}-\mathrm{H}$ bonds adjacent to the $\mathrm{CH}_{3}$ and $\pi$-like orbitals at the $\mathrm{CH}_{3}$. If the immediate, local chemical environment around the $\mathrm{CH}_{3}$ is symmetric like in toluene ${ }^{45}$ and $N$-MP, ${ }^{46}$ then a small $V_{6}$ is detected and if the symmetry is reduced, the barrier height increases. Hydration of $N$-MI is expected to further reduce the symmetry around the $\mathrm{N}-\mathrm{CH}_{3}$ bond. Based on the geometry assumptions made earlier for $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, secondary interactions involve the H 2 on the C 2 adjacent to the $\mathrm{N}-\mathrm{CH}_{3}$ bond. The lone pair from the non-bonding orbital on the O of water donates its electrons into the anti-bonding $\sigma^{*}$ of H 2 . Propagation of electronic effects across the aromatic system is also expected to be affected by attachment of $\mathrm{H}_{2} \mathrm{O}$. However, the current experiment and the available computational methods are not able to provide a detailed insight into the electronic effects involved.

Following similar arguments and assumptions about the orientation of the water subunit in 4- and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, it follows that the O atom of water is not in close proximity to the $\mathrm{CH}_{3}$ in 4 - and $5-\mathrm{MI}$ and thus sterical hinderence does not directly influence internal rotation. Electronic effects caused by attachement of $\mathrm{H}_{2} \mathrm{O}$ are also subtle considering that no secondary interactions occur around the local chemical environment around the $\mathrm{CH}_{3}$. Considering the resonance canonicals of 4 - and $5-\mathrm{MI}$, it is apparent that delocalization of charges is not concerned with the site of the C4 and C5 carbons. The resonance canonicals are displayed in figure 7.6 highlighting that 4 - and $5-\mathrm{MI}$ are tautomers of each other.

The performance of the computational methods described in section 7.3 was benchmarked against the experimentally determined rotational constants and their percentage deviations are summarized in tables 7.10 and 7.11 . The calculated $V_{3}$ barriers were also checked against the experimentally determined ones. The highest level of consistency between the rotational constants is observed at the MP2/aug-cc-pVDZ level with deviations in the range of 0.2-2.5 \%. Comparing the calculated $V_{3}$ values with the experimentally determined
ones, the highest consistency is observed at the B3LYP/aug-cc-pVTZ level with some disagreements for $N$ - and $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$, as described in previous paragraphs.

Table 7.8. Comparison of calculated and experimentally determined $V_{3}$ barriers for $N-$, 2-, $4-$, and $5-\mathrm{MI}$ and $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$.

|  | $N$-MI | 2-MI | 4-MI | 5-MI |
| :---: | :---: | :---: | :---: | :---: |
| $V_{3}^{\text {XIAM }}\left(\mathrm{cm}^{-1}\right)^{\text {a }}$ | 185.104(11) ${ }^{\text {b }}$ | 122.7529(38) | 317.20(14) | 386.001(19) |
| $V_{3}^{B 3 L Y P}\left(\mathrm{~cm}^{-1}\right)^{\text {c }}$ | 189.74 | 115.28 | 295.17 | 376.57 |
|  | $N-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | 2-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ | 4-MI ${ }^{\text {H }} \mathrm{H}_{2} \mathrm{O}$ | 5-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ |
| $V_{3}^{\text {XIAM }}\left(\mathrm{cm}^{-1}\right)$ | 210.611(46) | 154.1193(50) | 321.05(11) | 380.230(54) |
| $V_{3}^{B 3 L Y P}\left(\mathrm{~cm}^{-1}\right)$ | 185.01 | 173.38 | 244.18 | 363.61 |

${ }^{\mathrm{a}}$ Experimental values.
${ }^{\mathrm{b}}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
${ }^{c}$ Calculated values at the B3LYP(D3BJ)/aug-cc-pVTZ level.


Figure 7.6. Resonance canonicals of the 4- and 5-MI tautomeric pair. Based on the calculated electric dipole moments and the relative intensity of the two molecules in the spectra, 4-MI is more abundant than 5-MI in the gas phase.

Table 7.9. Percentage deviations of calculated rotational constants and $V_{3}$ barrier heights from experimentally determined ones.
Deviations calculated by means of $\frac{A_{\text {calc }}-A_{\text {exp }}}{A_{\text {exp }}} \times 100$. (Continues to table 4)

|  | B3LYP(D3BJ)/aug-cc-pVTZ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $N-\mathrm{MI} \cdots{ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  | 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ |  | 4-MI ${ }^{-\mathrm{H}_{2} \mathrm{O}}$ |  | 5-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ |  |
| $A_{e}$ (MHz) | 5754.89 | 12.9 \% | 4183.14 | -1.31 \% | 3812.17 | -7.14 \% | 7574.94 | $-11.43 \%$ |
| $B_{e}(\mathrm{MHz})$ | 1313.14 | -7.4\% | 1769.10 | 2.0 \% | 1752.87 | 2.60 \% | 1183.73 | 1.37 \% |
| $C_{e}(\mathrm{MHz})$ | 1079.70 | -2.6\% | 1255.94 | 1.2 \% | 1216.30 | 0.16 \% | 1033.88 | 0.10 \% |
| $V_{3}\left(\mathrm{~cm}^{-1}\right)$ | 185.01 | -13.84\% | 173.38 | 11.11 \% | 244.18 | -31.48\% | 363.61 | -4.57\% |
| MP2/aug-cc-pVDZ |  |  |  |  |  |  |  |  |
|  | $N-\mathrm{MI}{ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  | 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ |  | 4-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ |  | 5-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ |  |
| $A_{e}$ (MHz) | 5034.14 | 0.39 \% | 4149.27 | 0.26 \% | 3987.81 | -2.43 \% | 8291.84 | -1.80\% |
| $B_{e}(\mathrm{MHz})$ | 1424.65 | 1.1 \% | 1739.08 | 0.31 \% | 1714.32 | 0.41 \% | 1164.63 | -0.25\% |
| $C_{e}(\mathrm{MHz})$ | 1121.24 | 1.2 \% | 1243.81 | 0.28 \% | 1215.47 | 0.10 \% | 1030.84 | -0.20 \% |
| $V_{3}\left(\mathrm{~cm}^{-1}\right)$ | 185.58 | -13.49\% | 121.18 | -27.18\% | 241.29 | -33.06\% | 344.28 | -10.44 \% |

Table 7.10. Percentage deviations of calculated rotational constants and $V_{3}$ barrier heights from experimentally determined ones.
Deviations calculated by means of $\frac{A_{\text {calc }}-A_{\text {exp }}}{A_{\text {exp }}} \times 100$.

|  | $N-\mathrm{MI}{ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  | 2-MI ${ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  | 4-MI ${ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  | 5-MI ${ }^{-} \mathrm{H}_{2} \mathrm{O}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\omega \mathrm{B97X}$-D/aug-cc-pVQZ |  |  |  |  |  |  |  |
| $A_{e}(\mathrm{MHz})$ | 6111.37 | 17.94 \% | 4197.93 | -0.96 \% | 3993.46 | -2.27 \% | 7828.8 | -7.82 \% |
| $B_{e}(\mathrm{MHz})$ | 1277.08 | -10.40 \% | 1758.92 | 1.43 \% | 1740.95 | 1.93 \% | 1176.29 | 0.74 \% |
| $C_{e}(\mathrm{MHz})$ | 1067.08 | -3.77\% | 1252.42 | 0.97 \% | 1230.17 | 1.29 \% | 1032.29 | -0.06 \% |
| $V_{3}\left(\mathrm{~cm}^{-1}\right)$ | 230.02 | 24.33\% | 223.09 | 28.67\% | 289.06 | 18.38\% | 384.68 | 5.80\% |

### 7.8 Conclusions

The microwave spectra of $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ monohydrate complexes were recorded in the $7.0-18.5 \mathrm{GHz}$ frequency range with CP-FTMW spectrometer at Newcastle University. The geometry of $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ is consistent with that determined for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ in chapter 5, meaning the pyridinic N 3 nitrogen is involved in the intermolecular hydrogen bond. Alternative isomers of the monohydrates, $\mathrm{H}_{2} \mathrm{O} \cdots 2$-MI, $\mathrm{H}_{2} \mathrm{O} \cdots 4-\mathrm{MI}$ and $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ were not observed under the current experimental conditions. Internal rotation of the $\mathrm{CH}_{3}$ group occurs at the timescale of the experiment and couples the overall rotation resulting in splitting of the energy levels into $A$ - and $E$-states. Spectrocopic parameters including rotational, centrifugal and nuclear quadrupole coupling constants were determined through fitting of $A$-state transitions. Global fits including both $A$ - and $E$-state transitions were perfomormed and internal rotation paramaters were determined. The $V_{3}$ barriers to internal rotation in these complexes vary significantly from one another and these values are dependent on the position where the $\mathrm{CH}_{3}$ group substitutes on the imidazole ring. Attachment of $\mathrm{H}_{2} \mathrm{O}$ on methylimidazole via a primary hydrogen bond at the N3 position does not significantly affects the $V_{3}$ in 4 - and 5-MI. More profound effects are observed for N - and 2-MI upon $\mathrm{H}_{2} \mathrm{O}$ attachment at the N 3 position. The variation in $V_{3}$ is driven by electronic effects propagating across the aromatic system and steric factors around the immediate environment of each $\mathrm{CH}_{3}$. The geometry of $N$-, 2, 4 -, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ is consistent with that determined for $\mathrm{imid} \cdots \mathrm{H}_{2} \mathrm{O}$ in chapter 5 , meaning the pyridinic N3 nitrogen is involved in the intermolecular hydrogen bond. Alternative isomers of the monohydrates, $\mathrm{H}_{2} \mathrm{O} \cdots 2-\mathrm{MI}, \mathrm{H}_{2} \mathrm{O} \cdots 4-\mathrm{MI}$ and $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ were not observed under the current experimental conditions.

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## Chapter 8. Overview, Conclusions and Future Work

The CP-FTMW spectrometer at Newcastle University was used to record the microwave spectra of phosphine carboxamide and phosphine carboxaminde-argon (chapter 4), two isomers of a complex between imidazole and water (chapter 5), isomers of methylimidazole (chapter 6) and microsolvated methylimidazole complexes with water (chapter 7) in the $7.0-18.5 \mathrm{GHz}$ frequency range. This work focuses on probing weak intermolecular interactions and internal motions in molecules and complexes by means of gas phase microwave spectroscopy. The species of interest are generated through supersonic gas expansion in conjunction with laser ablation methods.

In chapter 4, the spectrum of phosphine carboxamide (PCA), a phosphorus-bearing analogue of urea, was recorded for the first time with MW spectroscopy. The molecule was synthesized in the group of Prof Jose M. Goichoechea at Oxford University. ${ }^{1}$ Despite it being a primary phosphine, which are typically known for being hard to handle, it was stable at room temperature. Laser ablation was used to vaporize PCA from a solid target prior to in interaction with MW chirped pulses. Detection of ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ isotopologues of PCA in their natural isotopic abundance allowed for determination of the atomic coordinates of C and N , which are in good agreement with the previously determined crystal structure and DFT calculations. The H atoms at the $\mathrm{PH}_{2}$ site adopt a steeply pyramidal arrangement both in the crystal and gas phase PCA. The $\mathrm{NH}_{2}$ site configuration is consistent with that observed for urea at the zero point. ${ }^{2,3}$ Recording the spectra of deuterated isotopologues of PCA would give a more accurate insight into the $\mathrm{PH}_{2}$ and $\mathrm{NH}_{2}$ sites. Experiments with ${ }^{18} \mathrm{O}-\mathrm{PCA}$ are likely to be to be harder but would allow to experimentally measure the carbonyl length. Attachment of an Ar atom onto PCA follows the broad trend that has been observed for various van der Waals complexes between an organic molecule and Ar ; the Ar atom coordinates at the point where the electronic on the organic molecule is concentrated.

Two isomers of a complex between imidazole and water ${ }^{4}$ (imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\left.\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{imid}\right)$ were discussed in chapter 5. Imidazole has two chemically distinct nitrogen atoms, pyrrolic (N1) and pyridinic (N3), which can act either as a proton donor or a proton acceptor, respectively. A hydrogen bond is formed between the nitrogen atoms of imidazole and the oxygen or hydrogen of water. Large amplitude internal motions associated with the water subunit were detected in the spectra of the $\mathrm{H}_{2} \mathrm{O}$ imid complex. The intermolecular hydrogen bond in imid $\cdots \mathrm{H}_{2} \mathrm{O}$ is non-linear as an outcome of secondary long-range interactions at the O atom. In $\mathrm{H}_{2} \mathrm{O}$ imid, the intermolecular hydrogen also slightly
deviates from linearity as the chemical environment around the $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ bond is not symmetric.

The barriers to internal rotation of the $\mathrm{CH}_{3}$ groups in methylimidazole isomers ${ }^{5}$ were determined and discussed in chapter 6. To the author's best knowledge this is the first comparative study of their $V_{3}$ barriers and the first time their spectra are reported in the 7.018.5 GHz frequency range. A correlation between the height of the barrier and the position where the $\mathrm{CH}_{3}$ group substitutes on the ring was observed. The trend agrees with previous studies of methylthiazole and methyloxazole isomers where two heteroatoms are present in the ring and separated by a C atom. Consistently, the lowest and highest barriers are observed for each 2-methyl- and 5-methyl-analogues, respectively. The variation in the barrier arises from a combination of steric and electronic effects.

Complexes between methylimidazole isomers and water were reported in chapter 7. The scope of that chapter explored the effect of microsolvation on the $V_{3}$ barrier height of each methylimidazole isomer. Internal rotation if further hindered upon complex formation of N - and 2-methylimidazole with water while for 4 - and 5-methylimidazole only subtle changes are observed. The increase in the barrier of the former two isomers was rationalized in terms of steric and electronic effects around the $\mathrm{CH}_{3}$ environment. It appears that attachment of one water molecule preserves the general barrier height trend which is dependent on the position where the $\mathrm{CH}_{3}$ group substitutes on the ring; 2methylimidazole $\cdots \mathrm{H}_{2} \mathrm{O}$ exhibits the lowest barrier and 5-methylimidazole $\cdots \mathrm{H}_{2} \mathrm{O}$ the lowest barrier.

In previous works, the Newcastle group has reported the benefits of using copper or silver iodide ${ }^{6-8}$ as a binder in conjunction with an organic precursor for formation of rods to be used with laser ablation. In this work, the use of new binding materials was explored. Zinc powder was used with PCA as a more affordable alternative to copper and silver iodide. Given that copper powder may ignite and considering the potential risk of releasing $\mathrm{PH}_{3}$ whilst handling PCA, zinc was deemed as a safer alternative for that experiment. It is worth exploring the effect that copper may have on the signal intensity of PCA and whether it prompts formation of more fragmentation products by acting as a catalyst during laser ablation. However, for that matter, more PCA need to be synthesized and transported to Newcastle University which has not been possible during the pandemic. In chapter 6, it was also reported that $\mathrm{MgSO}_{4}$ can be mixed with copper and hygroscopic organic substances or substances with low melting points prior to rod formation, i.e. 4(5)-
methylimidazole. $\mathrm{MgSO}_{4}$ combined with copper powder was also used for various experiments which are not reported here and successfully allowed us to measure their spectra, i.e. pyrazole, serinol, $N, N$-dimethylserinol which are all hygroscopic.

It is worth exploring the formation higher microsolvated clusters of methylimidazole isomers and rationalize the effect on the barrier height. It is also important to establish which intermolecular interactions are fundamental and drive the shape of each microsolvated cluster. Across the different methylimidazole isomers, different positions are available for hydrogen bonding of the type $\mathrm{C}-\mathrm{H} \cdots \mathrm{O}$ and as such the shape of the microsolavated clusters is expected to vary. Hydrogen bond cooperativity has been observed in water clusters $\left[\left(\mathrm{H}_{2} \mathrm{O}\right)_{\mathrm{n}}, n=2,3, \ldots, 10\right] .{ }^{9-16} \mathrm{~A}$ key point about future studies would be whether the water molecules in the microsolvated cluster maintain the arrangement observed in the free-water clusters. It also important to determine the highest microsolvated methylimidazole cluster that can be detected with MW spectroscopy.

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## Appendix A

Complete lists of calculated and experimental (where available) atomic coordinates of the molecules and complexes discussed in this thesis may be found here. The tables are organized such that the order of molecules or complexes follows the order in which they appear in the main thesis body. Other information that cannot be embedded in the main chapters are also summarized here.

Table A1. PCA (Chapter 4), B3LYP(D3BJ)/aug-cc-pVTZ

|  |  | PCA |  |
| :---: | :---: | :---: | :---: |
|  | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| O 1 | -1.094458 | -1.167516 | -0.000935 |
| C 1 | -0.550289 | -0.083719 | 0.020713 |
| N 3 | -1.230127 | 1.093383 | -0.008232 |
| $\mathrm{H}_{\mathrm{N} 1}$ | -2.237238 | 1.063770 | -0.014605 |
| $\mathrm{H}_{\mathrm{N} 2}$ | -0.770800 | 1.976956 | 0.111132 |
| P 4 | 1.333920 | 0.029060 | -0.063484 |
| $\mathrm{H}_{\mathrm{P} 1}$ | 1.529555 | -0.824327 | 1.047635 |
| $\mathrm{H}_{\mathrm{P} 2}$ | 1.496605 | 1.224800 | 0.689504 |

Table A2. PCA " Ar (Chapter 4), B3LYP(D3BJ)/aug-cc-pVTZ

|  | $\mathrm{PCA} \cdots \mathrm{Ar}$ |  |  |
| :---: | :---: | :---: | :---: |
|  | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| O 1 | 0.843774 | -1.128886 | -1.182195 |
| C 1 | 1.077455 | -0.639920 | -0.096916 |
| N 3 | 0.905107 | -1.307179 | 1.074269 |
| $\mathrm{H}_{\mathrm{N} 1}$ | 0.582815 | -2.261047 | 1.039542 |
| $\mathrm{H}_{\mathrm{N} 2}$ | 1.177062 | -0.916460 | 1.956914 |
| P 4 | 1.560270 | 1.181292 | 0.033603 |
| $\mathrm{H}_{\mathrm{P} 1}$ | 2.642825 | 1.058020 | -0.868845 |
| $\mathrm{H}_{\mathrm{P} 2}$ | 2.377451 | 1.089091 | 1.194166 |
| Ar | -2.358731 | 0.212435 | 0.016026 |

Table A3. Some experimentally $\left(r_{0}, r_{s}\right)$ and calculated $\left(r_{e}\right)$ structural parameters for PCA as well as some structural parameters from X-ray crystallography. Parameters for the structural analogues urea and thiourea are also summarized.

|  | PCA |  |  |  | Urea |  | Thiourea |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $r_{s}$ | $r_{0}$ | $r_{e}$ | X-ray | $r_{s} / r_{0}$ | $r_{e}$ | $r_{s}$ | $r_{e}$ |
| $r(N-C)$ | $1.346(23)$ | $1.3329(15)$ | 1.360 | $1.329(2)$ | 1.3779 | 1.3911 | $1.368(3)$ | 1.3640 |
| $r(P-C)$ | - | - | 1.900 | $1.865(1)$ | - | - | - | - |
| $r(C-O)$ | - | - | 1.213 | $1.230(2)$ | 1.2211 | 1.2179 | - | - |
| $r(C-S)$ | - | - | - | - | - | - | $1.645(4)$ | 1.6480 |
| $r\left(P-H_{1}\right)$ | - | - | 1.4146 | $1.27(2)$ | - | - | - | - |
| $r\left(P-H_{2}\right)$ | - | - | 1.4224 | $1.30(2)$ | - | - | - | - |
| $r\left(N-H_{1}\right)$ | - | - | 1.0030 | $0.85(2)$ | 0.9978 | 1.0099 | - | 1.0058 |
| $r\left(N-H_{2}\right)$ | - | - | 1.0076 | $0.88(2)$ | 1.0212 | 1.0100 | - | 1.0075 |
| $\angle(N-C-P)$ | - | $117(2)^{\circ}$ | 116.50 | $117.3(1)$ | - | - | - | - |
| $\angle(N-C-N)$ | - | - | - | - | 114.71 | 113.11 | - | - |
| $\angle(N-C-O)$ | - | $126.4(6)^{\circ}$ | 123.30 | $124.1(1)$ | 122.64 | 123.45 | - | - |
| $\angle(N-C-S)$ | - | - | - | - | - | - | $123.0(2)$ | 123.07 |

Table A4. Imidazole-water (Chapter 5)

| B3LYP(D3BJ) |  | imid $\cdots \mathrm{H}_{2} \mathrm{O}$ |  |
| :---: | :---: | :---: | :---: |
| /aug-cc-pVTZ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
|  | -1.615374 | 0.806280 | -0.019777 |
| N 1 | -2.295863 | 1.544682 | -0.048017 |
| H 1 | -0.266459 | 0.960219 | 0.040607 |
| C 2 | 0.217182 | 1.921485 | 0.063646 |
| H 2 | 0.337720 | -0.204622 | 0.060796 |
| N 3 | -0.657821 | -1.152979 | 0.010598 |
| C 4 | -0.434988 | -2.205138 | 0.010900 |
| H 4 | -1.880242 | -0.545453 | -0.039670 |
| C 5 | -2.880648 | -0.933539 | -0.087331 |
| H 5 | 2.239001 | -0.154897 | -0.009942 |
| $\mathrm{H}_{\mathrm{b}}$ | 3.195103 | 0.037564 | -0.084533 |
| O | 3.591841 | -0.338637 | 0.705064 |
| $\mathrm{H}_{\mathrm{nb}}$ |  | $\mathrm{imid} \cdots \mathrm{H}_{2} \mathrm{O}$ |  |
| $\omega \mathrm{B} 97 \mathrm{XD} / \mathrm{aug}-$ |  |  |  |
| $\mathrm{cc}-\mathrm{pVQZ}$ |  | $b / \AA$ | $-0 . \AA / \AA$ |
|  | -1.622908 | -0.800110 | -0.013285 |
| N 1 | -2.301568 | -1.537156 | -0.038116 |
| H 1 | -0.280639 | -0.952715 | 0.041072 |
| C 2 | 0.201260 | -1.915388 | 0.064178 |
| H 2 | 0.327091 | 0.203692 | 0.057305 |
| N 3 | -0.664420 | 1.147949 | 0.010111 |
| C 4 | -0.443213 | 2.200765 | 0.008406 |
| H 4 | -1.883636 | 0.545509 | -0.033524 |
| C 5 | -2.881975 | 0.939680 | -0.078315 |
| H 5 | 2.253901 | 0.141020 | -0.054538 |
| $\mathrm{H}_{\mathrm{b}}$ | 3.203723 | -0.048453 | -0.124829 |
|  | 0.289172 | 0.682930 |  |

Table A5. Water-imidazole (Chapter 5)

| $\begin{gathered} \hline \hline \text { B3LYP(D3BJ) } \\ \text { /aug-cc-pVTZ } \end{gathered}$ | $\mathrm{H}_{2} \mathrm{O}$ - imid |  |  |
| :---: | :---: | :---: | :---: |
|  | $a / \AA{ }^{\text {a }}$ | b/Å | $c / \AA$ |
| N1 | -0.256587 | -0.022689 | -0.000509 |
| H1 | -1.268207 | $-0.016502$ | -0.000985 |
| C2 | 0.559694 | 1.065756 | -0.000144 |
| H2 | 0.178600 | 2.073051 | -0.000169 |
| N3 | 1.827879 | 0.723135 | 0.000329 |
| C4 | 1.834559 | -0.652136 | 0.000255 |
| H4 | 2.754350 | -1.211039 | 0.000657 |
| C5 | 0.552955 | -1.133820 | -0.000238 |
| H5 | 0.178600 | 2.073051 | -0.000169 |
| H | -3.787567 | 0.135023 | -0.766216 |
| O | -3.224258 | -0.008568 | 0.000097 |
| H | -3.784036 | 0.130190 | 0.769885 |
| $\begin{gathered} \omega \text { B97XD/aug- } \\ \text { cc-pVQZ } \end{gathered}$ |  | $\mathrm{H}_{2} \mathrm{O} \cdots$ imid |  |
|  | $a / \AA$ ¢ | $b / \AA$ | $c / \AA$ |
| N1 | -0.192148 | 0.081550 | 0.000004 |
| H1 | -1.201279 | 0.141483 | 0.000026 |
| C2 | 0.536766 | $-1.058420$ | 0.000019 |
| H2 | 0.077839 | -2.033225 | 0.000060 |
| N3 | 1.822306 | -0.820108 | -0.000022 |
| C4 | 1.931681 | 0.545367 | -0.000062 |
| H4 | -1.201279 | 0.141483 | 0.000026 |
| C5 | 0.696116 | 1.122257 | -0.000047 |
| H5 | 0.377954 | 2.148809 | -0.000070 |
| H | -3.657410 | -0.200079 | -0.763499 |
| O | -3.153620 | 0.077918 | 0.000070 |
| H | -3.657362 | -0.200038 | 0.763686 |

Table A6. Calculated atomic coordinates and residuals for the alternative, experimentally determined, fitted geometries of imid $\cdots \mathrm{H}_{2} \mathrm{O}$ described under "Molecular Geometry". The geometry determined while assuming $\angle\left(\mathrm{H}_{\mathrm{nb}}-\mathrm{O}-\mathrm{H}_{\mathrm{b}} \cdots \mathrm{N} 3\right)=180^{\circ}, \angle\left(\mathrm{O}-\mathrm{H}_{b} \cdots \mathrm{~N} 3-\mathrm{C} 2\right)=0^{\circ}$ leads to the parameters and coordinates displayed in Tables xx and xx. All c-coordinates are constrained to zero by the assumption that the molecule is planar.

|  | $\mathrm{imid} \cdots \mathrm{H}_{2} \mathrm{O}\left(\angle\left(\mathrm{H}_{\mathrm{nb}}-\mathrm{O}-\mathrm{H}_{\mathrm{b}} \cdots \mathrm{N} 3\right)=180^{\circ}, \angle\left(\mathrm{O}-\mathrm{H}_{\mathrm{b}} \cdots \mathrm{N} 3-\mathrm{C} 2\right)=0^{\circ}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $a / \AA$ | $d a / \AA$ | $b / \AA$ | $d b / \AA$ |
| N 1 | -1.327352 | 0.03877 | -1.007995 | 0.01910 |
| H 1 | -1.739547 | 0.07363 | -1.916895 | 0.03491 |
| C 2 | 0.008189 | 0.02808 | -0.729346 | 0.03212 |
| H 2 | 0.756980 | 0.05787 | -1.505955 | 0.06083 |
| N 3 | 0.240898 | 0.02150 | 0.563375 | 0.04104 |
| C 4 | -1.010423 | 0.04401 | 1.150464 | 0.00695 |
| H 4 | -1.119783 | 0.08512 | 2.222400 | 0.01114 |
| C 5 | -1.988557 | 0.00756 | 0.200093 | 0.04446 |
| H 5 | -3.064932 | 0.01016 | 0.267765 | 0.08574 |
| O | 3.150931 | 0.00196 | -0.077040 | 0.00062 |
| $\mathrm{H}_{\mathrm{b}}$ | 2.230131 | 0.00531 | 0.187332 | 0.02450 |
| $\mathrm{H}_{\mathrm{nb}}$ | 3.635990 | 0.02058 | 0.749084 | 0.01376 |


| $\mathrm{imid} \cdots \mathrm{H}_{2} \mathrm{O}\left(\square\left(\mathrm{H}_{\mathrm{nb}}-\mathrm{O}-\mathrm{H}_{\mathrm{b}} \cdots \mathrm{N} 3\right)=180^{\circ}, \square\left(\mathrm{O}-\mathrm{H}_{\mathrm{b}} \cdots \mathrm{N} 3-\mathrm{C} 2\right)=180^{\circ}\right)$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| N 1 | $a / \AA$ | $d a / \AA$ | $b / \AA$ | $d b / \AA$ |
| H 1 | -1.332272 | 0.04004 | -1.006938 | 0.01996 |
| C 2 | 0.004611 | 0.02924 | -0.734802 | 0.03313 |
| H 2 | 0.243618 | 0.02205 | 0.556769 | 0.04262 |
| N 3 | -1.004826 | 0.04561 | 1.149950 | 0.00695 |
| C 4 | -1.987581 | 0.00806 | 0.204359 | 0.04598 |
| H 4 | -1.748893 | 0.07606 | -1.913818 | 0.03650 |
| C 5 | 0.749607 | 0.06022 | -1.515053 | 0.06271 |
| H 5 | -1.108959 | 0.08819 | 2.222407 | 0.01109 |
| O | -3.063613 | 0.01095 | 0.277276 | 0.08871 |
| $\mathrm{H}_{\mathrm{b}}$ | 3.151083 | 0.00203 | 0.050184 | 0.00056 |
| $\mathrm{H}_{\mathrm{nb}}$ | 2.229504 | 0.00543 | -0.211456 | 0.02547 |

Table A7. N-MI (Chapter 6), B3LYP(D3BJ)/aug-cc-pVTZ

| $N-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.671589 | -0.010546 | -0.000257 |
| C 2 | 0.164773 | 1.065843 | 0.000059 |
| H 2 | -0.208941 | 2.076622 | -0.000491 |
| N 3 | 1.427750 | 0.708278 | 0.000040 |
| C 4 | 1.417344 | -0.665138 | 0.000081 |
| H 4 | 2.329221 | -1.236962 | -0.000145 |
| C 5 | 0.129453 | -1.130294 | 0.000008 |
| H 5 | -0.282531 | -2.123332 | -0.000186 |
| C 6 | -2.119924 | 0.015399 | 0.000135 |
| H 6 | -2.453094 | 1.050263 | -0.002045 |
| H 6 | -2.514527 | -0.480577 | -0.886250 |
| H 6 | -2.514275 | -0.476812 | 0.888769 |

Table A8. N-MI (Chapter 6), B3LYP(D3BJ)/cc-pVTZ

| $N-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.671716 | -0.010801 | -0.000259 |
| C 2 | 0.165565 | 1.065244 | 0.000142 |
| H 2 | -0.208824 | 2.075956 | -0.000233 |
| N 3 | 1.428222 | 0.708301 | 0.000038 |
| C 4 | 1.416403 | -0.665106 | -0.000078 |
| H 4 | 2.328243 | -1.237354 | -0.000319 |
| C 5 | 0.129042 | -1.130662 | 0.000150 |
| H 5 | -0.283701 | -2.123456 | 0.000343 |
| C 6 | -2.119452 | 0.016375 | 0.000045 |
| H 6 | -2.452444 | 1.051497 | -0.001406 |
| H 6 | -2.515673 | -0.478611 | -0.886406 |
| H 6 | -2.515513 | -0.476082 | 0.888006 |

Table A9. N-MI (Chapter 6), B3LYP(D3BJ)/Def2-TZVP

| $N-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.671580 | -0.010651 | -0.000350 |
| C 2 | 0.165044 | 1.065510 | 0.000129 |
| H 2 | -0.208776 | 2.077409 | -0.000328 |
| N 3 | 1.427498 | 0.708010 | 0.000067 |
| C 4 | 1.416946 | -0.664774 | -0.000048 |
| H 4 | 2.329613 | -1.237322 | -0.000232 |
| C5 | 0.129039 | -1.130336 | 0.000125 |
| H5 | -0.283438 | -2.124228 | 0.000315 |
| C6 | -2.119070 | 0.015762 | 0.000107 |
| H 6 | -2.452585 | 1.051614 | -0.001897 |
| H 6 | -2.514816 | -0.480400 | -0.886989 |
| H6 | -2.514511 | -0.476887 | 0.889334 |

Table A10. 2-MI (Chapter 6), B3LYP(D3BJ)/aug-cc-pVTZ

| 2-MI | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N1 | 0.131449 | -1.069486 | -0.000246 |
| H1 | -0.187075 | -2.022056 | 0.000731 |
| C2 | -0.659470 | 0.045650 | -0.000267 |
| N3 | 0.079149 | 1.132386 | -0.000138 |
| C4 | 1.389822 | 0.708437 | 0.000168 |
| H4 | 2.207784 | 1.407596 | 0.000088 |
| C5 | 1.447651 | -0.655045 | 0.000191 |
| H5 | 2.268020 | -1.349010 | 0.000022 |
| C6 | -2.146268 | -0.005266 | 0.000201 |
| H6 | -2.532377 | -0.527768 | -0.877458 |
| H6 | -2.532391 | -0.511186 | 0.887578 |
| H6 | -2.527935 | 1.011894 | -0.009134 |

Table A11. 2-MI (Chapter 6), B3LYP(D3BJ)/cc-pVTZ

| 2-MI | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N1 | 0.132006 | -1.069709 | -0.000250 |
| H1 | -0.186108 | -2.022520 | 0.000665 |
| C2 | -0.658611 | 0.045462 | -0.000278 |
| N3 | 0.078490 | 1.133078 | -0.000147 |
| C4 | 1.388509 | 0.708635 | 0.000181 |
| H4 | 2.206618 | 1.407943 | 0.000055 |
| C5 | 1.447504 | -0.654875 | 0.000201 |
| H5 | 2.268336 | -1.348418 | 0.000050 |
| C6 | -2.145654 | -0.005896 | 0.000213 |
| H6 | -2.526469 | 1.011601 | -0.010825 |
| H6 | -2.532471 | -0.529918 | -0.876508 |
| H6 | 2.532635 | -0.510393 | 0.888310 |

Table A12. 2-MI (Chapter 6), B3LYP(D3BJ)/Def2-TZVP

| 2-MI | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N1 | 0.131648 | -1.069531 | -0.000302 |
| H1 | -0.186776 | -2.023007 | 0.000390 |
| C2 | -0.658666 | 0.045679 | -0.000304 |
| N3 | 0.078912 | 1.132745 | -0.000213 |
| C4 | 1.388741 | 0.708580 | 0.000197 |
| H4 | 2.207303 | 1.408626 | 0.000217 |
| C5 | 1.447159 | -0.655132 | 0.000257 |
| H5 | 2.268458 | -1.349578 | 0.000197 |
| C6 | -2.145571 | -0.005609 | 0.000271 |
| H6 | -2.527224 | 1.012570 | -0.008665 |
| H6 | -2.532290 | -0.528198 | -0.878396 |
| H6 | -2.532082 | -0.512237 | 0.888387 |

Table A13. 4-MI (Chapter 6), B3LYP(D3BJ)/aug-cc-pVTZ

| $4-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N1 | 1.422668 | -0.604647 | 0.000132 |
| H1 | 2.278863 | -1.129297 | -0.000699 |
| C2 | 1.303572 | 0.750978 | -0.000095 |
| H2 | 2.156988 | 1.407971 | 0.000231 |
| N3 | 0.045917 | 1.119184 | 0.000021 |
| C4 | -0.696509 | -0.044770 | -0.000031 |
| C5 | 0.144606 | -1.125349 | -0.000020 |
| H5 | -0.042055 | -2.183755 | -0.000015 |
| C6 | -2.185769 | -0.019663 | 0.000019 |
| H6 | -2.594856 | -1.029204 | -0.001738 |
| H6 | -2.564317 | 0.503578 | 0.879385 |
| H6 | -2.564072 | 0.506298 | -0.877793 |

Table A14. 4-MI (Chapter 6), B3LYP(D3BJ)/cc-pVTZ

| 4-MI | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N1 | 1.422640 | -0.604419 | 0.000246 |
| H1 | 2.278803 | -1.129241 | -0.000810 |
| C2 | 1.302572 | 0.750890 | -0.000068 |
| H2 | 2.156133 | 1.408001 | 0.000386 |
| N3 | 0.045161 | 1.119848 | -0.000066 |
| C4 | -0.695608 | -0.044562 | -0.000069 |
| C5 | 0.145180 | -1.125402 | -0.000153 |
| H5 | -0.041518 | -2.183834 | 0.000017 |
| C6 | -2.185281 | -0.020537 | 0.000090 |
| H6 | -2.594442 | -1.030212 | -0.002411 |
| H6 | -2.564520 | 0.501992 | 0.501992 |
| H6 | -2.564470 | 0.506126 | -0.877099 |

Table A15. 4-MI (Chapter 6), B3LYP(D3BJ)/Def2-TZVP

| $4-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.422527 | -0.604166 | 0.000059 |
| H 1 | 2.279163 | -1.129527 | -0.000338 |
| C 2 | 1.302864 | 0.750952 | -0.000104 |
| H 2 | 2.156847 | 1.409092 | 0.000058 |
| N 3 | 0.045349 | 1.119059 | 0.000069 |
| C 4 | -0.696080 | -0.044412 | -0.000006 |
| C5 | 0.145375 | -1.125355 | 0.000029 |
| H 5 | -0.041358 | -2.184773 | -0.000037 |
| C6 | -2.185471 | -0.020159 | -0.000012 |
| H 6 | -2.594045 | -1.031030 | -0.000857 |
| H 6 | -2.564950 | 0.503925 | 0.879647 |
| H 6 | -2.564637 | 0.505002 | -0.879144 |

Table A16. 5-MI (Chapter 6), B3LYP(D3BJ)/aug-cc-pVTZ

| $5-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.085541 | -1.055933 | -0.000258 |
| H 1 | 0.240684 | -2.006276 | 0.001134 |
| C 2 | -1.389786 | -0.648393 | 0.000137 |
| H 2 | -2.213010 | -1.342822 | -0.000013 |
| N 3 | -1.478914 | 0.656782 | 0.000271 |
| C 4 | -0.179216 | 1.115247 | -0.000172 |
| H 4 | 0.046878 | 2.168033 | -0.000131 |
| C 5 | 0.708947 | 0.073143 | -0.000510 |
| C 6 | 2.194976 | 0.020924 | 0.000303 |
| H 6 | 2.584868 | -0.490467 | 0.883702 |
| H 6 | 2.586135 | -0.493480 | -0.880801 |
| H 6 | 2.596860 | 1.032181 | -0.001206 |

Table A17. 5-MI (Chapter 6), B3LYP(D3BJ)/cc-pVTZ

| $5-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.084959 | -1.056188 | -0.000428 |
| H 1 | 0.242420 | -2.006225 | 0.001548 |
| C 2 | -1.388716 | -0.648637 | 0.000284 |
| H 2 | -2.211627 | -1.343694 | 0.000129 |
| N 3 | -1.479597 | 0.656697 | 0.000256 |
| C 4 | -0.180308 | 1.114604 | -0.000191 |
| H 4 | 0.045975 | 2.167506 | -0.000080 |
| C 5 | 0.708751 | 0.073209 | -0.000585 |
| C 6 | 2.194955 | 0.021959 | 0.000355 |
| H 6 | 2.596844 | 1.033320 | 0.000595 |
| H 6 | 2.585605 | -0.490642 | 0.882960 |
| H 6 | 2.587455 | -0.490944 | -0.881132 |

Table A18. 5-MI (Chapter 6), B3LYP(D3BJ)/Def2-TZVP

| $5-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.085141 | -1.055727 | -0.000285 |
| H 1 | 0.242194 | -2.006535 | 0.001425 |
| C 2 | -1.388927 | -0.648654 | 0.000132 |
| H 2 | -2.212946 | -1.343926 | -0.000097 |
| N 3 | -1.478849 | 0.656354 | 0.000306 |
| C 4 | -0.180429 | 1.115091 | -0.000173 |
| H 4 | 0.045781 | 2.168924 | -0.000224 |
| C 5 | 0.708738 | 0.073166 | -0.000547 |
| C 6 | 2.194836 | 0.021422 | 0.000326 |
| H 6 | 2.596618 | 1.033744 | -0.000752 |
| H 6 | 2.585706 | -0.490500 | 0.884292 |
| H 6 | 2.586974 | -0.492715 | -0.881824 |

Table A19. N -MI $\cdots \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), B3LYP(D3BJ)/aug-cc-pVTZ

| $N-\mathrm{MI}^{\cdots} \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -1.330478 | 0.255040 | -0.000158 |
| C 2 | -0.043393 | 0.686423 | -0.052153 |
| H 2 | 0.218220 | 1.730760 | -0.082357 |
| N 3 | 0.804207 | -0.318391 | -0.054274 |
| C 4 | 0.037076 | -1.455940 | -0.000861 |
| H 4 | 0.479275 | -2.436560 | 0.012755 |
| C 5 | -1.288805 | -1.121664 | 0.032639 |
| H 5 | -2.183253 | -1.715961 | 0.076763 |
| C 6 | -2.521220 | 1.082404 | 0.020034 |
| H 6 | -2.223673 | 2.127296 | -0.009033 |
| H 6 | -3.148722 | 0.871611 | -0.845055 |
| H 6 | -3.094074 | 0.905843 | 0.929499 |
| O | 3.532356 | 0.543698 | 0.085819 |
| $\mathrm{H}_{\mathrm{b}}$ | 2.639465 | 0.148974 | 0.012775 |
| $\mathrm{H}_{\mathrm{nb}}$ | 4.004428 | 0.249346 | -0.697002 |

Table A20. $N$-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), $\omega$ B97XD/aug-cc-pVQZ

| $N-\mathrm{MI}_{\cdots} \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -1.357174 | -0.231787 | 0.008588 |
| C 2 | -0.099160 | -0.721263 | 0.062897 |
| H 2 | 0.107524 | -1.778352 | 0.101293 |
| N 3 | 0.796658 | 0.232451 | 0.061732 |
| C 4 | 0.087957 | 1.400243 | 0.001122 |
| H 4 | 0.576279 | 2.358912 | -0.015310 |
| C 5 | -1.247427 | 1.133689 | -0.033036 |
| H 5 | -2.110130 | 1.773649 | -0.079802 |
| C 6 | -2.581119 | -0.998193 | -0.035331 |
| H 6 | -2.347795 | -2.048243 | 0.119485 |
| H 6 | -3.260370 | -0.673033 | 0.750364 |
| H 6 | -3.070516 | -0.885539 | -1.001446 |
| O | 3.588113 | -0.506146 | -0.093761 |
| $\mathrm{H}_{\mathrm{b}}$ | 2.669123 | -0.195381 | -0.034050 |
| $\mathrm{H}_{\mathrm{nb}}$ | 3.997168 | -0.226173 | 0.722259 |

Table A21. N -MI ${ }^{\mathrm{H}} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), MP2/aug-cc-pVDZ

| $N-\mathrm{MI}^{\cdots} \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -1.250018 | 0.313323 | -0.002740 |
| C 2 | 0.083145 | 0.568578 | -0.053451 |
| H 2 | 0.485217 | 1.568292 | -0.086878 |
| N 3 | 0.795493 | -0.551020 | -0.049914 |
| C 4 | -0.123051 | -1.565507 | 0.005593 |
| H 4 | 0.174734 | -2.599887 | 0.022576 |
| C 5 | -1.400976 | -1.048537 | 0.035326 |
| H 5 | -2.371202 | -1.512340 | 0.079258 |
| C 6 | -2.313094 | 1.299515 | 0.013147 |
| H 6 | -1.866313 | 2.289075 | -0.027705 |
| H 6 | -2.963131 | 1.166356 | -0.848892 |
| H 6 | -2.896086 | 1.209756 | 0.927172 |
| O | 3.394397 | 0.612111 | 0.080198 |
| $\mathrm{H}_{\mathrm{b}}$ | 2.610614 | 0.032603 | 0.017017 |
| $\mathrm{H}_{\mathrm{nb}}$ | 3.967917 | 0.316053 | -0.631072 |

Table A22. 2-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), B3LYP(D3BJ)/aug-cc-pVTZ

| 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.603938 | -0.647532 | -0.015257 |
| H 1 | 2.190785 | -1.462578 | -0.033754 |
| C 2 | 0.240795 | -0.647284 | 0.012197 |
| N 3 | -0.206695 | 0.591265 | 0.028442 |
| C 4 | 0.898245 | 1.413602 | 0.009686 |
| H 4 | 0.804606 | 2.485060 | 0.015127 |
| C 5 | 2.036041 | 0.663316 | -0.017158 |
| H 5 | 3.077609 | 0.925265 | -0.037233 |
| C 6 | -0.588906 | -1.881515 | 0.015798 |
| H 6 | -1.638034 | -1.600982 | 0.062643 |
| H 6 | -0.427178 | -2.470469 | -0.889087 |
| H 6 | -0.356450 | -2.514454 | 0.874356 |
| O | -3.045496 | 0.564008 | -0.064429 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.081383 | 0.736065 | -0.013024 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.442650 | 1.113129 | 0.615955 |

Table A23. 2-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), $\omega$ B97XD/aug-cc-pVQZ

| 2-MI $\mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.610674 | -0.633079 | -0.001090 |
| H 1 | 2.201624 | -1.442578 | -0.005724 |
| C 2 | 0.254852 | -0.642298 | 0.012642 |
| N 3 | -0.207781 | 0.583735 | 0.014195 |
| C 4 | 0.886215 | 1.411753 | -0.001147 |
| H 4 | 0.782666 | 2.482594 | -0.005503 |
| C 5 | 2.027401 | 0.675993 | -0.010290 |
| H 5 | 3.066282 | 0.949231 | -0.020542 |
| C 6 | -0.560578 | -1.885871 | 0.004610 |
| H 6 | -1.606181 | -1.625183 | 0.146866 |
| H 6 | -0.463607 | -2.409208 | -0.947316 |
| H 6 | -0.254048 | -2.566814 | 0.798947 |
| O | -3.070668 | 0.553547 | -0.054869 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.110527 | 0.712036 | -0.029976 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.426471 | 1.044396 | 0.682725 |

Table A24. 2-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), MP2/aug-cc-pVDZ

| 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.583337 | 0.702515 | -0.000029 |
| H 1 | 2.129130 | 1.556638 | -0.000077 |
| C 2 | 0.211056 | 0.634247 | -0.000280 |
| N 3 | -0.182056 | -0.646256 | -0.000268 |
| C 4 | 0.973370 | -1.407665 | 0.000074 |
| H 4 | 0.943939 | -2.494831 | 0.000139 |
| C 5 | 2.091470 | -0.583319 | 0.000218 |
| H 5 | 3.158128 | -0.791355 | 0.000293 |
| C 6 | -0.684241 | 1.834555 | 0.000046 |
| H 6 | -1.728081 | 1.493961 | -0.004419 |
| H 6 | -0.519442 | 2.454772 | 0.895935 |
| H 6 | -0.513264 | 2.459848 | -0.891142 |
| O | -3.037817 | -0.563371 | 0.000392 |
| $\mathrm{H}_{\mathrm{b}}$ | -1.728081 | 1.493961 | -0.004419 |
| $\mathrm{H}_{\mathrm{nb}}$ | -2.084434 | -0.800073 | 0.000555 |

Table A25. 4-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), B3LYP(D3BJ)/aug-cc-pVTZ

| 4-MI $\mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.870120 | -0.868293 | -0.043074 |
| H 1 | 2.728321 | -1.387301 | -0.095133 |
| C 2 | 0.621837 | -1.389741 | 0.057352 |
| H 2 | 0.428439 | -2.448118 | 0.092281 |
| N 3 | -0.281032 | -0.438458 | 0.096908 |
| C 4 | 0.401381 | 0.759759 | 0.017047 |
| C 5 | 1.743010 | 0.506274 | -0.070759 |
| H 5 | 2.593341 | 1.158247 | -0.149572 |
| C 6 | -0.313427 | 2.065786 | 0.031183 |
| H 6 | 0.382815 | 2.892382 | -0.101688 |
| H 6 | -1.058570 | 2.105091 | -0.763686 |
| H 6 | -0.842013 | 2.209794 | 0.974676 |
| O | -3.140825 | -0.527326 | -0.118771 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.168511 | -0.535988 | -0.003616 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.501102 | -0.592596 | 0.769095 |

Table A26. 4-MI ${ }^{\prime} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), $\omega$ B97XD/aug-cc-pVQZ

| $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.941139 | -0.739671 | -0.061845 |
| H 1 | 2.838440 | -1.180048 | -0.130529 |
| C 2 | 0.753656 | -1.365743 | 0.074275 |
| H 2 | 0.659562 | -2.437288 | 0.124620 |
| N 3 | -0.229594 | -0.507434 | 0.130291 |
| C 4 | 0.338700 | 0.740064 | 0.023908 |
| C 5 | 1.689477 | 0.610459 | -0.096659 |
| H 5 | 2.471627 | 1.339865 | -0.201342 |
| C 6 | -0.489483 | 1.976621 | 0.049423 |
| H 6 | 0.122770 | 0.122770 | -0.136110 |
| H 6 | -1.273002 | 1.926754 | -0.705396 |
| H 6 | -0.978062 | 2.094295 | 1.016643 |
| O | -3.106219 | -0.588991 | -0.141629 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.143797 | -0.634498 | -0.015075 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.475006 | -0.644980 | 0.737299 |

Table A27. $\omega$ B97XD/aug-cc-pVQZ, MP2/aug-cc-pVDZ

| $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.988208 | -0.690030 | -0.056537 |
| H 1 | 2.912514 | -1.100527 | -0.119247 |
| C 2 | 0.810711 | -1.377742 | 0.063179 |
| H 2 | 0.760377 | -2.462908 | 0.102556 |
| N 3 | -0.226208 | -0.537975 | 0.115235 |
| C 4 | 0.304233 | 0.740378 | 0.023893 |
| C 5 | 1.690341 | 0.660192 | -0.084282 |
| H 5 | 2.458685 | 1.423500 | -0.176448 |
| C 6 | -0.572166 | 1.957151 | 0.048599 |
| H 6 | 0.028469 | 2.866755 | -0.101313 |
| H 6 | -1.33614 | 1.899056 | -0.741455 |
| H 6 | -1.097720 | 2.039333 | 1.012754 |
| O | -3.099972 | -0.608227 | -0.133924 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.130426 | -0.677558 | -0.004234 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.468150 | -0.847570 | 0.725421 |

Table A28. 5-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), B3LYP(D3BJ)/aug-cc-pVTZ

| $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.023574 | -1.102553 | 0.012058 |
| H 1 | 1.616286 | -1.913179 | 0.049428 |
| C 2 | -0.337382 | -1.106472 | -0.034833 |
| H 2 | -0.924631 | -2.008638 | -0.035864 |
| N 3 | -0.805450 | 0.116508 | -0.071624 |
| C 4 | 0.295138 | 0.945315 | -0.046934 |
| H 4 | 0.194861 | 2.016657 | -0.064656 |
| C 5 | 1.448845 | 0.211931 | 0.005242 |
| C 6 | 2.882872 | 0.601370 | 0.050214 |
| H 6 | 2.968267 | 1.685872 | 0.035712 |
| H 6 | 3.373556 | 0.240634 | 0.956981 |
| H 6 | 3.437205 | 0.211716 | -0.806557 |
| O | -3.659745 | 0.296181 | 0.106923 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.685398 | 0.326215 | 0.015165 |
| $\mathrm{H}_{\mathrm{nb}}$ | -4.002053 | 0.675593 | -0.706235 |

Table A29. 5-MI ${ }^{\prime} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), $\omega$ B97XD/aug-cc-pVQZ

| $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 1.002383 | -1.098151 | 0.004024 |
| H 1 | 1.573438 | -1.921990 | 0.025376 |
| C 2 | -0.351629 | -1.067247 | -0.024578 |
| H 2 | -0.960065 | -1.956016 | -0.026559 |
| N 3 | -0.794369 | 0.159067 | -0.043840 |
| C 4 | 0.322208 | 0.957079 | -0.026096 |
| H 4 | 0.247986 | 2.031079 | -0.033202 |
| C 5 | 1.454364 | 0.200042 | 0.003646 |
| C 6 | 2.897329 | 0.555415 | 0.031836 |
| H 6 | 3.008467 | 1.637052 | 0.033872 |
| H 6 | 3.389340 | 0.166990 | 0.924735 |
| H 6 | 3.424462 | 0.166183 | -0.840477 |
| O | -3.675852 | 0.269815 | 0.085592 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.707901 | 0.340493 | 0.036971 |
| $\mathrm{H}_{\mathrm{nb}}$ | -3.675852 | 0.269815 | 0.085592 |

Table A30. 5-MI ${ }^{\cdots} \mathrm{H}_{2} \mathrm{O}$ (Chapter 7), MP2/aug-cc-pVDZ

| $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | 0.891780 | -1.101082 | -0.003291 |
| H 1 | 1.378247 | -1.990552 | 0.015246 |
| C 2 | -0.469382 | -0.934760 | -0.036241 |
| H 2 | -1.174721 | -1.762384 | -0.044557 |
| N 3 | -0.788922 | 0.361634 | -0.049753 |
| C 4 | 0.417476 | 1.038700 | -0.024055 |
| H 4 | 0.462654 | 2.125964 | -0.026239 |
| C 5 | 1.488538 | 0.148975 | 0.005180 |
| C 6 | 2.971745 | 0.354561 | 0.040838 |
| H 6 | 3.186265 | 1.432730 | 0.040644 |
| H 6 | 3.421345 | -0.080881 | 0.948322 |
| H 6 | 3.466050 | -0.090285 | -0.838407 |
| O | -3.647949 | 0.153675 | 0.092743 |
| $\mathrm{H}_{\mathrm{b}}$ | -2.707391 | 0.421925 | 0.029209 |
| $\mathrm{H}_{\mathrm{nb}}$ | -4.055775 | 0.545579 | -0.689097 |

Table A31. $\mathrm{H}_{2} \mathrm{O} \cdots 2$-MI (Chapter 8), B3LYP(D3BJ)/aug-cc-pVTZ

| $\mathrm{H}_{2} \mathrm{O} \cdots 2-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.249934 | -0.389696 | -0.000700 |
| H 1 | -1.260937 | -0.391259 | -0.000841 |
| C 2 | 0.554366 | 0.712140 | -0.000035 |
| N 3 | 1.824479 | 0.365086 | 0.000514 |
| C 4 | 1.841629 | -1.011629 | 0.000257 |
| H 4 | 2.765552 | -1.563714 | 0.000577 |
| C 5 | 0.565636 | -1.500189 | -0.000481 |
| H 5 | 0.171544 | -2.500093 | -0.000931 |
| C 6 | 0.030945 | 2.105394 | 0.000014 |
| H 6 | 0.872259 | 2.793120 | 0.000303 |
| H 6 | -0.582389 | 2.305104 | 0.880993 |
| H 6 | -0.581956 | 2.305349 | -0.881215 |
| H | -3.798818 | -0.451262 | -0.768112 |
| O | -3.232170 | -0.335771 | 0.000462 |
| H | -3.797733 | -0.466479 | 0.767398 |

Table A32. $\mathrm{H}_{2} \mathrm{O} \cdots 4$-MI (Chapter 8), B3LYP(D3BJ)/aug-cc-pVTZ

| $\mathrm{H}_{2} \mathrm{O} \cdots 4 \mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.728193 | 0.059688 | -0.002902 |
| H 1 | -1.726551 | -0.101213 | -0.003310 |
| C 2 | -0.104116 | 1.265813 | -0.000782 |
| H 2 | -0.645484 | 2.197070 | -0.000578 |
| N 3 | 1.203090 | 1.136900 | 0.001145 |
| C 4 | 1.449154 | -0.220294 | 0.000323 |
| C 5 | 0.259202 | -0.901207 | -0.002082 |
| H 5 | 0.033063 | -1.952113 | -0.003695 |
| C 6 | 2.836819 | -0.762924 | 0.001703 |
| H 6 | 2.830888 | -1.852476 | 0.002782 |
| H 6 | 3.388220 | -0.423712 | -0.876849 |
| H 6 | 3.387123 | -0.421919 | 0.880229 |
| H | -4.244585 | -0.282076 | -0.763403 |
| O | -3.671119 | -0.387117 | 0.001692 |
| H | -4.236673 | -0.279836 | 0.772355 |

Table A33. $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ (Chapter 8), B3LYP(D3BJ)/aug-cc-pVTZ

| $\mathrm{H}_{2} \mathrm{O} \cdots 5-\mathrm{MI}$ | $a / \AA$ | $b / \AA$ | $c / \AA$ |
| :---: | :---: | :---: | :---: |
| N 1 | -0.249815 | 0.341360 | -0.003985 |
| H 1 | -1.261402 | 0.345219 | -0.005836 |
| C 2 | 0.562048 | 1.437082 | -0.002162 |
| H 2 | 0.174823 | 2.442265 | -0.003785 |
| N 3 | 1.829064 | 1.100229 | 0.001968 |
| C 4 | 1.837627 | -0.277305 | 0.003015 |
| H 4 | 2.758532 | -0.835867 | 0.006099 |
| C 5 | 0.559922 | -0.773858 | -0.000491 |
| C 6 | 0.026559 | -2.162451 | -0.001000 |
| H 6 | 0.851170 | -2.872893 | 0.003830 |
| H 6 | -0.583927 | -2.364095 | -0.884329 |
| H 6 | -0.591992 | -2.361593 | 0.877260 |
| H | -3.774813 | 0.576355 | -0.761188 |
| O | -3.232776 | 0.354250 | 0.001874 |
| H | -3.764169 | 0.571328 | 0.773826 |

Table A34. Diagonalized nuclear quadrupole coupling components $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ for $N-, 2-, 4-$, and $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$.

|  | $\mathrm{N}-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | 2-MI $\cdots \mathrm{H}_{2} \mathrm{O}$ | $4-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | $5-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ | Imid $\cdots \mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{\chi}_{x x}(\mathrm{~N} 1)(\mathrm{MHz})$ | $0.921(95)$ | $1.178(27)$ | $1.07(11)$ | $1.744(75)$ | $1.096(27)$ |
| $\boldsymbol{\chi}_{y y}(\mathrm{~N} 1)(\mathrm{MHz})$ | $1.656(97)$ | $1.496(50)$ | $2.235(96)$ | $1.48(12)$ | $1.332(54)$ |
| $\boldsymbol{\chi}_{z z}(\mathrm{~N} 1)(\mathrm{MHz})$ | $-2.577(29)$ | $-2.673(25)$ | $-2.509(28)$ | $-3.215(79)$ | $-2.428(30)$ |
| $\boldsymbol{\eta}$ | $0.285(53)$ | $0.119(21)$ | $0.464(58)$ | $-0.082(44)$ | $0.097(25)$ |
| $\boldsymbol{\chi}_{x x}(\mathrm{~N} 3)(\mathrm{MHz})$ | $1.837(23)$ | $1.646(25)$ | $1.886(32)$ | $1.44(48)$ | $1.23(19)$ |
| $\boldsymbol{\chi}_{y y}(\mathrm{~N} 3)(\mathrm{MHz})$ | $1.775(49)$ | $1.92(27)$ | $1.474(70)$ | $2.03(20)$ | $1.980(56)$ |
| $\boldsymbol{\chi}_{z z}(\mathrm{~N} 3)(\mathrm{MHz})$ | $-3.612(13)$ | $-3.57(26)$ | $-3.359(12)$ | $-3.46(32)$ | $-3.21(15)$ |
| $\boldsymbol{\eta}$ | $-0.017(15)$ | $0.077(76)$ | $-0.123(23)$ | $0.17(15)$ | $0.234(63)$ |

The calculation of diagonalized nuclear quadrupole coupling components $\chi_{x x}, \chi_{y y}$ and $\chi_{z z}$ of N1 and N3 with QDIAG from experimentally measured values of nuclear quadrupole coupling $\chi_{a a}, \chi_{b b}$ and $\chi_{c c}$ was described in previous chapters. The orientation of the nuclear axes on the individual N nuclei in the imidazole ring follows that described by Christen et al. for the imidazole monomer which was also followed for imid $\cdots \mathrm{H}_{2} \mathrm{O}$ and methylimidazole isomers. The $\chi_{a b}$ values for N1 and N3 for each complex are displayed in the tables 7.1-7.3 in chapter 7.


[^0]:    ${ }^{\text {A }}$ The generalized Hamiltonian is $\widehat{H}=\widehat{H}_{0}+\widehat{H}_{1}$ where $\widehat{H}_{1}$ is the time-dependence of the MW field.

[^1]:    ${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figure.
    ${ }^{\mathrm{b}} N$ and $\sigma_{\text {RMS }}$ are respectively the number of hyperfine transitions and the standard deviation of the fit.

[^2]:    ${ }^{a}$ Numbers in parentheses are one standard deviation in units of the last significant figure. ${ }^{\mathrm{b}}$ The two results shown for each of pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O} \cdots$ imid are those determined for the $0^{-}$and $0^{+}$states respectively. For pyridine $\cdots \mathrm{H}_{2} \mathrm{O}$, values for $k_{s}$ and $v$ were deduced from the spectroscopic parameters determined in the original work of R. B. Mackenzie et al. ${ }^{19}$

[^3]:    a. DFT result calculated at the M06-2X/6-311++G(3df,3pd) level.
    ${ }^{\text {b. }}$ Experimentally-determined $r_{0}$ parameters (this work).

[^4]:    ${ }^{\text {B }}$ Fit for 2-MI was performed by Chris Medcraft and Julianne Heitkämper.

[^5]:    ${ }^{a}$ Values of rotational constants implied by a rigid rotor (RR) geometry and the $r_{\mathrm{s}}$ coordinates of the carbon and nitrogen atoms given in Table 6.5. Internal coordinates that establish the positions of hydrogen atoms are assumed equal to the results of DFT calculations.

[^6]:    ${ }^{\mathrm{c}}$ Fit for $2-\mathrm{MI} \cdots \mathrm{H}_{2} \mathrm{O}$ was performed by Chris Medcraft and Julianne Heitkämper.

[^7]:    ${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
    ${ }^{b}$ Numbers in square brackets fixed to the calculated value at the B3LYP(D3BJ)/aug-ccpVTZ level.
    ${ }^{\mathrm{c}}$ Number of $A$-state hyperfine components included in the fit.
    ${ }^{d}$ Root mean square deviation of the fit.

[^8]:    ${ }^{\text {D }}$ The H atom on the pyrrolic N 1 site in N -MI is replaced by a $\mathrm{CH}_{3}$ group, making that site unavailable for H -bonds.

[^9]:    ${ }^{\text {a }}$ Numbers in parentheses are one standard deviation in units of the last significant figures.
    ${ }^{\mathrm{b}}$ Number of $A$-state hyperfine components included in the fit.
    ${ }^{c}$ Root mean square deviation of the fit.

